

# Sternentstehung - Star Formation

Winter term 2017/2018

Henrik Beuther & Thomas Henning

17.10 Today: Introduction & Overview	(H.B.)
<b>24.10 Physical processes I</b>	<b>(H.B.)</b>
31.10 no lecture – Reformationstag	
07.11 Physical processes II	(H.B.)
14.11 Molecular clouds as birth places of stars	(H.L.)
21.11 Molecular clouds (cont.), Jeans Analysis	(H.B.)
28.11 Collapse models I	(H.B.)
05.12 Collapse models II	(T.H.)
12.12 Protostellar evolution	(T.H.)
19.12 Pre-main sequence evolution & outflows/jets	(T.H.)
09.01 Accretion disks I	(T.H.)
16.01 Accretion disks II	(T.H.)
23.01 High-mass star formation, clusters and the IMF	(H.B.)
30.01 Planet formation	(T.H.)
06.02 Examination week, no star formation lecture	

**Book: Stahler & Palla: The Formation of Stars, Wileys**

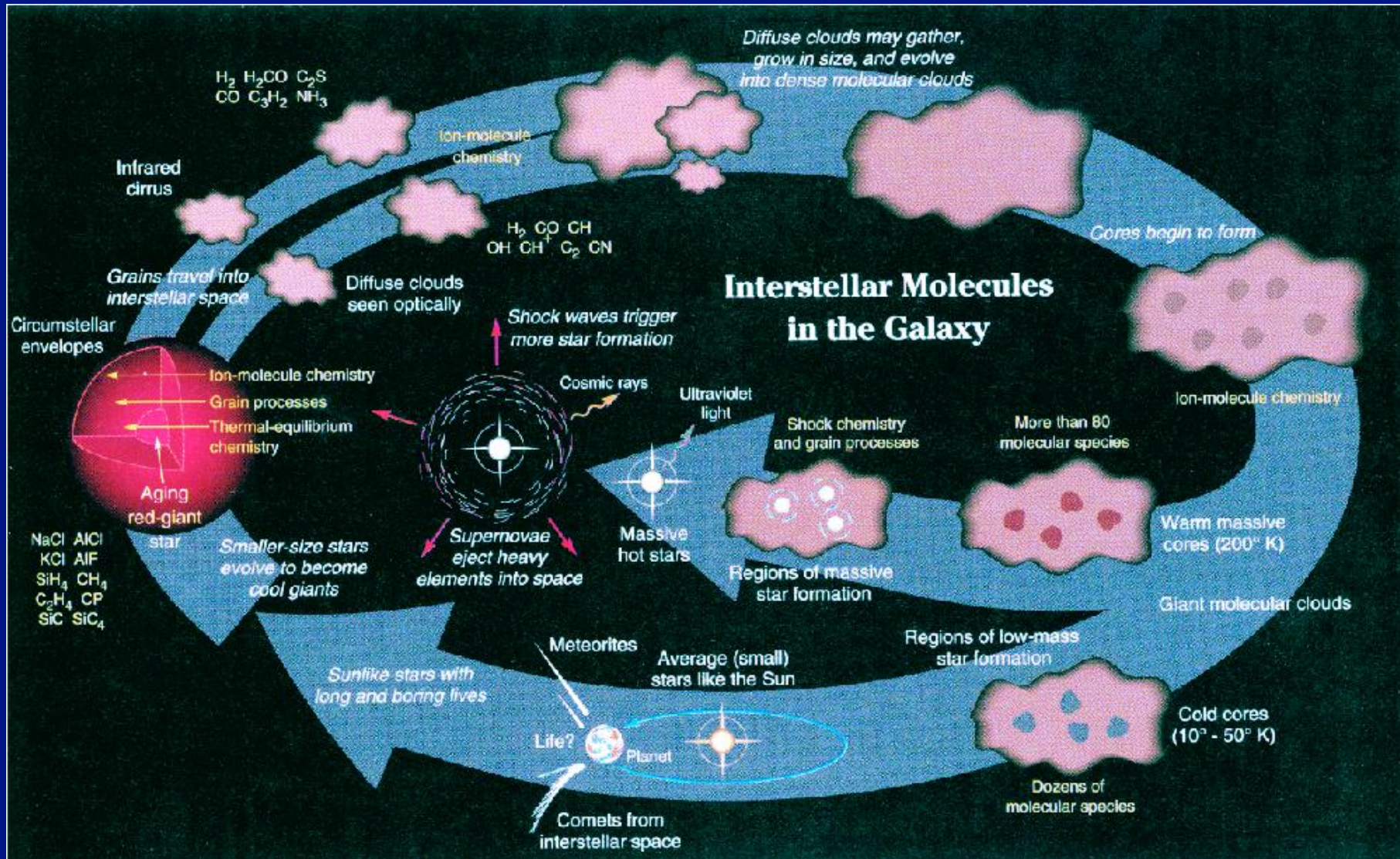
More Information and the current lecture files: [http://www.mpia.de/homes/beuther/lecture\\_ws1718.html](http://www.mpia.de/homes/beuther/lecture_ws1718.html)

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# Topics today

- The ISM, molecules and depletion
- Heating and cooling
- Radiation transfer and column density determination

