

# Sternentstehung - Star Formation

Winter term 2017/2018

Henrik Beuther & Thomas Henning

17.10. Introduction & Overview	(H.B.)
24.10. Physical processes I	(H.B.)
31.10. no Lecture – Reformationstag	(M.L.)
07.11. Physical processes II	(H.B.)
<b>14.11. Molecular clouds as birth places of stars</b>	<b>(H.L.)</b>
21.11. Molecular clouds (cont.), Jeans Analysis	(H.B.)
28.11. Collapse models I	(H.B.)
05.12. Collapse models II	(T.H.)
12.12. Protostellar evolution	(T.H.)
19.12. Pre-main sequence evolution & outflows/jets	(T.H.)
09.01. Accretion disks I	(T.H.)
16.01. Accretion disks II	(T.H.)
23.01. High-mass star formation, clusters and the IMF	(H.B.)
30.01. Planet formation	(T.H.)
06.02. Examination week, no star formation lecture	

**Book: Palla & Stahler (2004) The Formation of Stars, Wileys**

More Information and the current lecture files: [http://www.mpia.de/homes/beuther/lecture\\_ws1718.html](http://www.mpia.de/homes/beuther/lecture_ws1718.html)

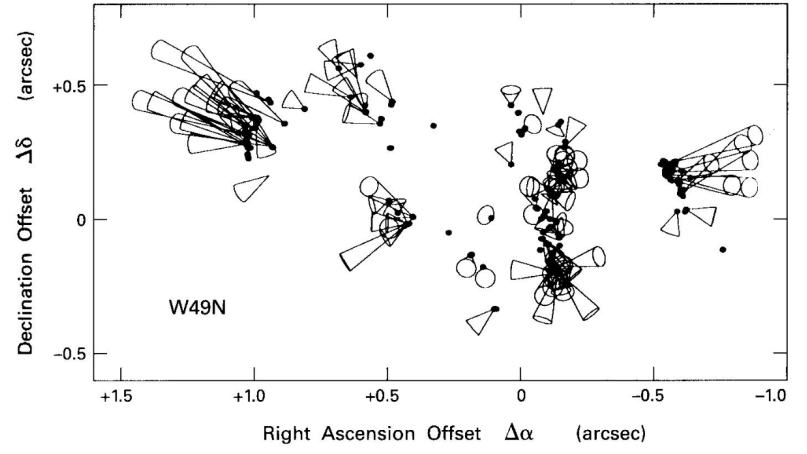
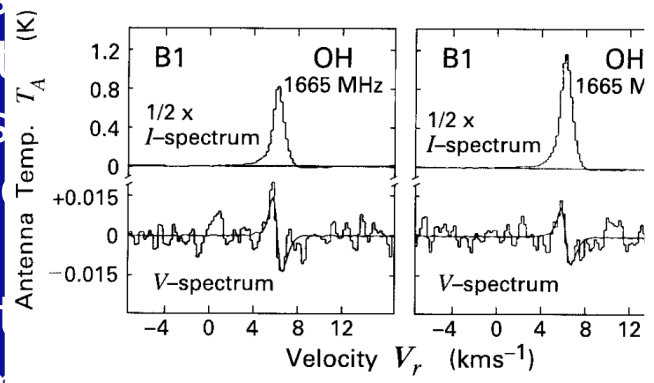
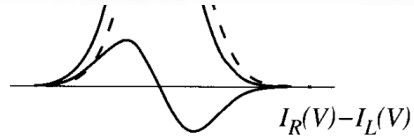
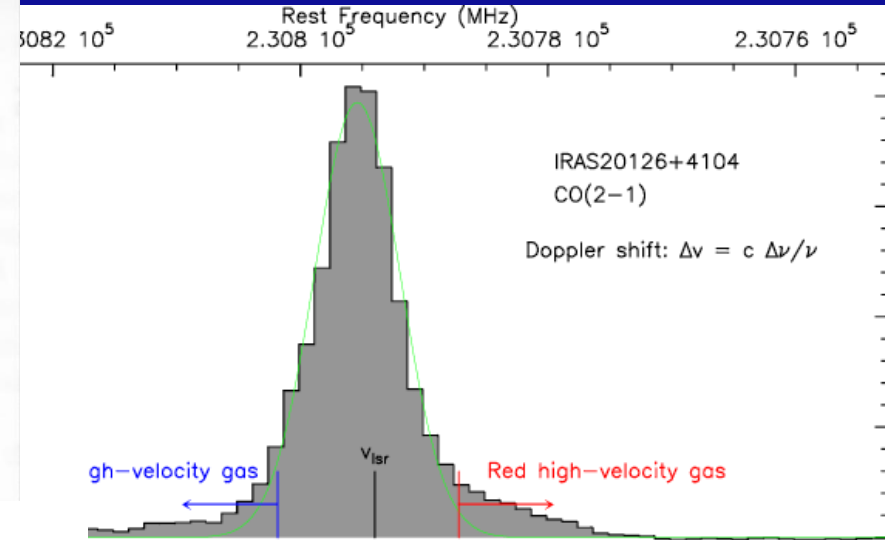
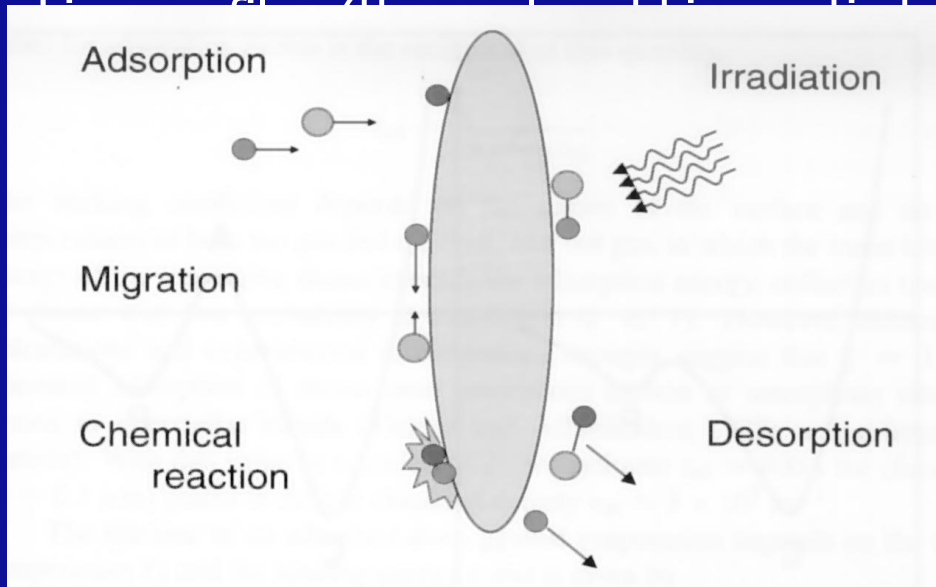
[beuther@mpia.de](mailto:beuther@mpia.de), [henning@mpia.de](mailto:henning@mpia.de)

# Last lecture

- Line profiles (thermal and kinematic broadening) and some applications
- Magnetic fields are very important but difficult to measure:
  - Zeeman effect traces **B** component along line of sight.
  - Dust polarisation traces **B** in plane of the sky.  
(Other magnetic field measurements possible.)
- Masers are non-thermal processes. Good for high spatial accuracy and proper motion studies.
- Dust important from many points of view:
  - Traces warm and cold components of ISM.
  - Important coolant at high densities.
  - Traces magnetic field.
  - Chemical catalyst.
- Physical distributions and their applicability to the ISM.  
(Maxwell, Boltzmann, Planck, Saha)

# Last lecture

(loading) and some applications



- Dust important
  - Traces
  - Important
  - Traces
  - Chemical
  - Physical dist
- (Maxwell, Boltzmann, Planck, Stefan)

# Topics today

- Physical distributions (cont.)
- **Components of the interstellar medium**
- General characteristics of molecular clouds
- Important cloud relations
- Cloud fragmentation

# Historical Models of the ISM (I)

## 1.) Simple Two-Phase Model (Field et al. 1969)

- Underlying idea: equilibrium: heating rate  $\Gamma(n, T) =$  cooling rate  $\Lambda(n, T)$
- Stationary condition  $\rightarrow$  equation of state between dens.  $n$  and temp.  $T$
- Pressure equilibrium  $\rightarrow$  several combinations of  $(n, T)$  are possible (remember ideal gas:  $p = n k T$ )
- Only certain combinations thermally stable (different dependence of  $\Gamma(n, T)$  and  $\Lambda(n, T)$  on the density) ...
- Two phases: a.)  $n < 0.3 \text{ cm}^{-3}$ ,  $T \approx 5000 - 10000 \text{ K}$  (thin, warm, ionised)  
b.)  $n \approx 50 \text{ cm}^{-3}$ ,  $T \approx 80 - 100 \text{ K}$  (dense, cold, neutral)

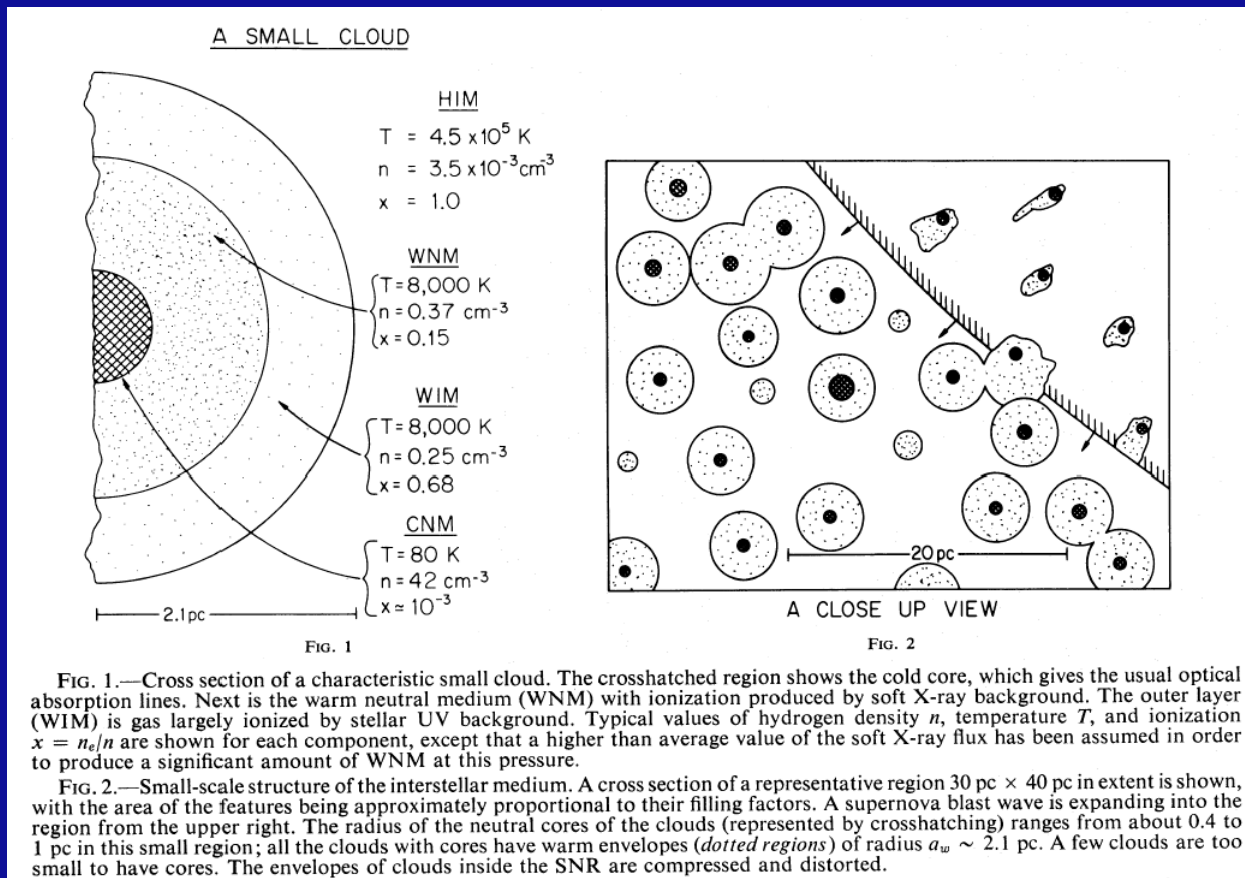
**BUT:** maintaining 80 – 100 K in dense gas with cosmic-ray heating difficult  
needed ionisation rate:  $10^{-15} \text{ s}^{-1}$ , observed (Copernicus UV satellite):  $10^{-17} \text{ s}^{-1}$

warm (inter-cloud) gas not observed in this way ...