# The cosmic cycle

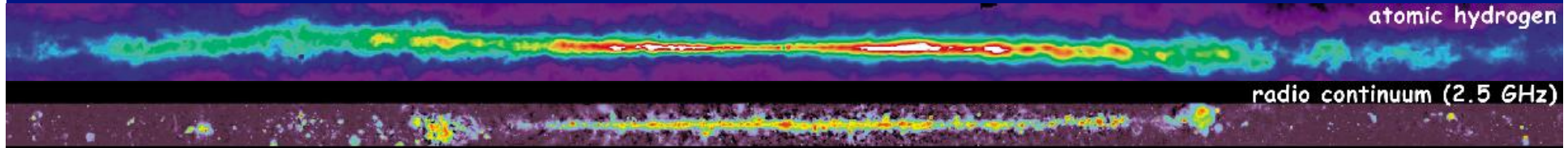


# Properties of Molecular Clouds

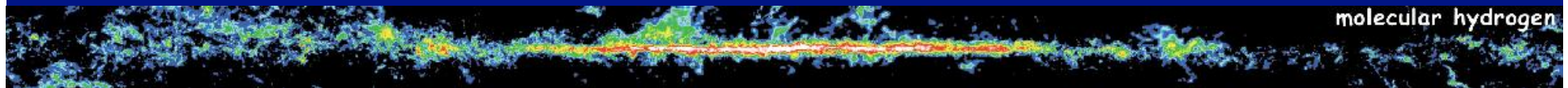
Type	n [cm <sup>-3</sup> ]	Size [pc]	T [K]	Mass [M <sub>sun</sub> ]
Giant Molecular Cloud	10 <sup>2</sup>	50	15	10 <sup>5</sup>
Dark Cloud Complex	5x10 <sup>2</sup>	10	10	10 <sup>4</sup>
Individual Dark Cloud	10 <sup>3</sup>	2	10	30
Dense low-mass cores	10 <sup>4</sup>	0.1	10	10
Dense high-mass cores	>10 <sup>5</sup>	0.1-1	10-30	100-10000

# Basics

Neutral and ionized medium



Stars form in the dense molecular gas and dust cores



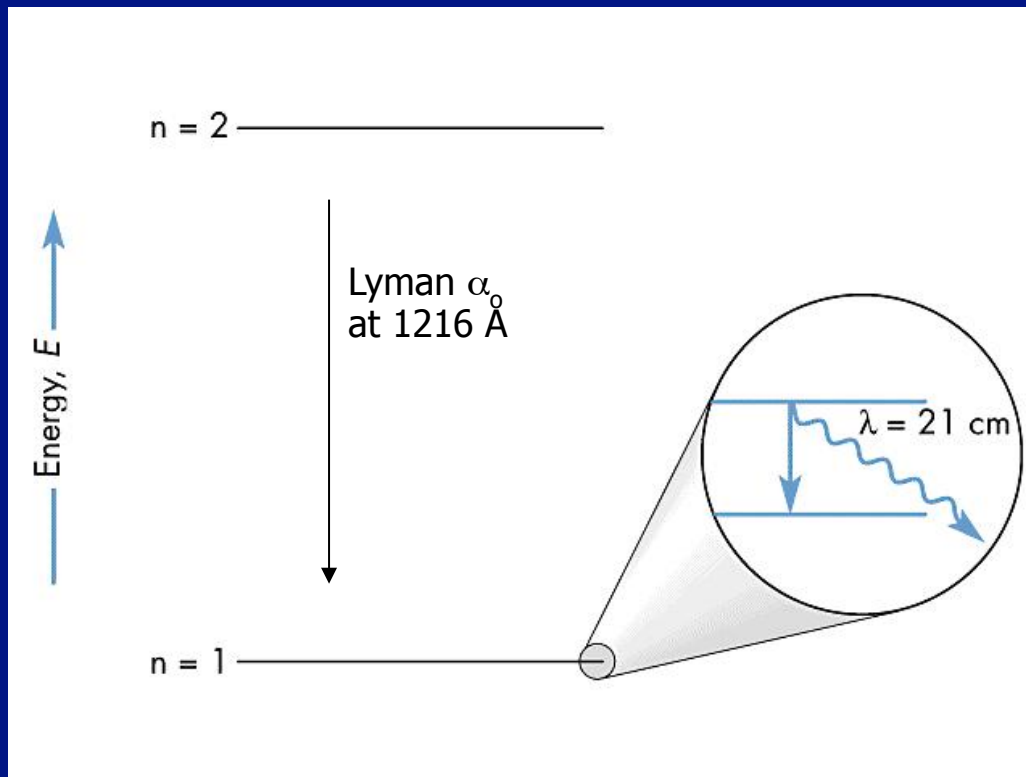
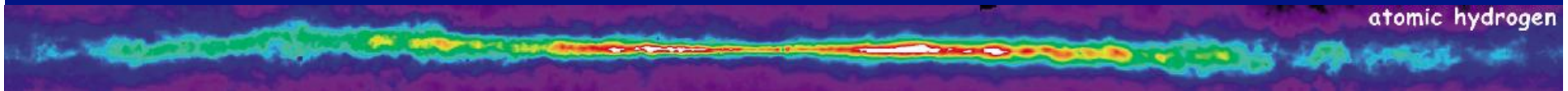
## ***Most important astrophysical tools:***