# Historical Models of the ISM (II)

## 2.) Three-Phase Model (McKee & Ostriker 1977)

Takes into account hot component of ISM and supernova blast waves. Model is more dynamical and coupled to the formation (and death) of massive stars



# Historical Models of the ISM (III)

## 2.) Three-Phase Model (McKee & Ostriker 1977)

Shortcomings in the original model:

- SN rate and SN "luminosity" overestimated, SNe not arbitrarily distributed
- Clouds are not round, but mostly elongated, layered and filamentary
- Observations indicate considerable amount of evenly distributed (i.e., not bound to clouds) warm HI gas

General comments:

- Model still assumes global pressure equilibrium between the phases
- One very important component still missing: **molecular clouds !!**  
( $T \approx 10 \text{ K}$ ,  $n > 300 \text{ cm}^{-3}$ )

Phase transitions are possible (e.g., by heating and cooling)

Diffuse clouds  $\longrightarrow$  molecular clouds  $\longrightarrow$  stars

# Historical Models of the ISM (III)

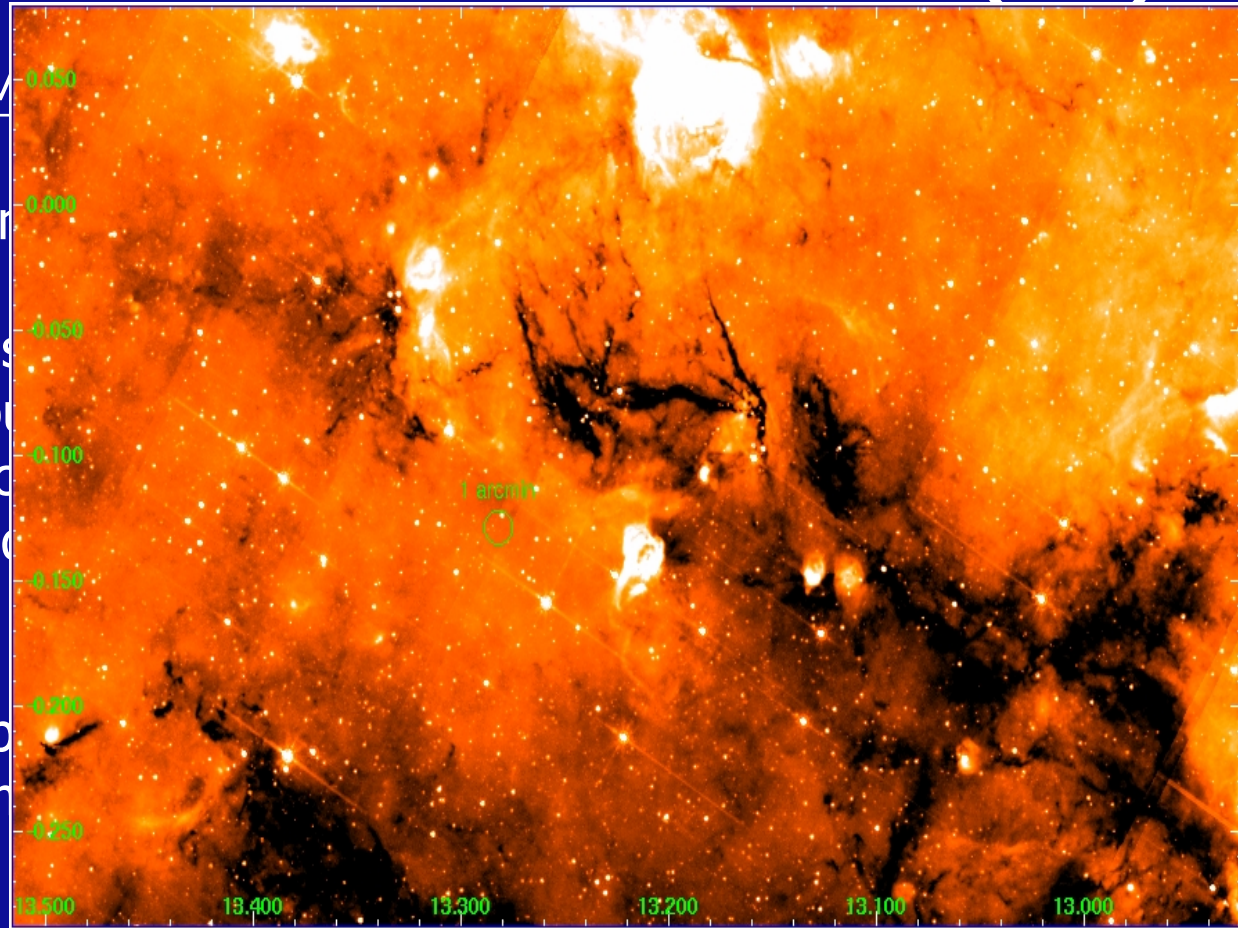
## 2.) Three-Phase Model (M

Shortcomings in the origin

- SN rate and SN "luminos
- Clouds are not round, b
- Observations indicate c
- (i.e., not bound to clou

General comments:

- Model still assumes glob
- One very important com



Phase transitions are possible (e.g., by heating and cooling)

Diffuse clouds → molecular clouds → stars



### 3.) Overview of the components

Phase	$n$ [cm <sup>-3</sup> ]	$T$ [K]	$f$	$M$ [10 <sup>9</sup> M <sub>⊙</sub> ]
Hot ionised medium	0.003	10 <sup>6</sup>	0.5	0.1
Warm neutral medium	0.5	8000	0.4	1.4
Warm ionised medium	0.3	8000	0.1	1.0
<b>Diffuse HI clouds</b>	<b>50</b>	<b>80</b>	-	<b>2.5</b>
<b>Molecular clouds</b>	<b>&gt;300</b>	<b>10</b>	-	<b>2.5</b>
<b>HII regions</b>	<b>1 – 10<sup>5</sup></b>	<b>10<sup>4</sup></b>	-	<b>0.05</b>

$f$  as volume filling factor regarding the Galactic disk

### 3.) Overview of the components

Phase

$n$  [ $\text{cm}^{-3}$ ]

$T$  [K]

$f$

$M$  [ $10^9 M_{\odot}$ ]

Hot ion

Warm

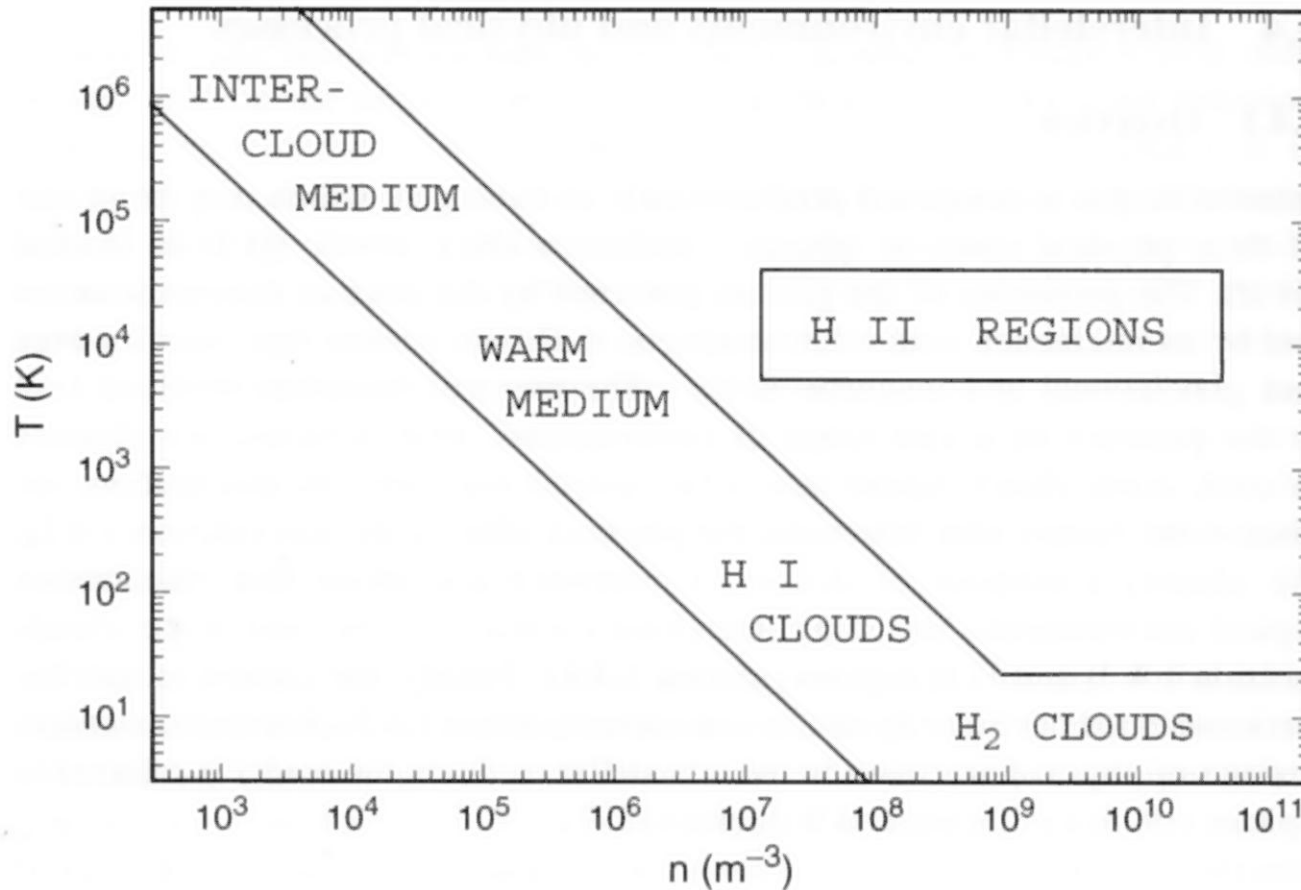
Warm

Diffuse

Molecu

HII reg

$f$  as vo

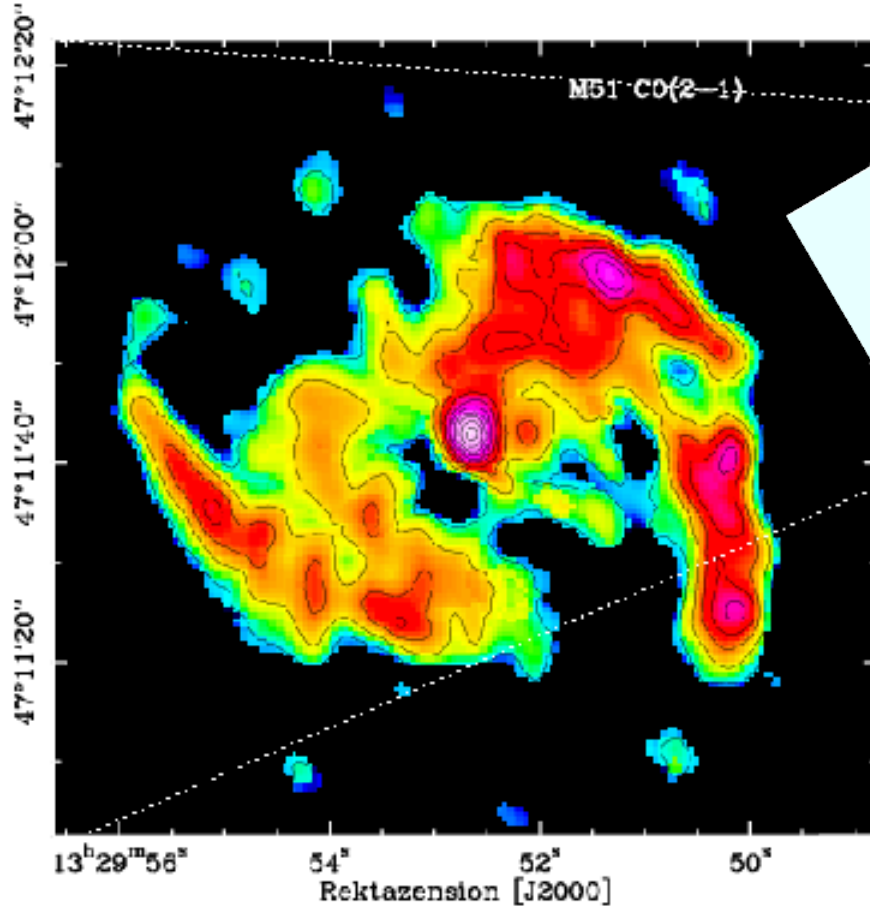


# Topics today

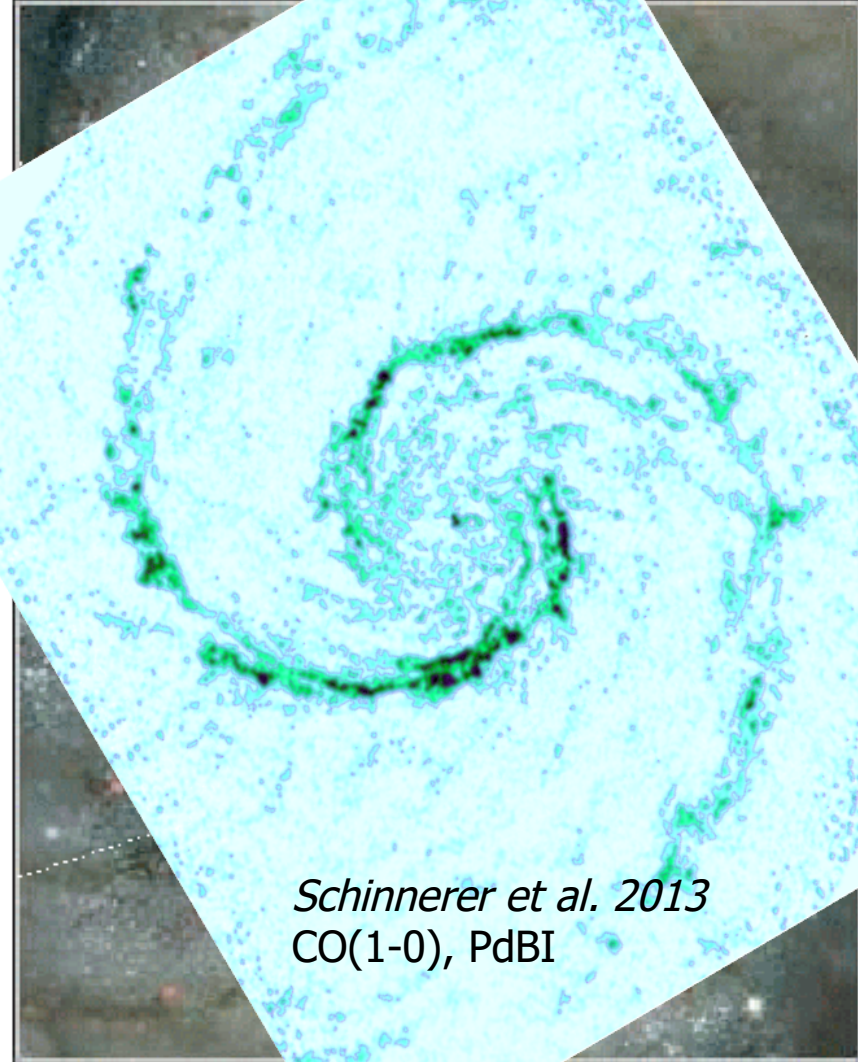
- Physical distributions (cont.)
- Components of the interstellar medium
- **General characteristics of molecular clouds**
- Important cloud relations
- Cloud fragmentation

# M51: The Whirlpool Galaxy

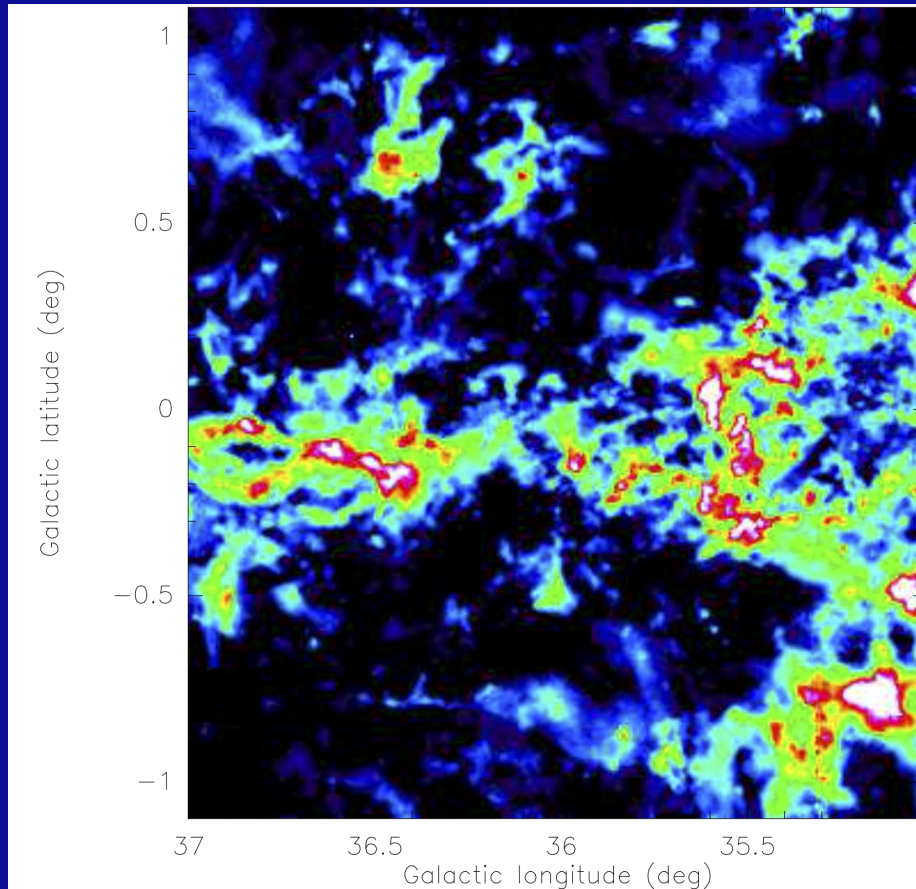
Deklination [J2000]



*Matsushita et al. 2004*



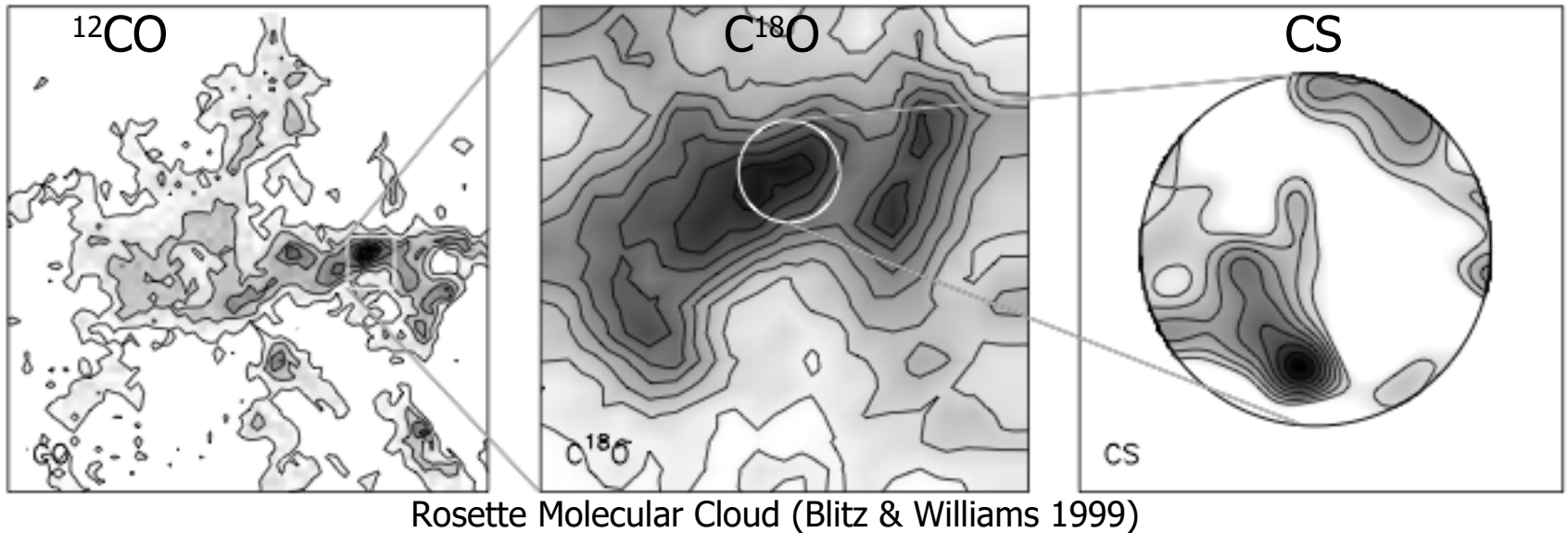
# Giant Molecular Clouds



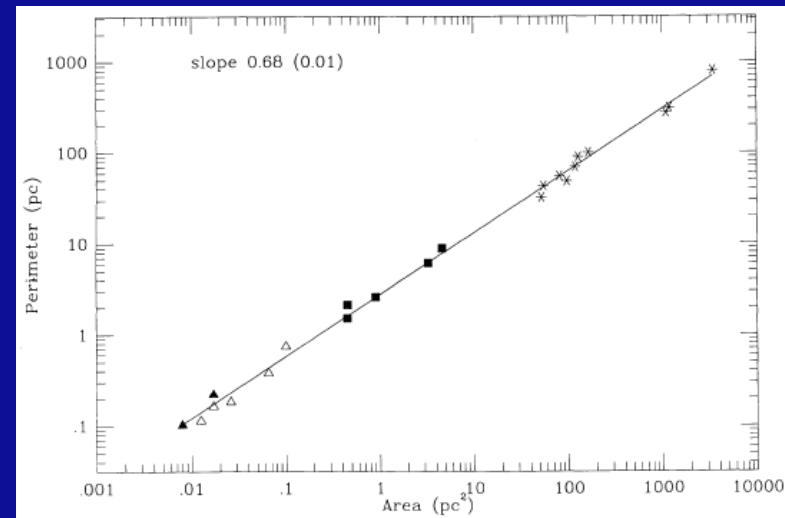
Galactic Ring survey  
 $^{13}\text{CO}(2-1)$   
Jackson et al. 2006

Sizes: 20 to 100pc; Masses:  $10^4$  to  $10^6 M_{\text{sun}}$ ; Temperatures: 10 to 20K  
Supersonic velocity dispersion  $\sim 2-3$  km/s mainly due to turbulence  
Magnetic field strengths on the order of  $10\mu\text{G}$   
Average local densities  $\sim 10^4\text{cm}^{-3}$ ; Volume-averaged densities  $\sim 10^2\text{cm}^{-3}$   
--> highly clumped material

# Hierarchical cloud structure



- Clouds are fractal and self-similar over many orders of magnitude in spatial scale (from 100pc to 0.1pc, Falgarone et al. 1991)
- Also independent of star-forming or non-star-forming clouds
- Remember predominantly used nomenclature: Clouds  $\rightarrow$  Clumps  $\rightarrow$  Cores (e.g., Williams, Blitz & McKee 2000, PPIV)
- Fractal dimension of perimeter  $P$  and area  $A$ :  $P \sim A^{D/2} \rightarrow D \sim 1.4$



# Fine-structure of Molecular clouds

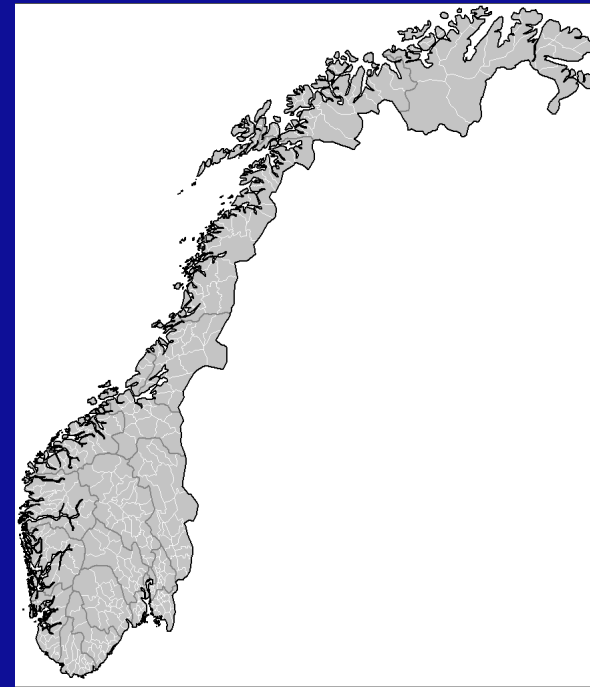
- Fractal dimension  $P \sim A^{D/2} \rightarrow D \sim 1.4$  for some molecular clouds