Spectral lines emitted by various molecules

Absorption and thermal emission from dust

# The neutral atomic gas

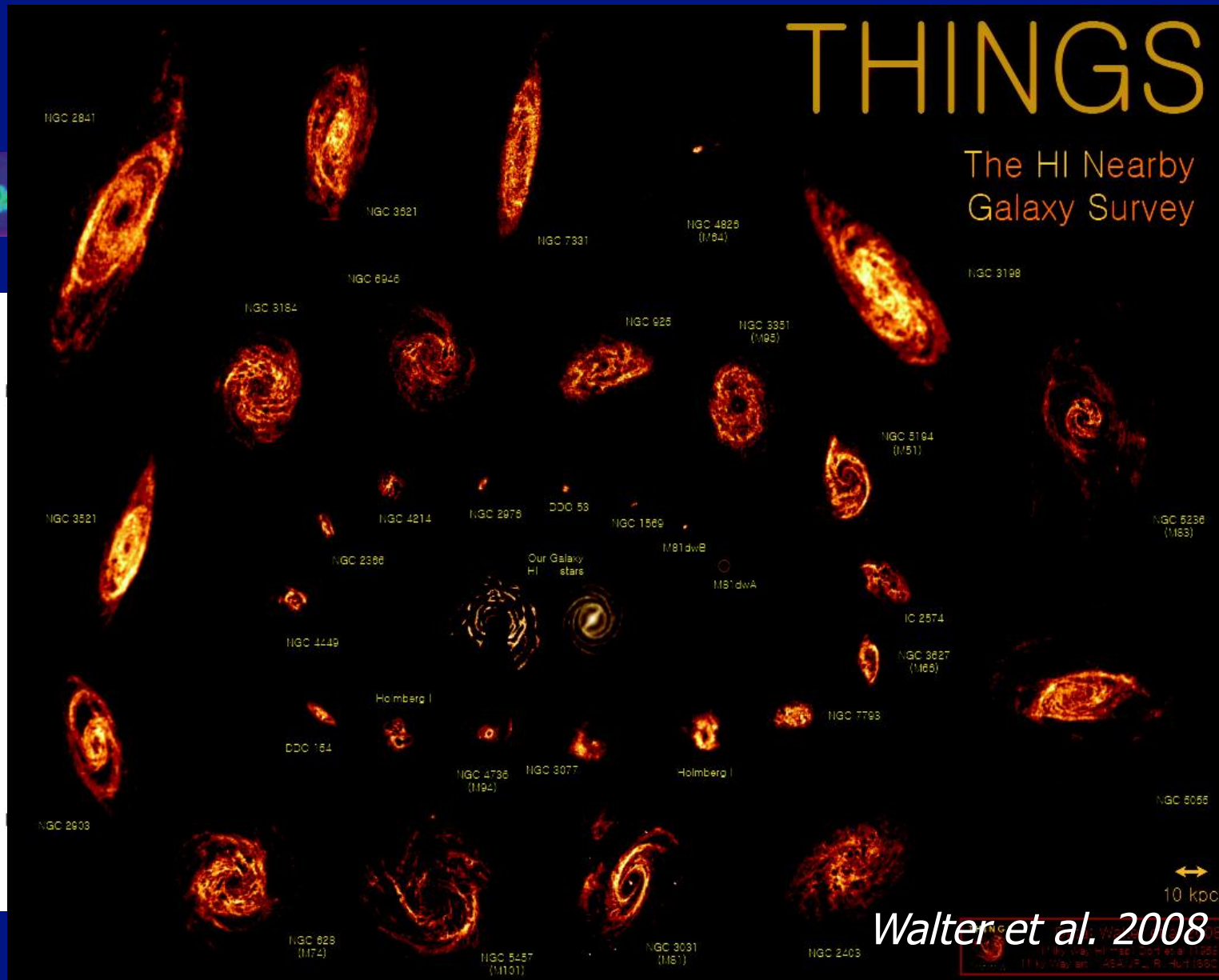
## Atomic Hydrogen



The 21cm line arises when the electron spin  $S$  flips from parallel ( $F=1$ ) to antiparallel ( $F=0$ ) compared to the Proton spin  $I$ .

$$\Delta E = 5.9 \times 10^{-5} \text{ eV}$$

# The neutral atomic gas



atomic hydrogen

in the  
parallel  
)  
spin I.

# The Ionized gas

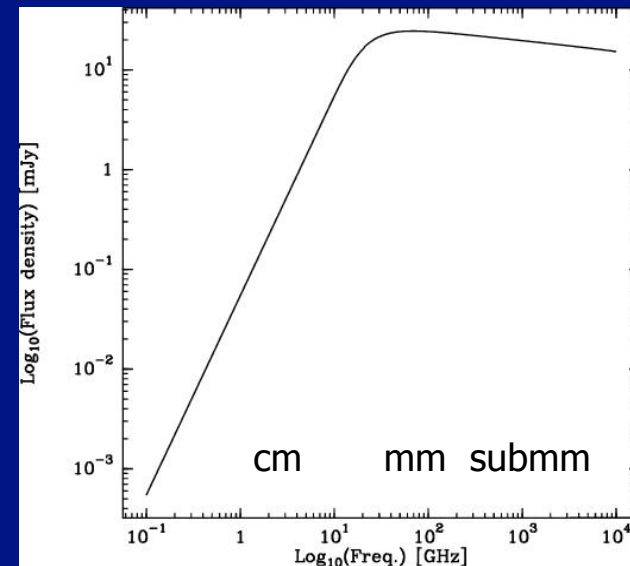
Ionized gas

radio continuum (2.5 GHz)

- Hydrogen recombination lines from optical to cm wavelengths
- Emission lines from heavier elements --> derive atomic abundances

He/H	0.1
C/H	$3.4 \times 10^{-4}$
N/H	$6.8 \times 10^{-5}$
O/H	$3.8 \times 10^{-4}$
Si/H	$3.0 \times 10^{-6}$

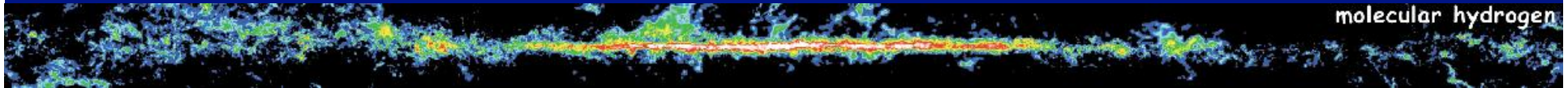
- Free-free emission between  $e^-$  and  $H^+$



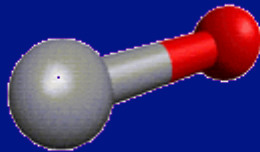


# The Molecular ISM

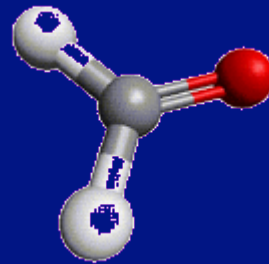
## Molecular Hydrogen



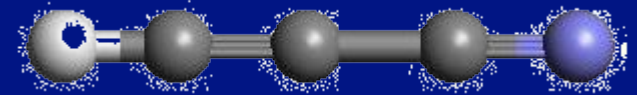
Carbon monoxide CO



Formaldehyde H<sub>2</sub>CO



Cyanoacetylene HC<sub>3</sub>N



### Excitation mechanisms:

- Rotation --> usually cm and (sub)mm wavelengths
- Vibration --> usually submm to FIR wavelengths
- Electronic transitions --> usually MIR to optical wavelengths

# Molecular ISM Basics

## History:

- Late 1930s: Detection of CH, CH<sup>+</sup> and CN in diffuse clouds by absorption of optical light by background stars
- 1960s: Detection of OH, NH<sub>3</sub> and H<sub>2</sub>O at radio wavelength, 1970 CO

## Formation of molecules is an energy problem:

Two atoms approach each other with positive total energy  
→ rebound if no energy can be given away

## Possibilities:

- Simultaneous collision with 3rd atom carrying away energy  
--> unlikely at the given low densities
- Form a molecule in excited state, and then radiating away energy  
--> probability of such radiative association low as well

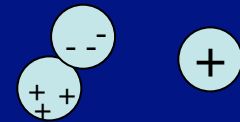
# Molecular ISM Basics

- Ion-molecule or ion-atom reactions can solve energy problem
- Neutral-neutral reactions on dust grain surfaces (catalytic) important

- Ion induces dipole moment in atom or molecule

--> creates electrostatic attraction between the two.

--> effective cross section increases over geometric values



- At low temperatures such reactions account for large fraction of molecules.

- However, not enough ions to account for large H<sub>2</sub> abundances

--> grain surface chemistry important

- Simple molecules like CO or CS → ion-molecule chemistry,

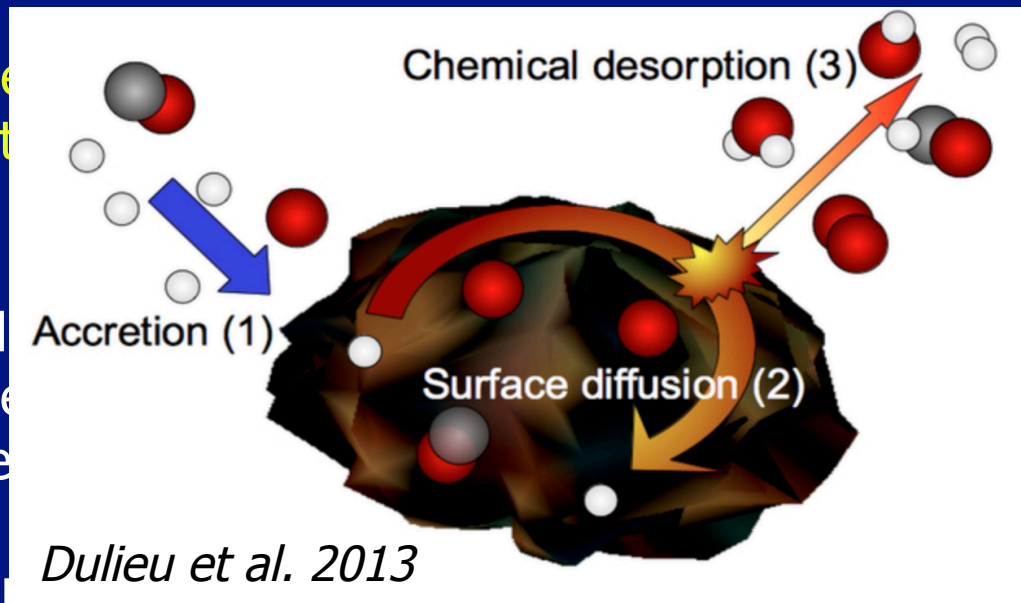
- More complex molecules → grain surface chemistry important

# Molecular ISM Basics

- Ion-molecule
- Neutral-neutral

- Ion induces d
- > creates e
- > effective

- At low temper

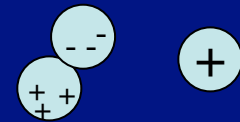


*Dulieu et al. 2013*

- However, not enough ions to account for large H<sub>2</sub> abundances
- > grain surface chemistry important

- Simple molecules like CO or CS → ion-molecule chemistry,
- More complex molecules → grain surface chemistry important

problem  
(c) important



es

ation of molecules.