Ireland



East coast:  $D = 1.10$   
West coast:  $D = 1.26$   
Average:  $D = 1.22$

Norway



Average:  $D = 1.52$

# Fine-structure

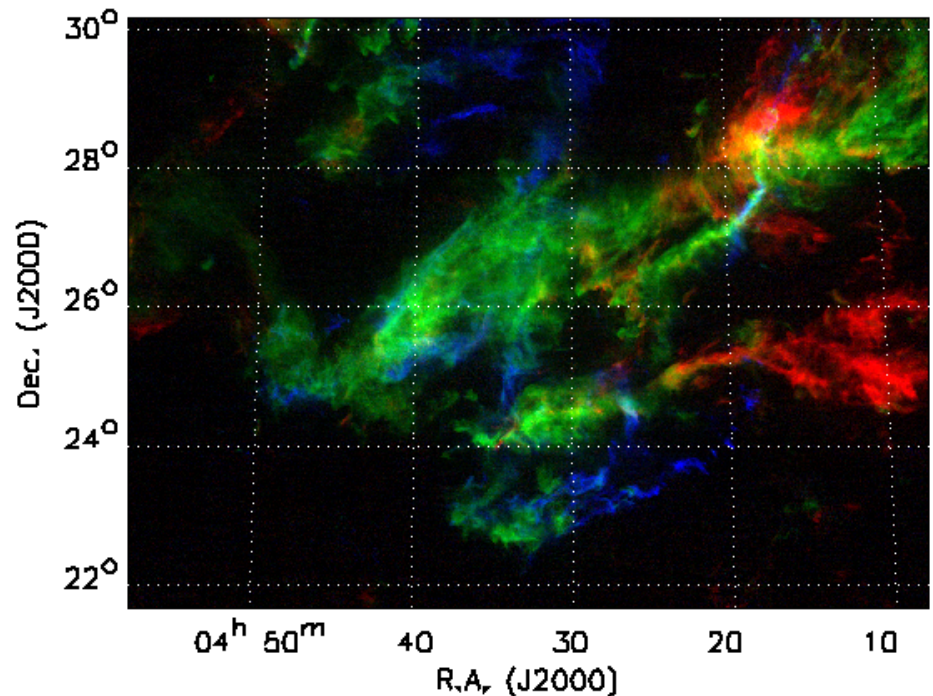
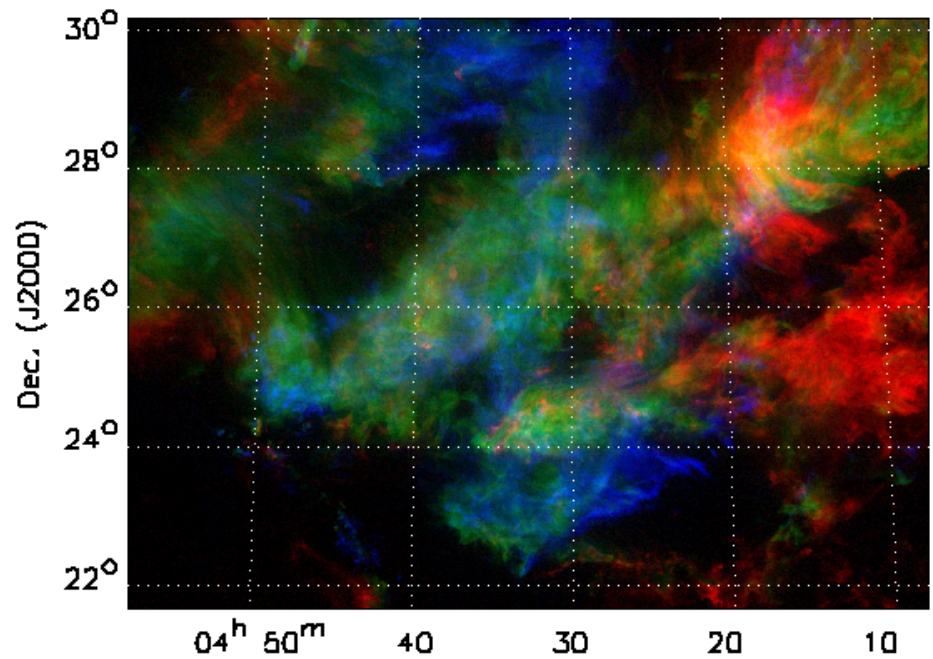
- Fractal dimension  $P \sim A^{D/2}$   
→  $D \sim 1.4$  for some molecular clouds ... probably quite dependent on observational capabilities

Shown is the Taurus molecular Cloud.  $M \sim 2.4 \times 10^4 M_{\text{sun}}$

Top:  $^{12}\text{CO}$  (1-0) with three distinct velocity components (in blue, green, red)

Down: The same in  $^{13}\text{CO}$ (1-0)

Source: Goldsmith et al. 2008,  
ApJ 680, 428

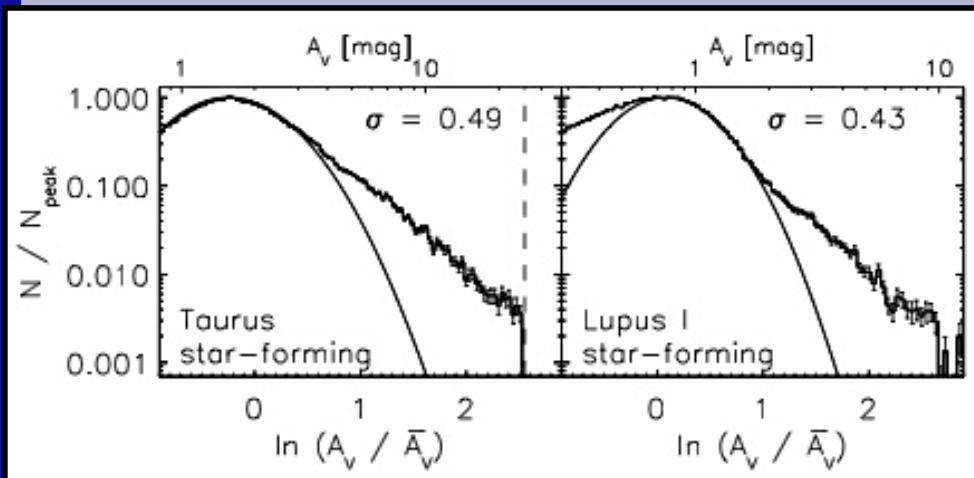
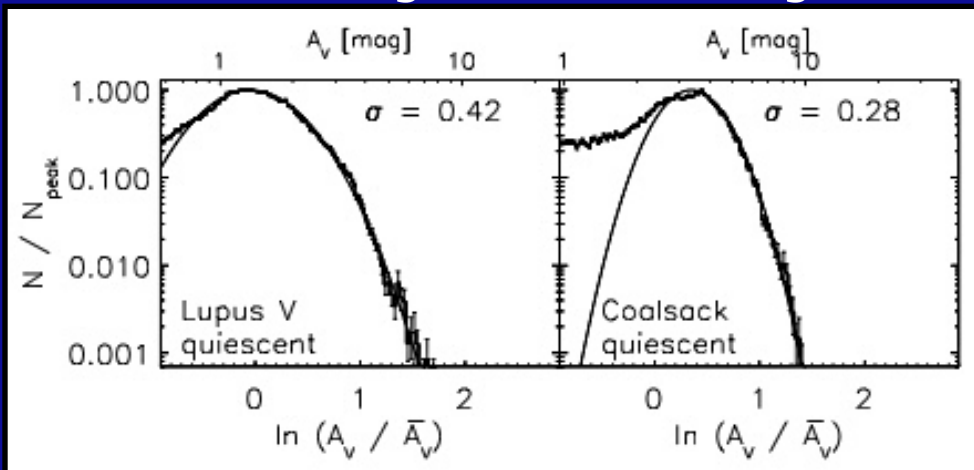




# Probability density distributions (PDFs)

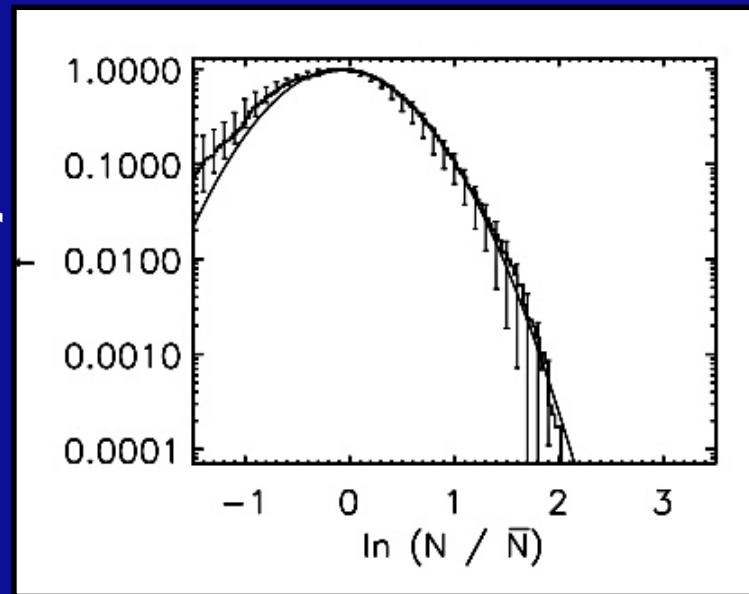
Non-star-forming vs. star-forming clouds

Observed distributions



Typical prediction for turbulent media

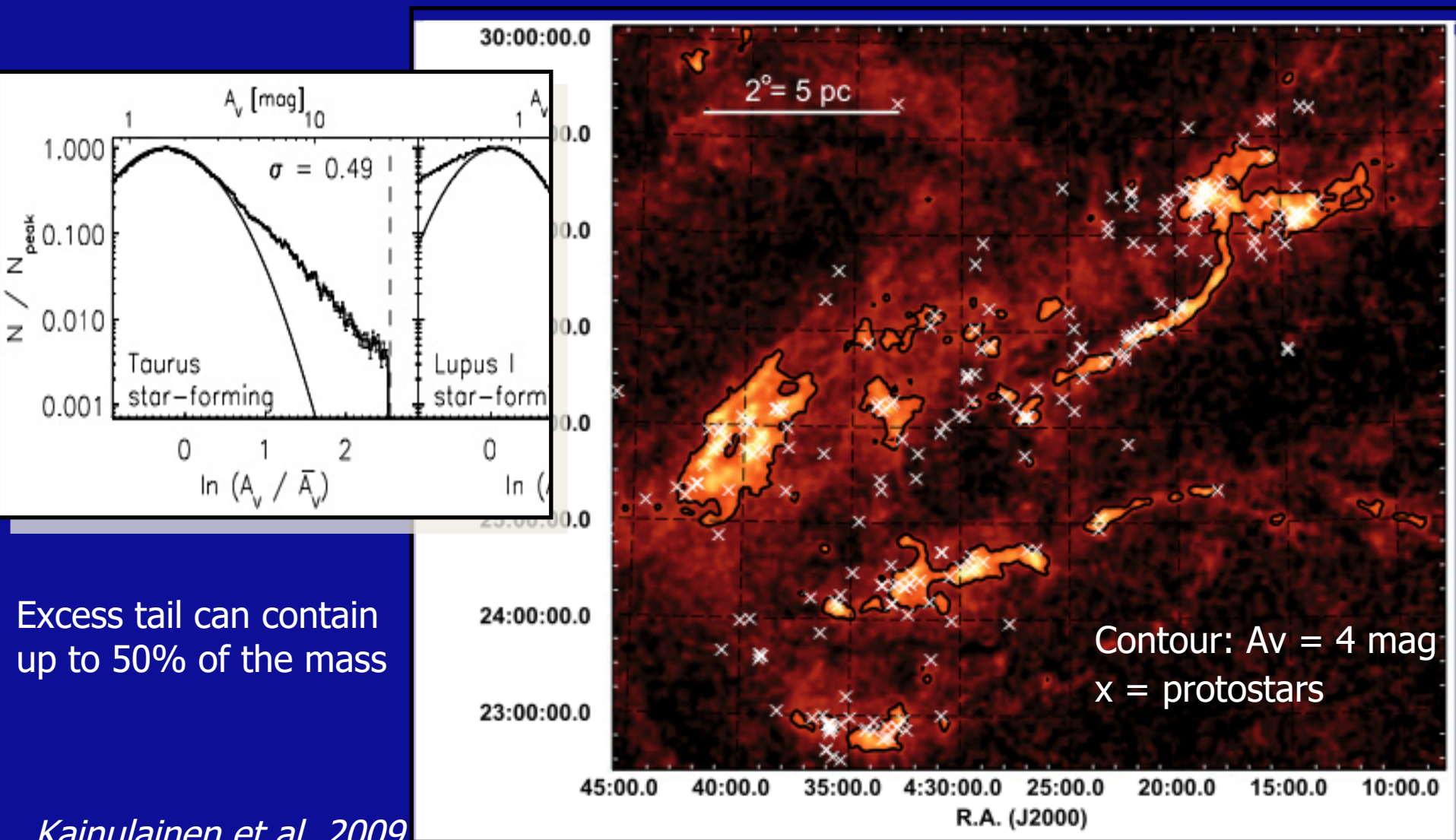
Probability



- non-star-forming: log-normal
- star-forming: high column density excess

# Correlation of "tail" with star formation

## Dust column density in Taurus, logarithmic color scale

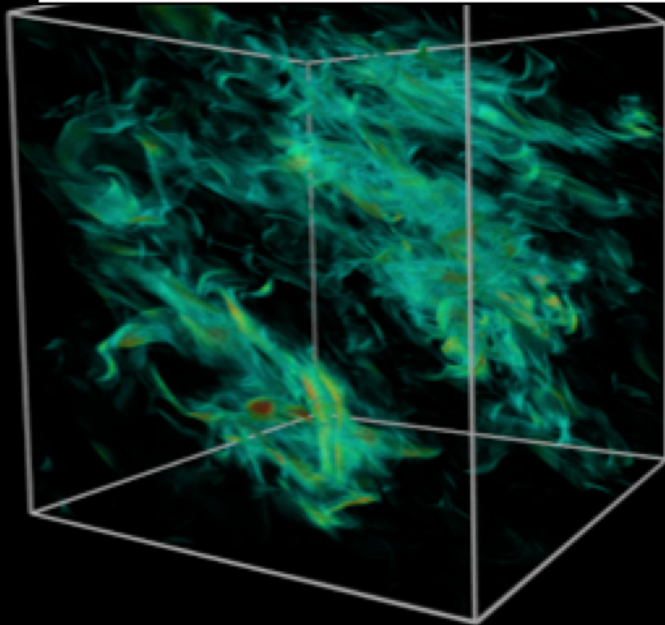


Excess tail can contain up to 50% of the mass

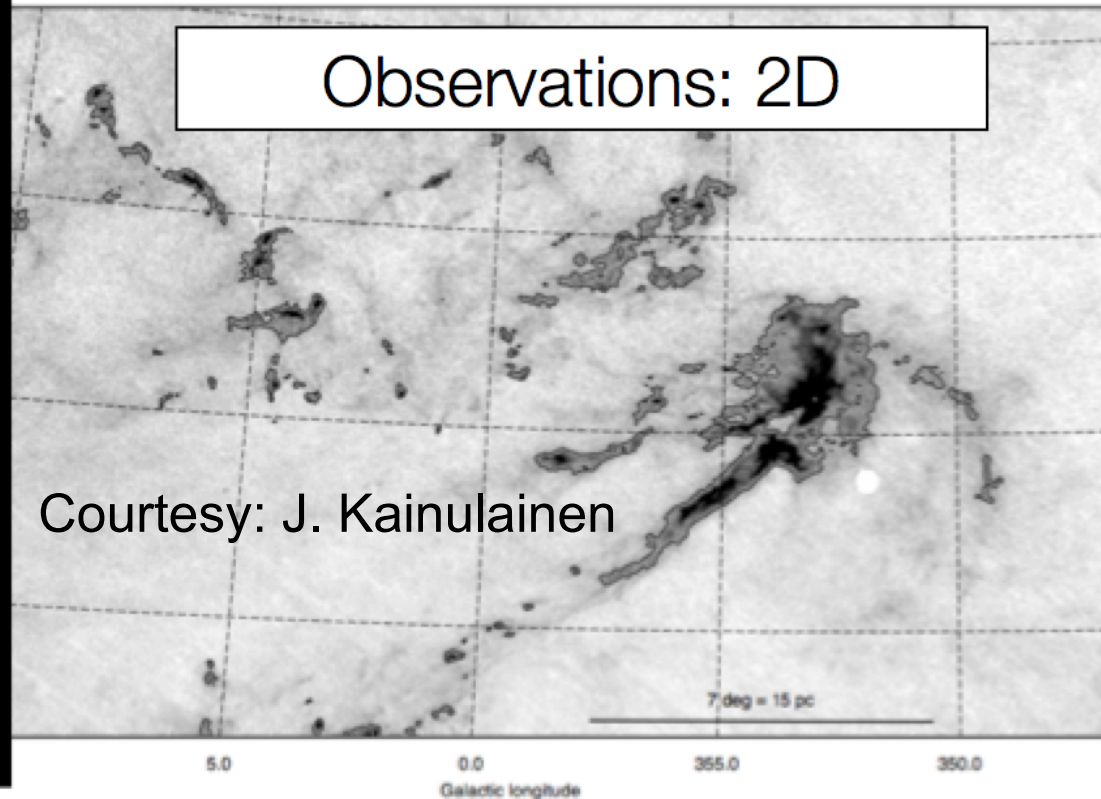
# The 3D structure of molecular clouds?

- Observations only probe *column* densities, but theories deal with *volume* densities.
- How to estimate the 3-dimensional structure?

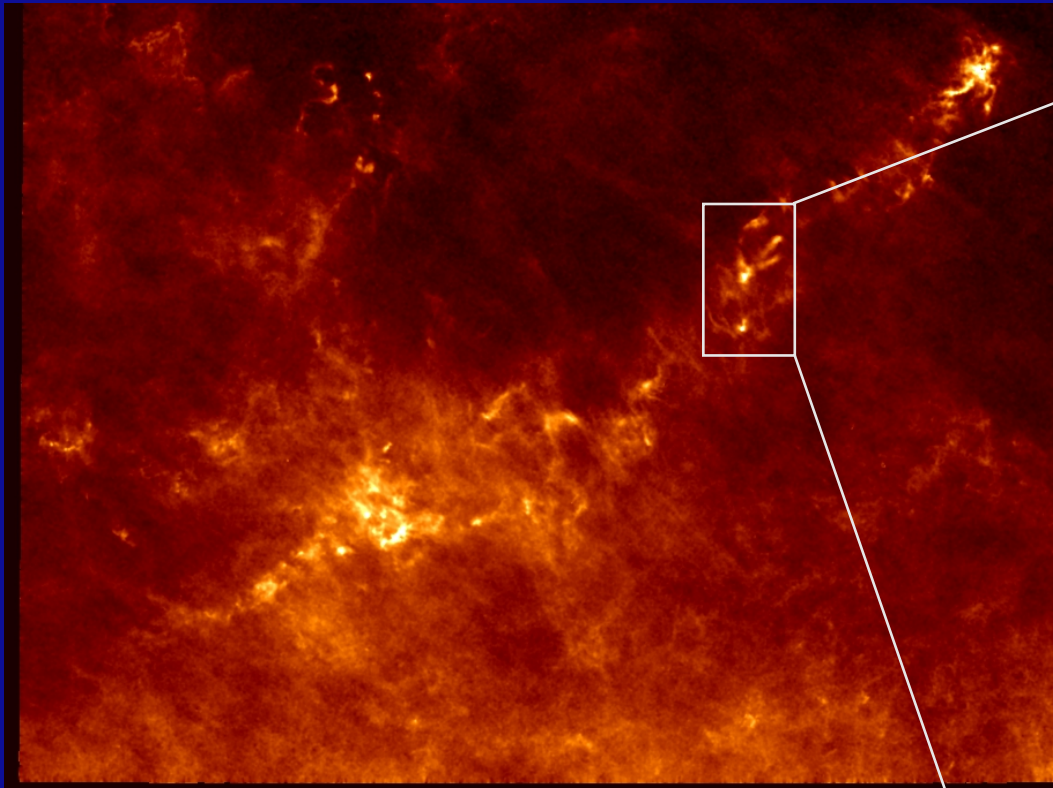
Theory: 3D



Observations: 2D

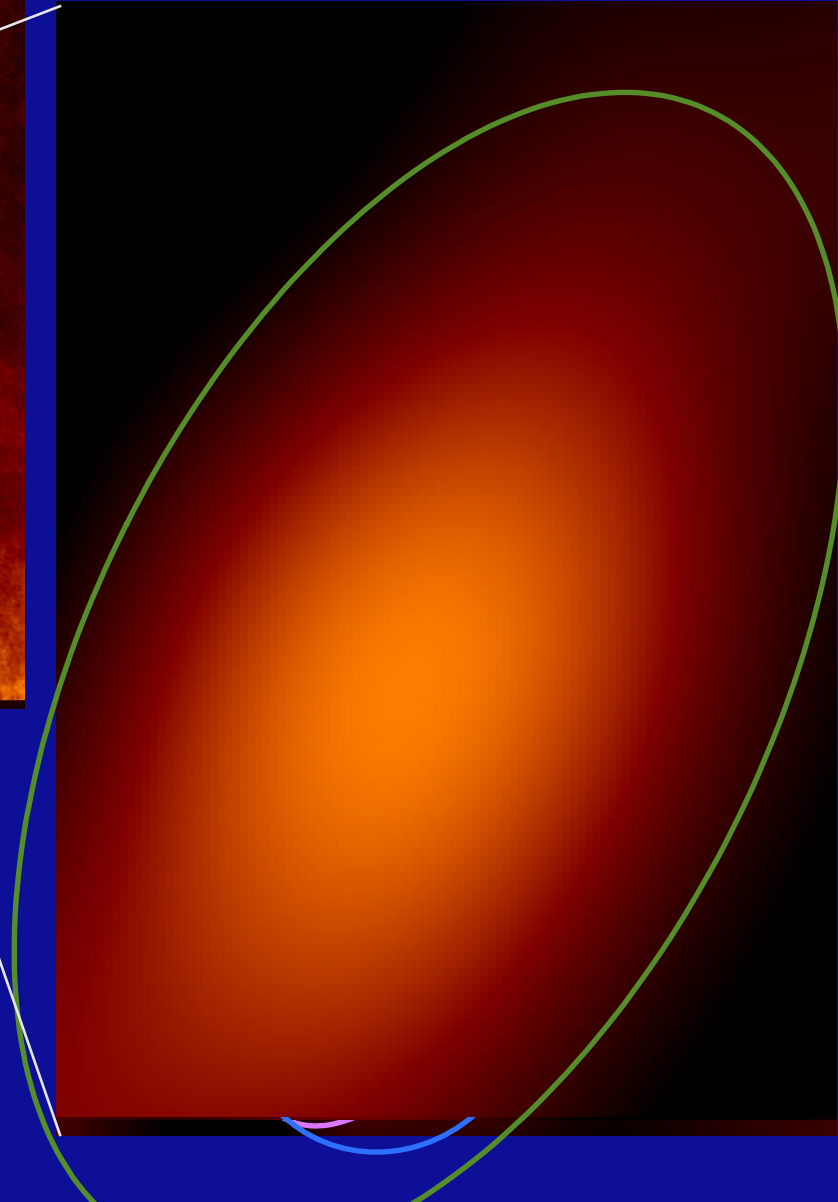


# The 3D structure of molecular clouds?

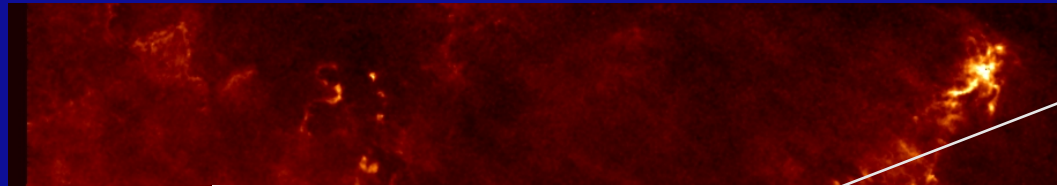


Column density map

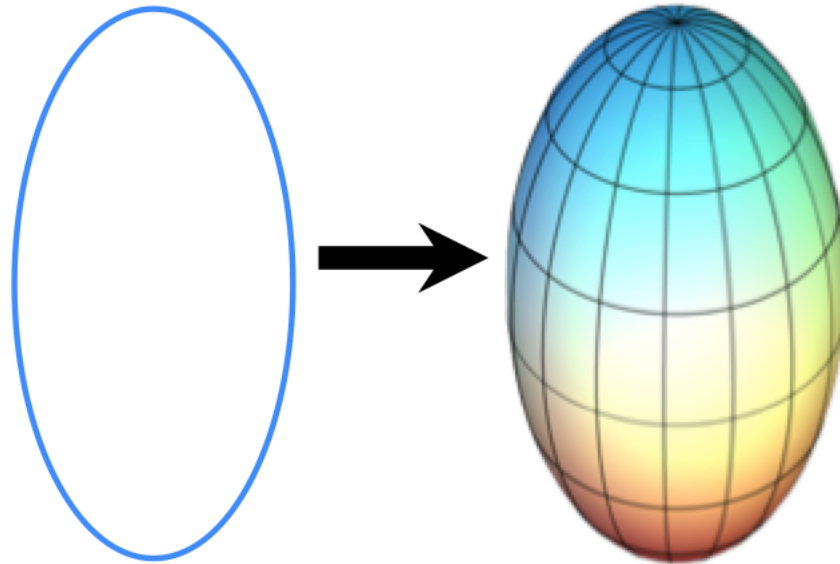
Scale decomposition  
and object recognition