# Molecules in Space

2	3	4	5	6	7	8	9	10	11	12	13 atoms
H2	C3	c-C3H	C5	C5H	C6H	CH3C3N	CH3C4H	CH3C5N?	HC9N	CH3OC2H5	HC11N
AlF	C2H	l-C3H	C4H	l-H2C4	CH2CHCN	HCOOCH3	CH3CH2CN	(CH3)2CO			
AlCl	C2O	C3N	C4Si	C2H4	CH3C2H	CH3COOH?	(CH3)2O	NH2CH2COOH?			
C2	C2S	C3O	l-C3H2	CH3CN	HC5N	C7H	CH3CH2OH	CH3CH2CHO			
CH	CH2	C3S	c-C3H2	CH3NC	HCOCH3	H2C6	HC7N				
CH+	HCN	C2H2	CH2CN	CH3OH	NH2CH3	CH2OHCHO	C8H				
CN	HCO	CH2D+?	CH4	CH3SH	c-C2H4O	CH2CHCHO					
CO	HCO+	HCCN	HC3N	HC3NH+	CH2CHOH						
CO+	HCS+	HCNH+	HC2NC	HC2CHO							
CP	HOC+	HNCO	HCOOH	NH2CHO							
CsI	H2O	HNCS	H2CHN	C5N							
HCl	H2S	HOCO+	H2C2O	HC4N							
KCl	HNC	H2CO	H2NCN								
NH	HNO	H2CN	HNC3								
NO	MgCN	H2CS	SiH4								
NS	MgNC	H3O+	H2COH+								
NaCl	N2H+	NH3									
OH	N2O	SiC3									
PN	NaCN	C4									
SO	OCS										
SO+	SO2										
SiN	c-SiC2										
SiO	CO2										
SiS	NH2										
CS	H3+										
HF	SiCN										
SH	AlNC										
FeO(?)	SiNC										

About 200 detected interstellar molecules as of October 2017 ([www.cdms.de](http://www.cdms.de)).  
61 molecular detection in extragalactic systems.

# A few important molecules

Mol.	Trans.	Abund.	Crit. Dens. [cm <sup>-3</sup> ]	Comments
H <sub>2</sub>	1-0 S(1)	1	8x10 <sup>7</sup>	Shock tracer
CO	J=1-0	8x10 <sup>-5</sup>	3x10 <sup>3</sup>	Low-density probe
OH	<sup>2</sup> Π <sub>3/2</sub> ; J=3/2	3x10 <sup>-7</sup>	1x10 <sup>0</sup>	Magnetic field probe (Zeeman)
NH <sub>3</sub>	J,K=1,1	2x10 <sup>-8</sup>	2x10 <sup>4</sup>	Temperature probe
CS	J=2-1	1x10 <sup>-8</sup>	4x10 <sup>5</sup>	High-density probe
SiO	J=2-1		6x10 <sup>5</sup>	Outflow shock tracer
H <sub>2</sub> O	6 <sub>16</sub> -5 <sub>23</sub>		1x10 <sup>3</sup>	Maser
H <sub>2</sub> O	1 <sub>10</sub> -1 <sub>11</sub>	<7x10 <sup>-8</sup>	2x10 <sup>7</sup>	Warm gas probe
CH <sub>3</sub> OH	7-6	1x10 <sup>-7</sup>	1x10 <sup>5</sup>	Dense gas/temperature probe
CH <sub>3</sub> CN	19-18	2x10 <sup>-8</sup>	2x10 <sup>7</sup>	Temperature probe in Hot Cores

# Basics IV

## Depletion of molecules on dust grains

In molecule's ref. frame, grains are moving at  $v_{\text{therm}}$  relative to molecules

$$E = 1/2 m v_{\text{therm}}^2 = 3/2 k_b T \Rightarrow v_{\text{therm}} = (3k_b T/m)^{1/2}$$

n grains sweeps out cylindrical volume in time  $\Delta t$  of

$$n(\pi a^2) v_{\text{therm}} \Delta t \quad (a: \text{grain radius})$$

Probability of molecule in volume V to be struck by grain in time  $\Delta t$

$$P(\Delta t) = n(\pi a^2) v_{\text{therm}} \Delta t / V$$

Hence the collision time  $t_{\text{coll}}$  (for  $P(\Delta t)V = 1$ )

$$t_{\text{coll}} = 1/(n(\pi a^2) v_{\text{therm}}) = 1/(n_H \Sigma v_{\text{therm}}) \quad (n_H: \text{density}; \Sigma: \text{cross section})$$

For example CS:  $v_{\text{therm}} \sim 5 \times 10^3 \text{ cm s}^{-1}$  at 10K, and  $n_H \sim 10^4 \text{ cm}^{-3}$

$$t_{\text{coll}} \sim 6 \times 10^5 \text{ yr}$$

Depletion time-scale very short

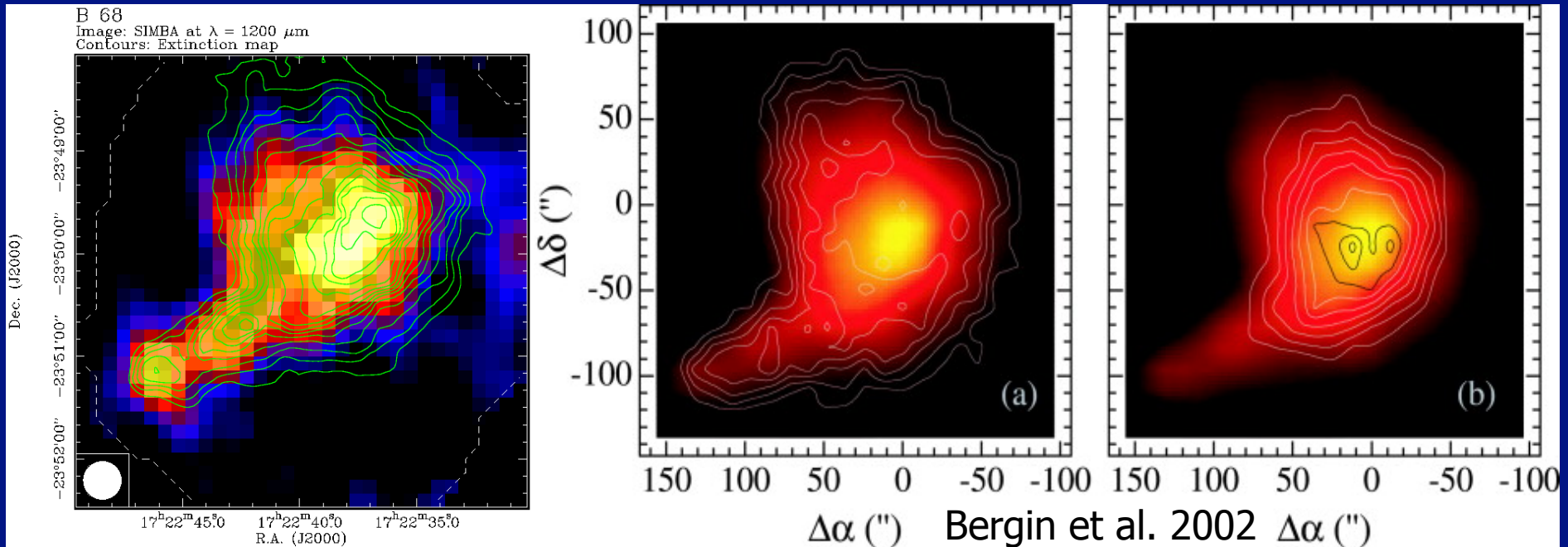
--> mechanisms for reinjecting molecules from grains important