# The 3D structure of molecular clouds?



prolate spheroid



Column

Scale decomposition  
and object recognition



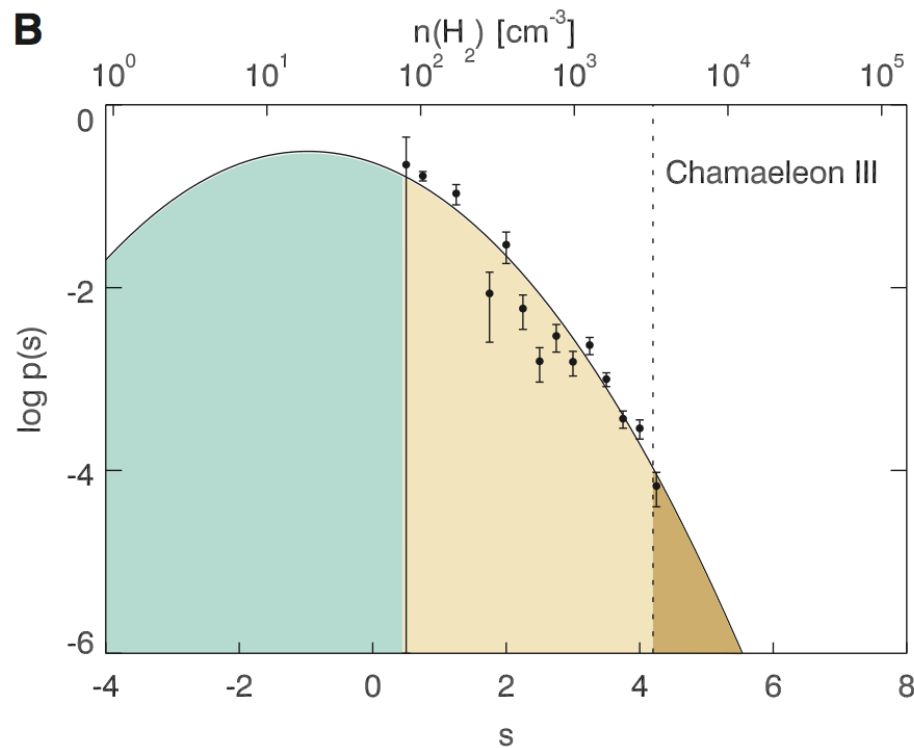
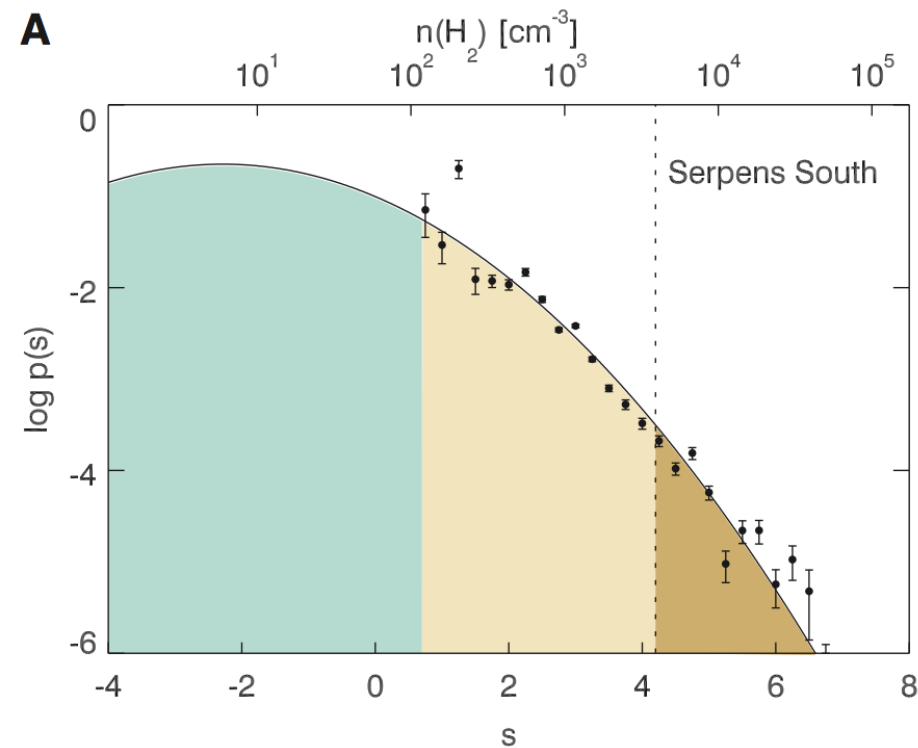
# → Density PDFs

Based on sample of Gould-Belt clouds

Dark brown: star-forming gas

light brown: structures enveloping star-forming gas

Green: non-structured gas



- Direct comparison with theory
- Star formation density threshold  $\rightarrow 5 \times 10^3 \text{ cm}^{-3}$

# Topics today

- Physical distributions (cont.)
- Components of the interstellar medium
- General characteristics of molecular clouds
- Important cloud relations
- Cloud fragmentation

# A GMC in virial equilibrium

Shortest version of virial theorem (next week):  $2T = -W$

(T kinetic energy, W gravitational energy)

$$2T = 2 * (1/2 m \Delta v^2) = -W = Gm^2/r$$

$$\rightarrow \text{virial velocity: } v_{\text{vir}} = (Gm/r)^{1/2}$$

$$\rightarrow \text{or virial mass: } m_{\text{vir}} = v^2 r / G$$

Keep in mind that this version of the virial theorem is a strong simplification and only valid if no magnetic energy is important, and if the cloud is in isolation (without important surface terms).

In its full(er) glory, the virial theorem would be like:

$$\begin{aligned} \frac{1}{2} \ddot{I}_L = & \int_V (3P_{\text{th}} + \rho v^2) dV - \int_S P_{\text{th}} \mathbf{r} \cdot d\mathbf{S} + \frac{1}{8\pi} \int_V B^2 dV \\ & + \frac{1}{4\pi} \int_S \mathbf{r} \cdot \left( \mathbf{B}\mathbf{B} - \frac{1}{2} B^2 \mathbf{I} \right) \cdot d\mathbf{S} + \int_V \rho \mathbf{r} \cdot \mathbf{g} dV \end{aligned}$$

From: McKee  
& Zweibel 1992,  
ApJ 399, 551



# Luminosity-mass relation

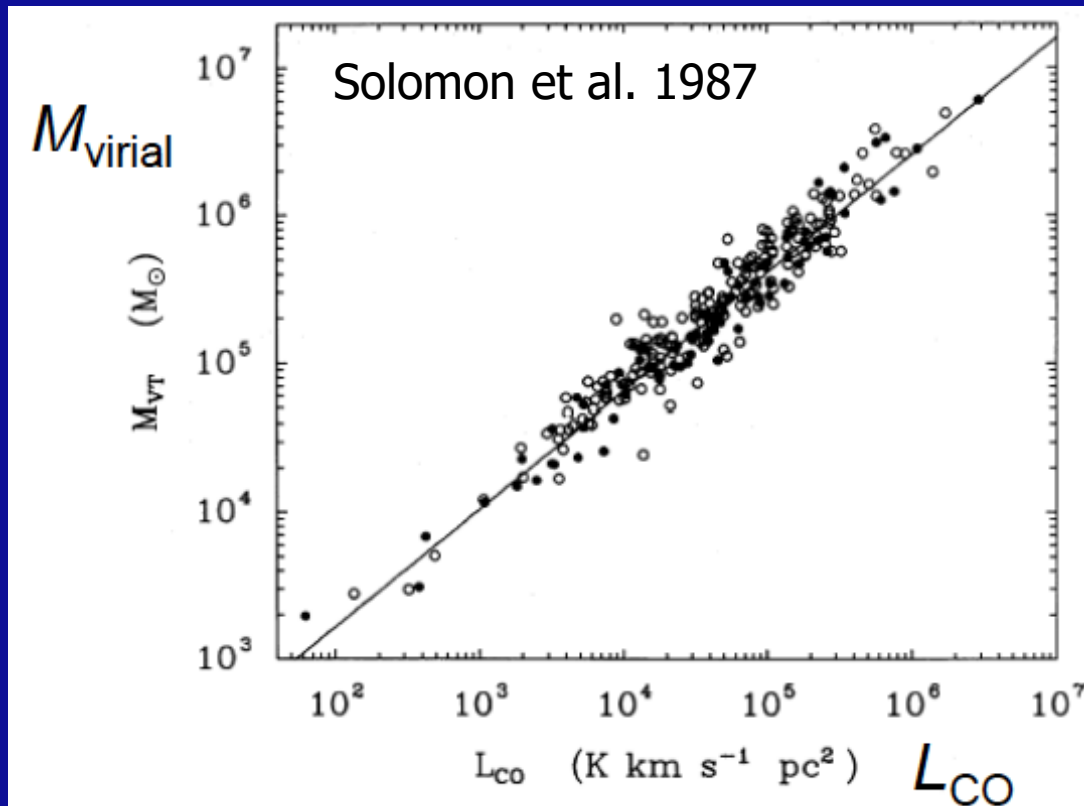
Integrated CO intensity:  $I_{\text{CO}} = \int T(v)dv$

$$\text{CO luminosity } L_{\text{CO}} = T \Delta v \pi r^2$$

( $T$  brightness temperature,  $\Delta v$  linewidth,  $r$  cloud radius)

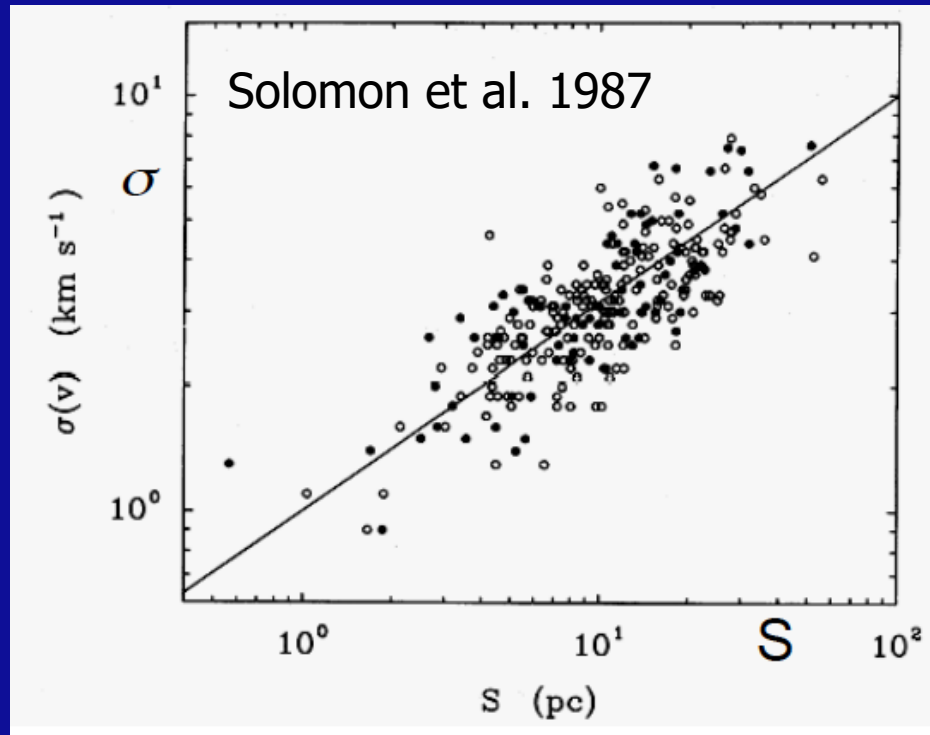
Substituting  $v = (Gm/r)^{1/2}$  and mass  $m = 4/3\pi r^3 \rho$

$$\rightarrow L_{\text{CO}} = (3\pi G/(4\rho))^{1/2} T m$$



Supports assessment that GMCs are in virial equilibrium.

# The linewidth-size relation



- Linewidth-size relation first found by Larson 1981 (Thermal CO linewidth at 20K only  $\approx 0.1$  km/s)
- Approximate relation: linewidth  $\approx \sqrt{\text{size}}$
- Extends over many orders of magnitude in size but not down to cores
- Implies strong turbulent contribution to the ISM

# Additional relations

- Linewidth-size relation:  $\Delta v \approx r^{1/2}$
- Virial equilibrium:  $\Delta v \approx (Gm/r)^{1/2} \rightarrow m = (\Delta v)^2 r/G$

This leads to other relations:

$\rightarrow m = r^2/G \rightarrow m/r^2 = \text{constant} \rightarrow$  approximate constant column density  $N$  in GMCs

$\rightarrow \rho \approx m/r^3 \approx (\Delta v)^2/G * 1/r^2$

Some average empirical values for GMCs:

$$N \approx 1.5 \times 10^{22} \text{ cm}^{-2}$$

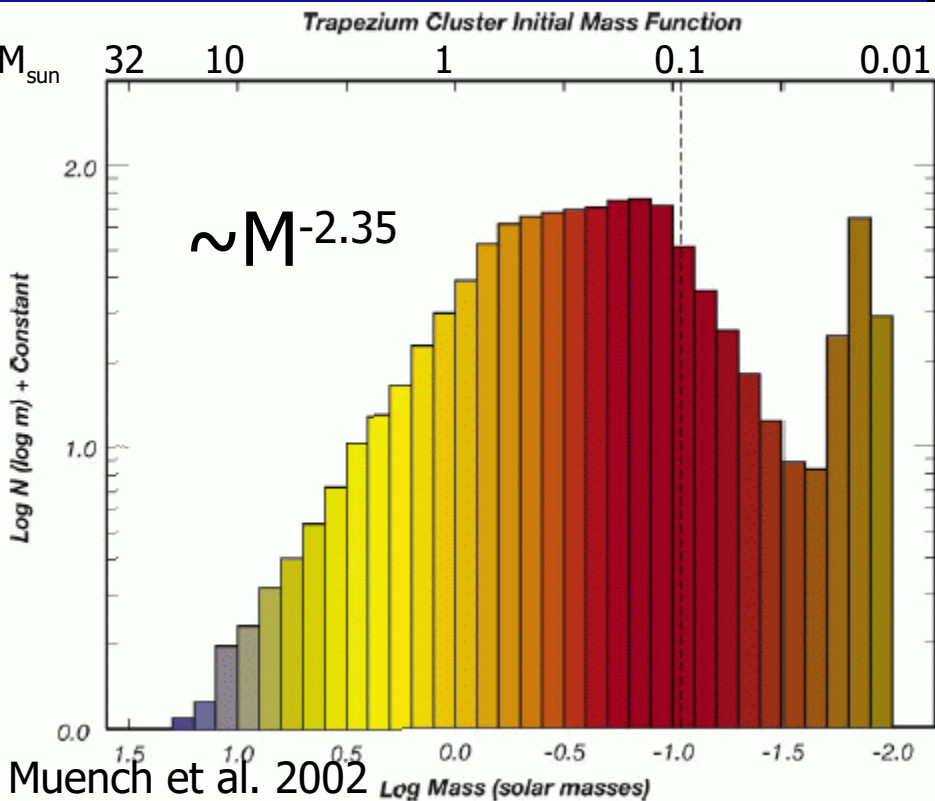
$$A_v \approx 10 \text{ mag}$$

$$\Sigma \approx 150 M_{\text{sun}} \text{ pc}^{-2}$$

# Topics today

- Physical distributions (cont.)
- Components of the interstellar medium
- General characteristics of molecular clouds
- Important cloud relations
- **Cloud fragmentation**

# Clusters and the Initial Mass Function (IMF)



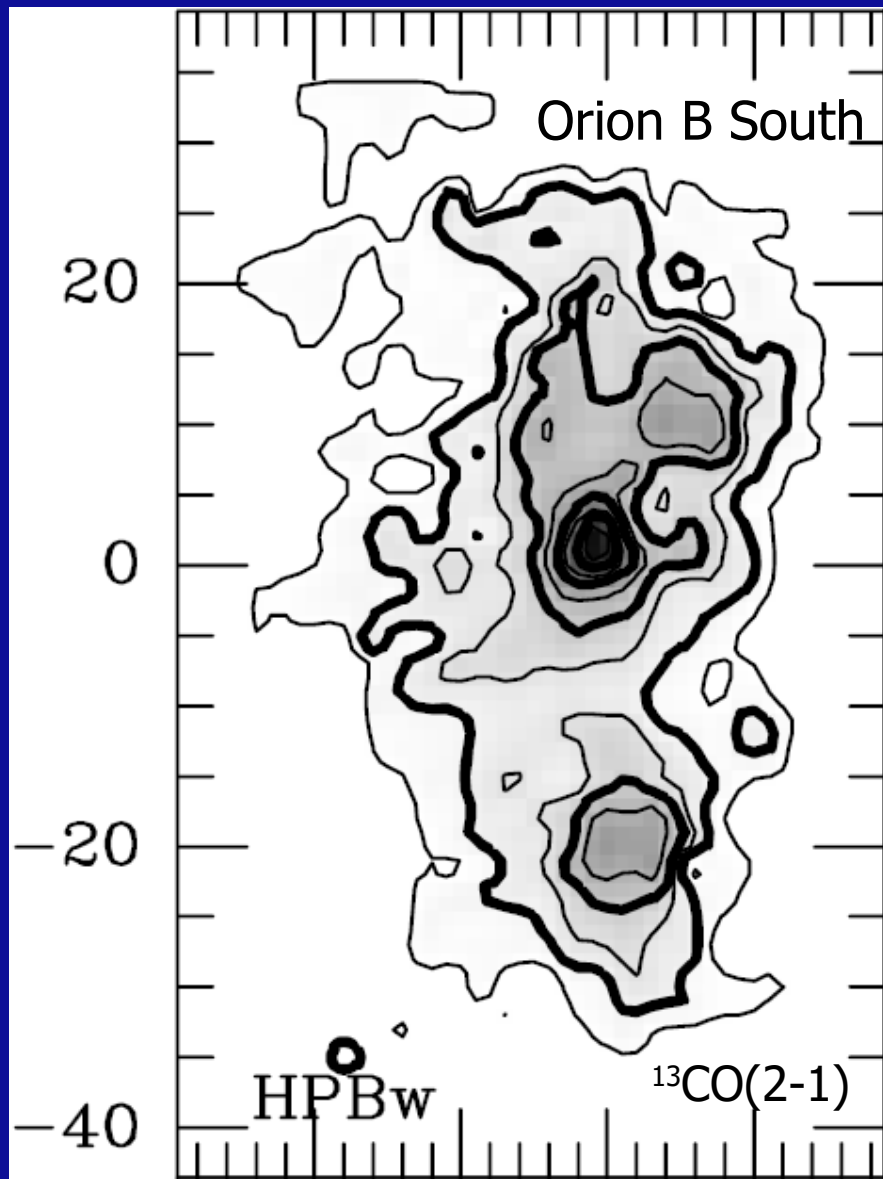
**Orion Nebula**

Subaru Telescope, National Astronomical Observatory of Japan

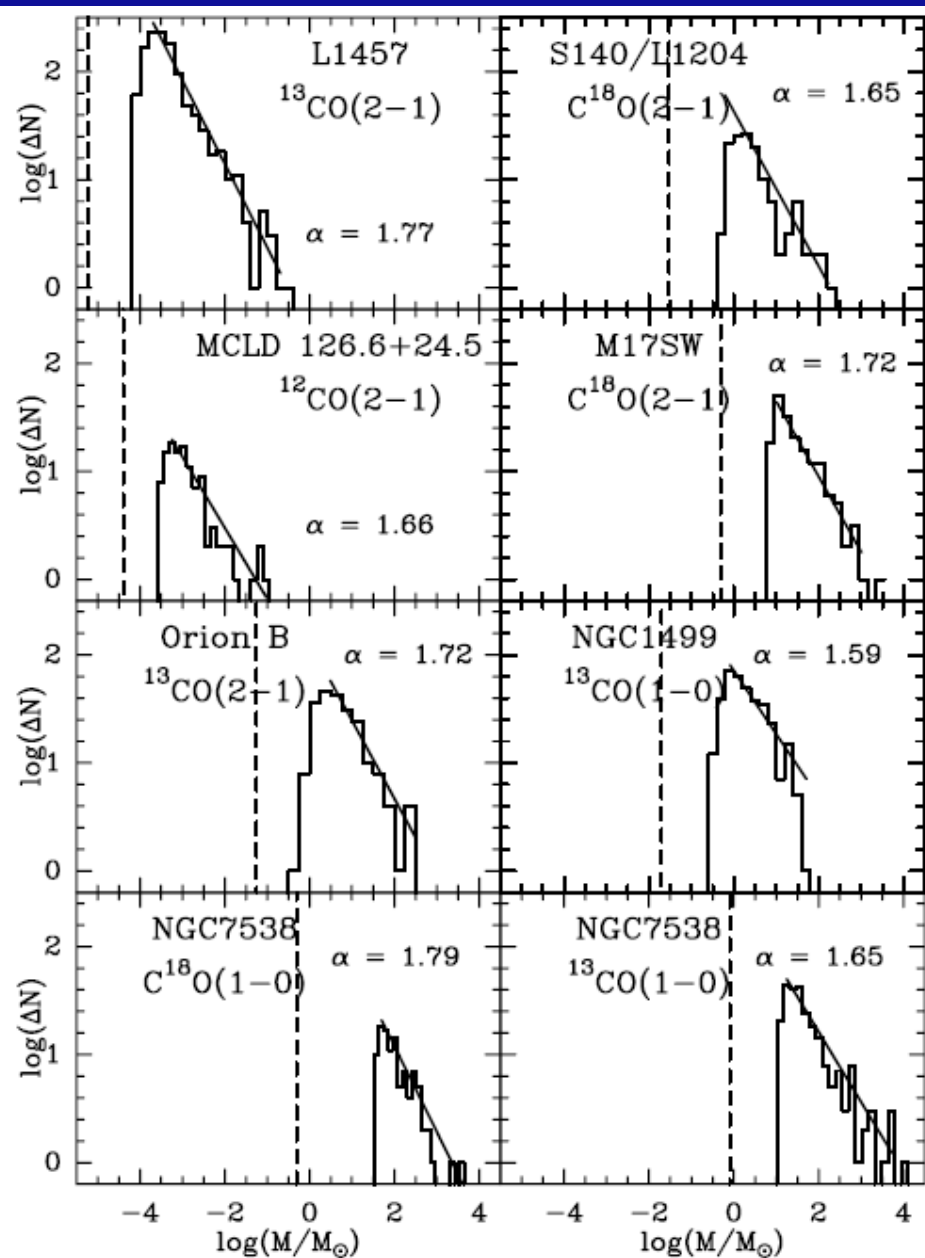
CISCO (J, K' & H<sub>2</sub> ( $v=1-0$  S(1)))