# Depletion example

1.2 mm Dust Continuum

$C^{18}O$

$N_2H^+$



Possible mechanisms working against depletion:

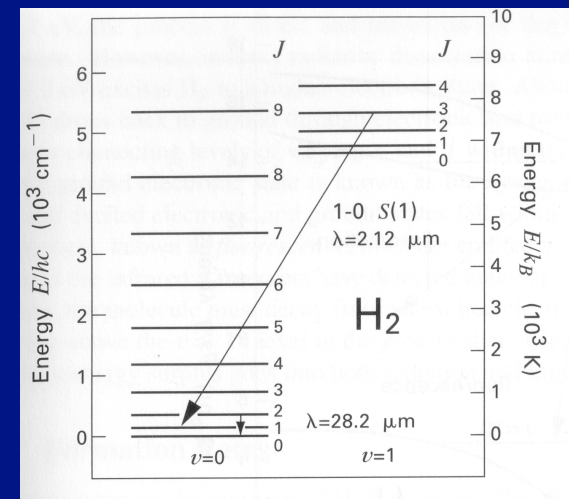
- UV radiation (not working in dense cores)
- In small grain, heat from chemical grain surface reactions could raise temperature
- Kelvin-Helmholtz contraction and energy
- Ignited central protostar
- Shocks
- ...



# Molecular Hydrogen (H<sub>2</sub>)

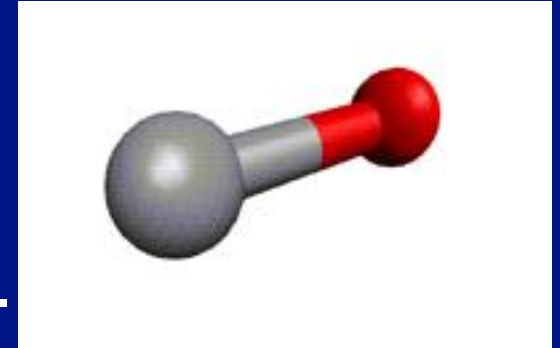
- H<sub>2</sub> consists of 2 identical atoms → no electric dipol moment
- Rotationally excited H<sub>2</sub> has allowed quadrupole transitions  $\Delta J = 2$   
→ lowest rotational transition J=2-0 has energy change of 510 K

- Rotational energy for H<sub>2</sub>:  
Classical mechanics:  $E_{\text{rot}} = J^2/2I$   
(J: Angular momentum; I: Moment of inertia)  
→ Small moment of inertia  
→ large spread of energy levels

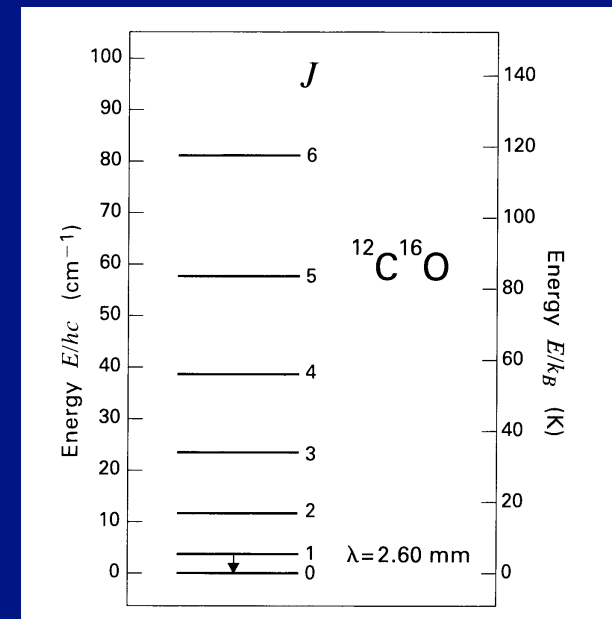


→ Cold clouds have to be observed other ways, e.g., CO

# Carbon monoxide (CO)



- Forms through gas phase reactions.
- Strong binding energy of 11.1 eV  
→ prevents much further destruction (self-shielding).
- Permanent dipole moment → strong emission at (sub)mm wavelengths.
- Larger moment of inertia than H<sub>2</sub>.  
→ more closely spaced rotational ladder,  
J=1 level at 4.8x10<sup>-4</sup>eV or 5.5K above ground
- In molecular clouds excitation mainly via collisions with H<sub>2</sub>.
- Critical density for thermodynamic equilibrium with H<sub>2</sub>  $n_{\text{crit}} = A/\gamma \sim 3 \times 10^3 \text{cm}^{-3}$ .  
(A: Einstein A coefficient;  $\gamma$ : collision rate with H<sub>2</sub>)
- The level population follows a Boltzmann-law:  
$$n_{j+1}/n_j = g_{j+1}/g_j \exp(-\Delta E/k_B T_{\text{ex}})$$
  
(for CO, the statistical weights  $g_j = 2J + 1$ )  
Excitation temperature  $T_{\text{ex}}$  is a measure for the level populations and equals the kinetic temperature  $T_{\text{kin}}$  if the densities are  $> n_{\text{crit}}$ .