January 28, 1999

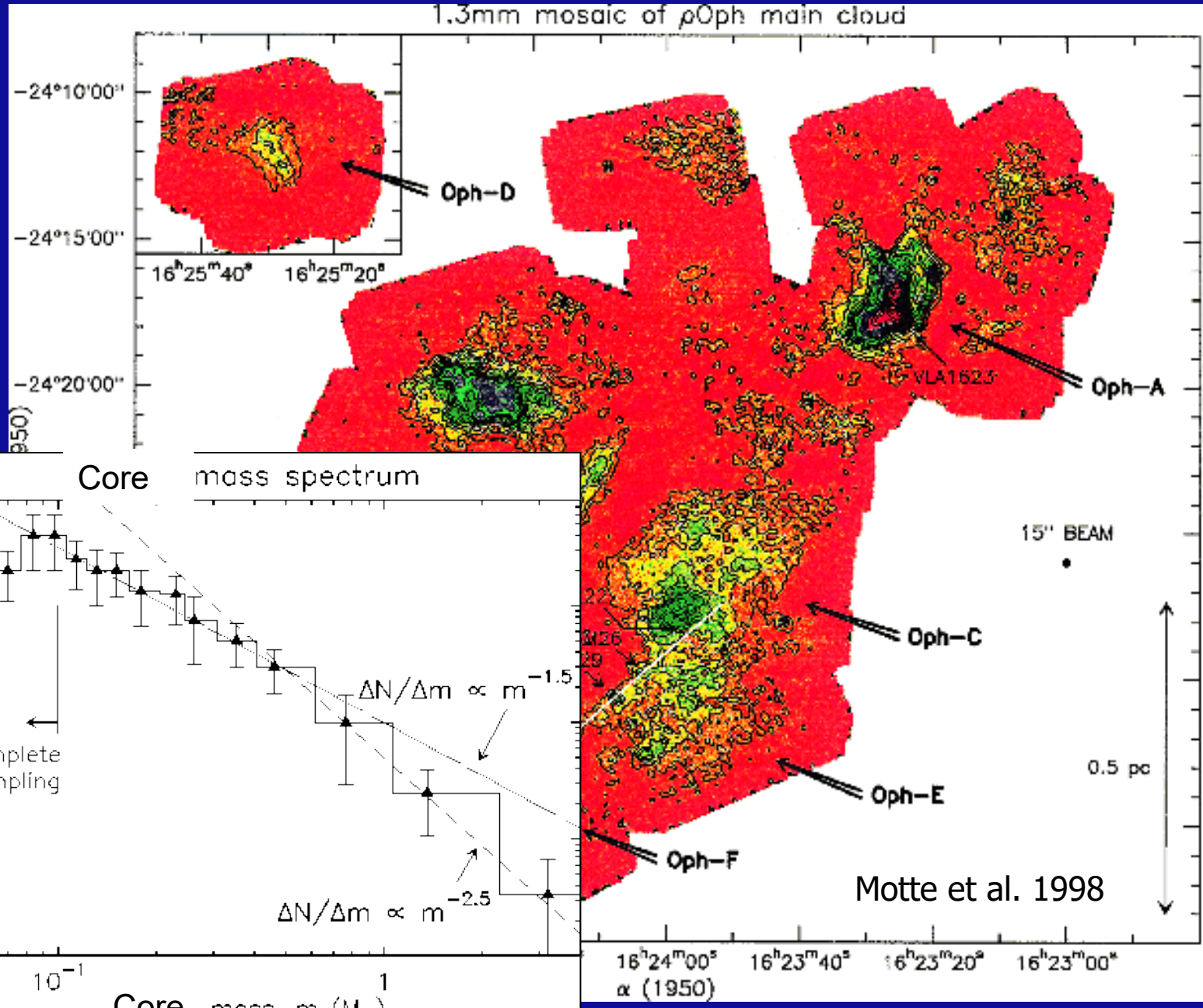
# Cloud mass distributions



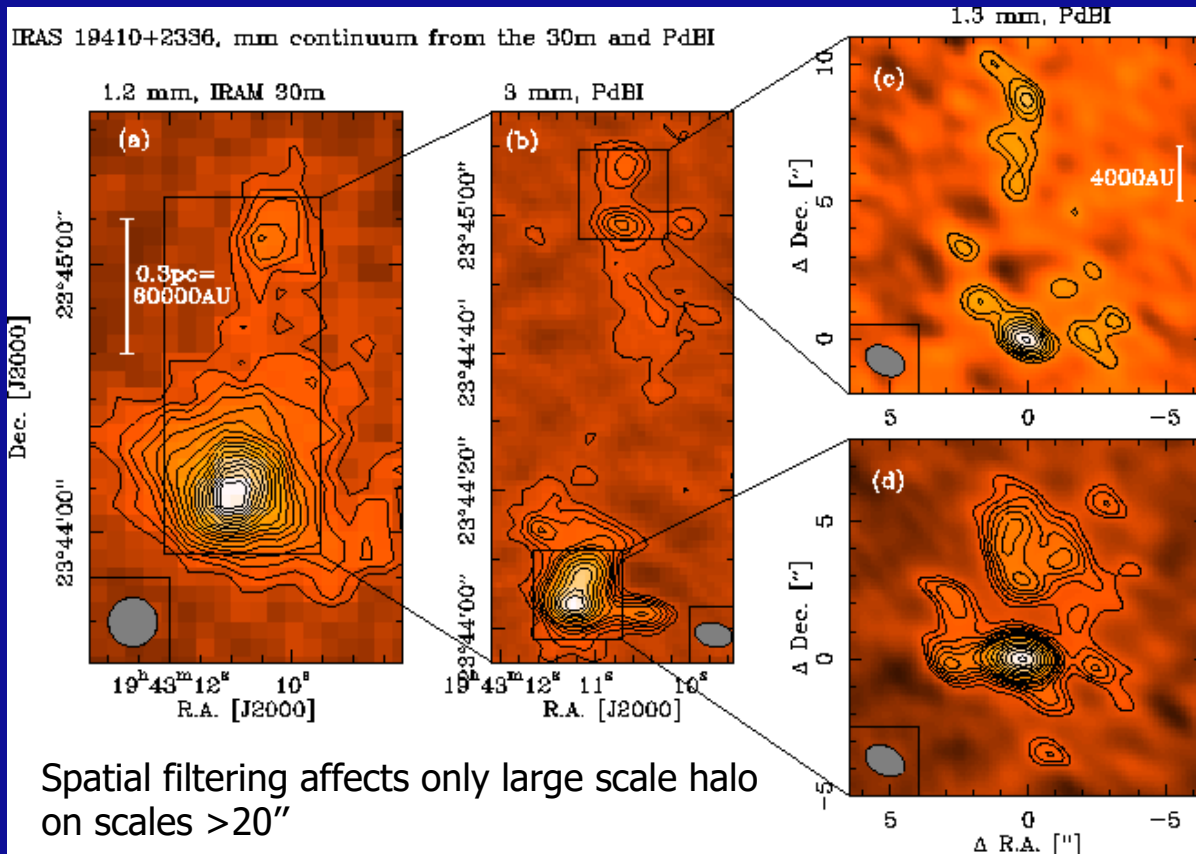
Kramer et al. 1996



# Pre-stellar core mass functions



# Fragmentation of a massive protocluster

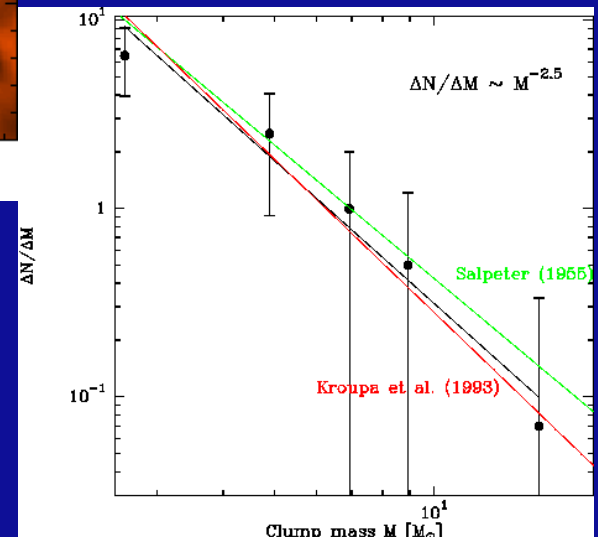


- 12 clumps within each core

- Integrated masses  
 98M<sub>sun</sub> (south)  
 42M<sub>sun</sub> (north)  
 --> 80 to 90% of the gas in halo

- Clump masses  
 1.7M<sub>sun</sub> to 25M<sub>sun</sub>

- Column densities



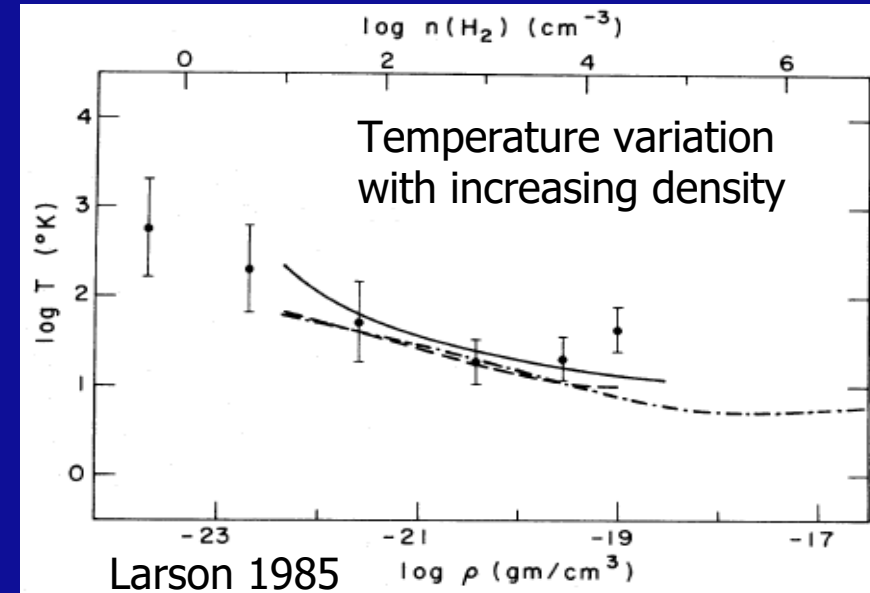
(Assumptions: - All emission peaks of protostellar nature  
 - Same temperature for all clumps (46K, IRAS))



# Characteristic mass defined by thermal physics

- Jeans mass depends on T:

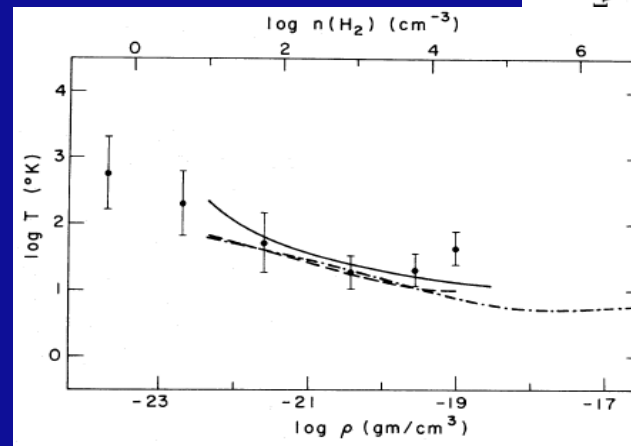
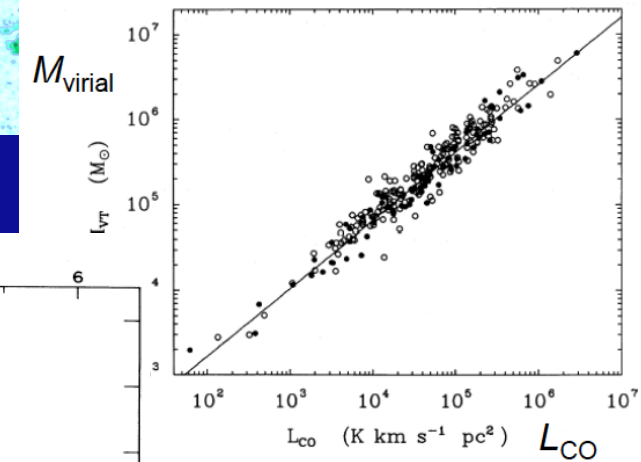
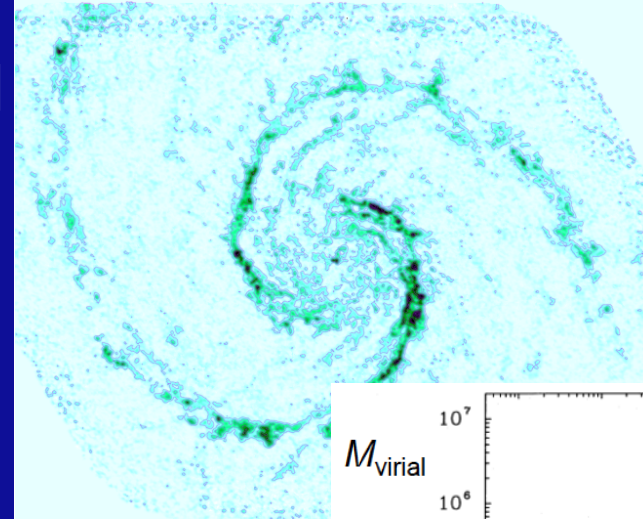
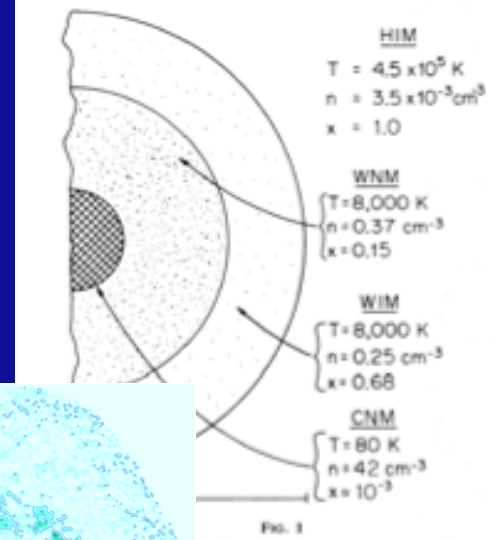
$$M_J = \text{constant} * a_t^3 / (\rho_0^{1/2} G^{3/2})$$
$$= 1.0 M_{\text{sun}} (T/(10\text{K}))^{3/2} (n_{\text{H}_2}/(10^4\text{cm}^{-3}))^{-1/2}$$



- Low densities  $\rightarrow$  T decreases with increasing  $\rho \rightarrow$  regions cool efficiently  
 $\rightarrow$  decreasing  $M_J$  suggests that fragmentation may be favoured there.
  - Further increasing  $\rho \rightarrow$  gas thermally couples to dust and clouds, and become partially optically thick  $\rightarrow$  Cannot cool well enough anymore  
 $\rightarrow$  temperature increases again.  
 $\rightarrow M_J$  decreases slower, inhibiting much further fragmentation.
- $\rightarrow$  Regime with lowest T should correspond to preferred fragmentation scale
- $\rightarrow$  The Jeans mass at this point is about  $0.5 M_{\text{sun}}$ .

# Summary

- Physical distribution
- Different components of ISM
- Basic characteristics
- Important cloud relations
- Cloud fragmentation



# Sternentstehung - Star Formation

Winter term 2017/2018

Henrik Beuther & Thomas Henning

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