# Topics today

- The ISM, molecules and depletion
- Heating and cooling
- Radiation transfer and column density determination

# Heating processes

UV radiation from stars

Energy injection from supernovae

Energy injection from outflows/jets

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Cosmic rays interact with HI and H<sub>2</sub>

(consist mainly of relativistic protons accelerated within magnetized shocks produced by supernova-remnant--molecular cloud interactions)



Interstellar radiation (diffuse field permeating interstellar space)

Mainly dissociates carbon (lower ionization potential than H<sub>2</sub>)



Photoelectric heating: - Heats grains which re-radiate in infrared regime  
- UV photons eject e<sup>-</sup> from dust and these e<sup>-</sup> heat surrounding gas via collisions

# Cooling processes

- H & H<sub>2</sub> no dipole moment → no efficient coolant in cold mol cloud  
→ other coolants needed

--> Hydrogen collides with ambient atoms/molecules/grains  
→ Cooling via these secondary constituents.



collisional excitation (FIR)



fine structure excitation (FIR)



rotational excitation (radio/(sub)mm)

At higher densities other molecules come into play, e.g., H<sub>2</sub>O.

→ CO the most effective coolant in molecular clouds.

- Collisions with gas atoms/molecules cause lattice vibrations on grain surfaces, that decay through the emission of infrared photons.

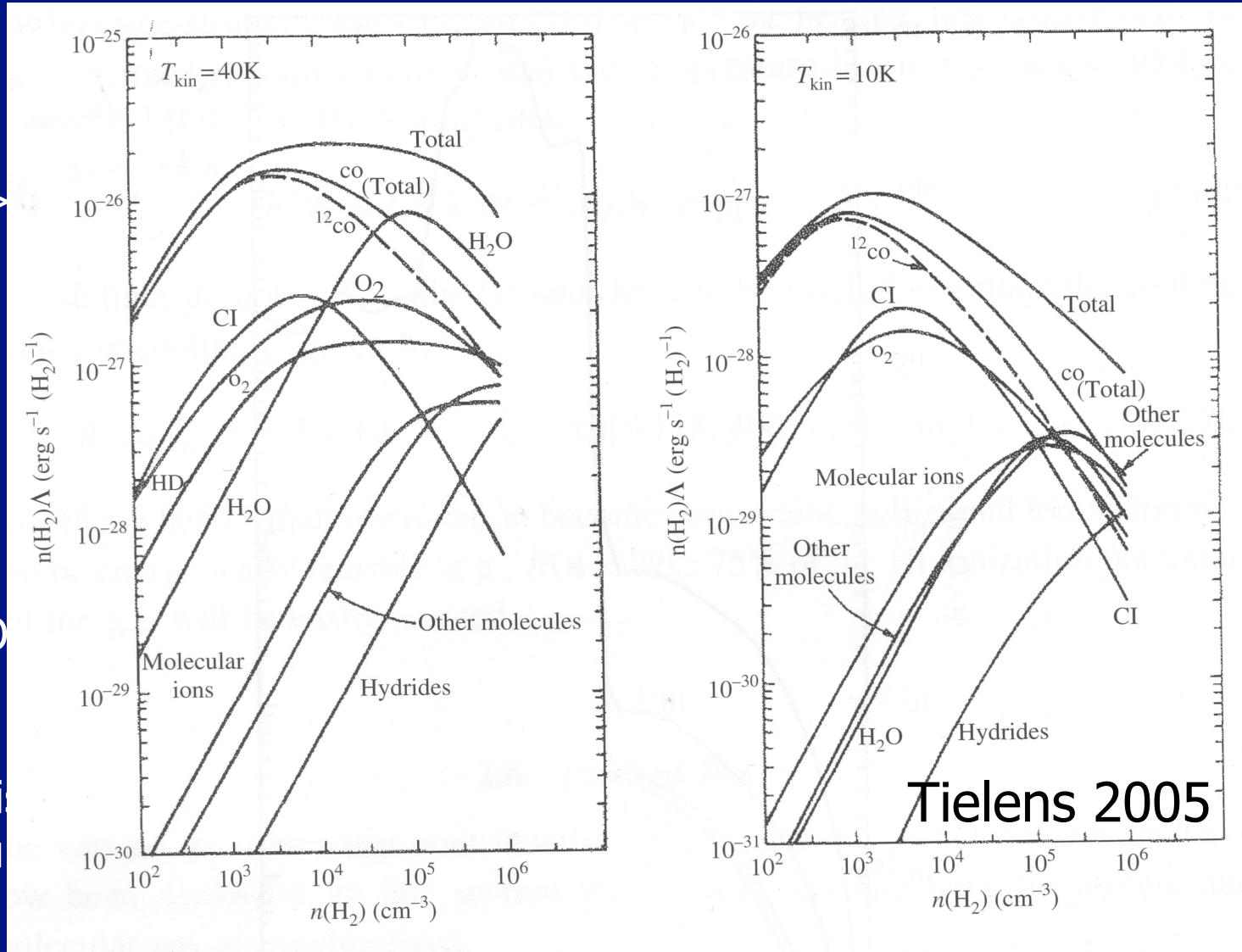
# Cooling processes

- H &

-->

→ CO

- Collisi  
SU



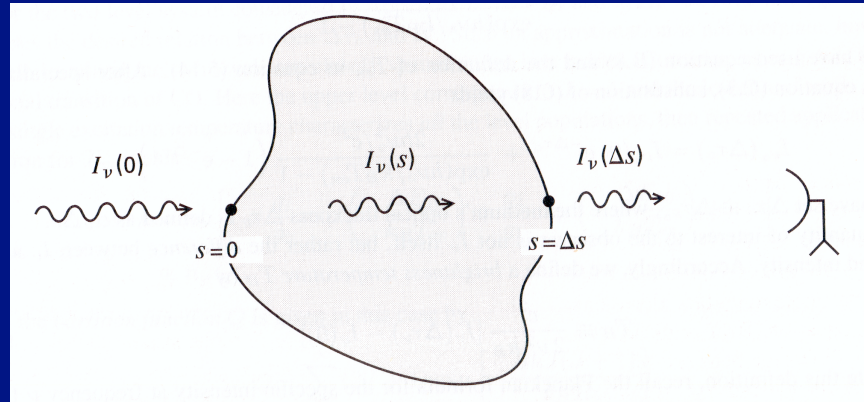
b)mm)  
 $\text{H}_2\text{O}$ .

n

# Topics today

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- Radiation transfer and column density determination

# Radiation transfer I



$$dI_v = -\kappa_v I_{v,0} ds + \varepsilon_v ds$$

with the opacity

$$d\tau_v = -\kappa_v ds$$

and the source function

$$S_v = \varepsilon_v / \kappa_v$$

$$\Rightarrow dI_v / d\tau_v = I_{v,0} - S_v$$

Assuming a spatially constant source function  $\rightarrow$  radiation transfer equation

$$\Rightarrow I_v = S_v (1 - e^{-\tau(v)}) + I_{v,0} e^{-\tau(v)}$$

$\kappa$ : absorption coef.  
 $\varepsilon$ : emission coef.



# Radiation transfer II

The excitation temperature  $T_{\text{ex}}$  is defined via a Boltzmann distribution as

$$n_j/n_{j-1} = g_j/g_{j-1} \exp(-h\nu/kT_{\text{ex}})$$

with  $n_j$  and  $g_j$  the number density and statistical weights.

In case of rotational transitions

$$g_j = 2J + 1$$

J: rot. quantum  
number

In thermal equilibrium

$$T_{\text{ex}} = T_{\text{kin}}$$

In a uniform molecular cloud the source function  $S_\nu$  equals Planck function

$$S_\nu = B_\nu(T_{\text{ex}}) = 2h\nu^3/c^2 (\exp(h\nu/kT_{\text{ex}}) - 1)^{-1}$$

# Radiation transfer III

Then the radiation transfer equation

$$\Rightarrow I_\nu = B_\nu(T_{\text{ex}}) (1 - e^{-\tau(\nu)}) + I_{\nu,0} e^{-\tau(\nu)}$$

In the Rayleigh-Jeans limits ( $h\nu \ll kT$ ) B equals

$$B = 2k\nu^2/c^2 T \quad (\text{def.} \rightarrow T = c^2/(2k\nu^2) I_\nu)$$

And the radiation transfer equation using now the radiation temperature is

$$T_r = J_\nu(T_{\text{ex}}) (1 - e^{-\tau(\nu)}) + J_{\nu,0}(T_{\text{bg}}) e^{-\tau(\nu)}$$

with

$$J_\nu = h\nu/k (\exp(h\nu/kT) - 1)^{-1}$$

# Molecular column densities I

To derive molecular column densities, 3 quantities are important:

- 1) Intensity  $T$  of the line
- 2) Optical depth  $\tau$  of the line (observe isotopologues or hyperfine structure)
- 3) Partition function  $Q$

The optical depth  $\tau$  of a molecular transition can be expressed like

$$\tau = c^2/8\pi\nu^2 A_{ul}N_u (\exp(h\nu/kT) - 1) \phi$$

with the Einstein  $A_{ul}$  coefficient

$$A_{ul} = 64\pi^4\nu^3/(3c^3h) \mu^2 J_u/(2J_u-1)$$

and the line form function  $\phi$

$$\phi = c/\nu 2\text{sqrt}(\ln 2)/(\text{sqrt}(\pi)\Delta\nu)$$

# Molecular column densities II

Using furthermore the radiation transfer eq. ignoring the background

$$T = J_\nu(T_{\text{ex}}) \tau (1 - e^{-\tau})/\tau$$

And solving this for  $N_u$ , one gets

$$N_u = \frac{3k/8\pi^3 \nu}{1/\mu^2} \frac{(2J_u - 1)/J_u}{\tau} \frac{\tau}{(1 - e^{-\tau})} (T \Delta \nu \sqrt{\pi}) / (2\sqrt{\ln 2})$$

The last expression equals the integral  $\int T dv$ .

The column density in the upper level  $N_u$  relates to the total column density  $N_{\text{tot}}$

$$N_{\text{tot}} = N_u/g_u \exp(E_u/kT) Q$$

For a linear molecule like CO, the partition function  $Q$  can be approximated to

$$Q = kT/hB.$$

However, for more complex molecules  $Q$  can become very complicated.

# Summary

- Main tools: Spectral line emission and thermal emission and extinction from dust (more on dust next week)
- Molecules interesting for themselves and chemistry
- However, also extremely useful to trace physical processes.
- Molecules deplete on grains at low temperatures
- Discussed main cooling and heating processes
- Discussed basic line radiation transfer and column density determination

# Sternentstehung - Star Formation

Winter term 2017/2018

Henrik Beuther & Thomas Henning

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