

# *HST* Proper Motions of Globular Clusters



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# Introduction

## Part I: astrometry with *HST*

- undersampling
- geometric distortion
- differential nature

## Part II: proper motions of globular clusters with HST

- what we can do with them

## Part III: our project

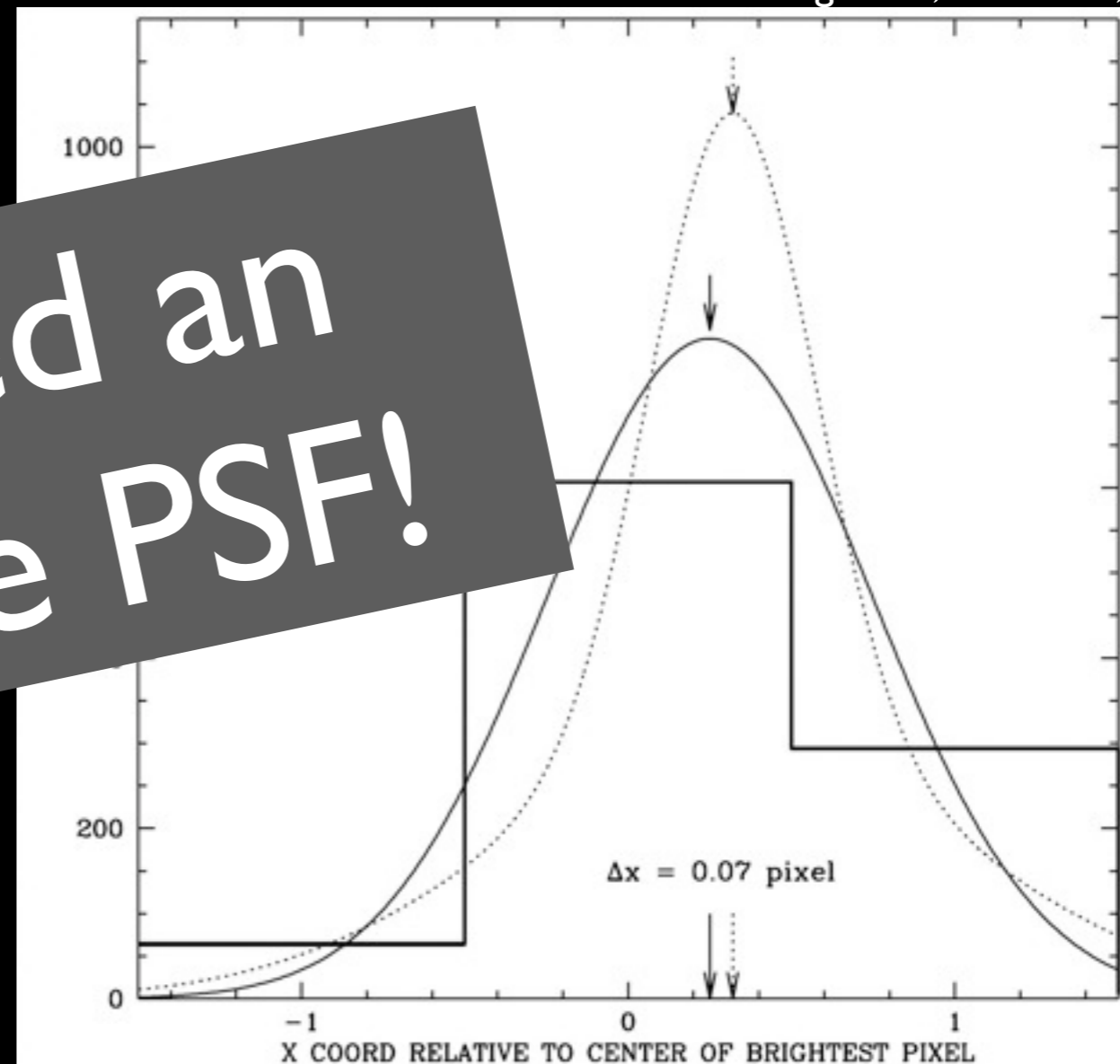
- the catalog
- preliminary results

# ISSUES#I: Undersampling

## Illustration of Undersampling conditions

Where is the center?

Anderson & King 2000, PASP 112,



Easy

We need an accurate PSF!

Harder

# Undersampling and Astrometry

## Impossible?

- A point source has “no hair”
  - 3 parameters ( $x_*$ ,  $y_*$ ,  $f$ ),  $\sim 9$  pixels
- Minimal requirements: “slosh”



## What is possible?

- $\approx 0.01$  pixel possible  $\sim (S/N)^{-1}$ 
  - Need good PSF model
  - Need good dithering

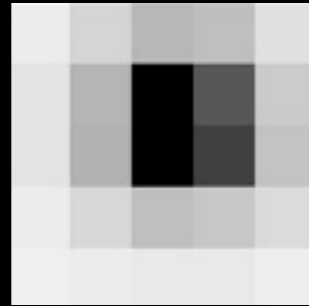


## Limitations

- Individual images; no stacks
- Hard in crowded fields
  - Neighbor finding/subtraction
- Ideal in “semi-crowded” regime



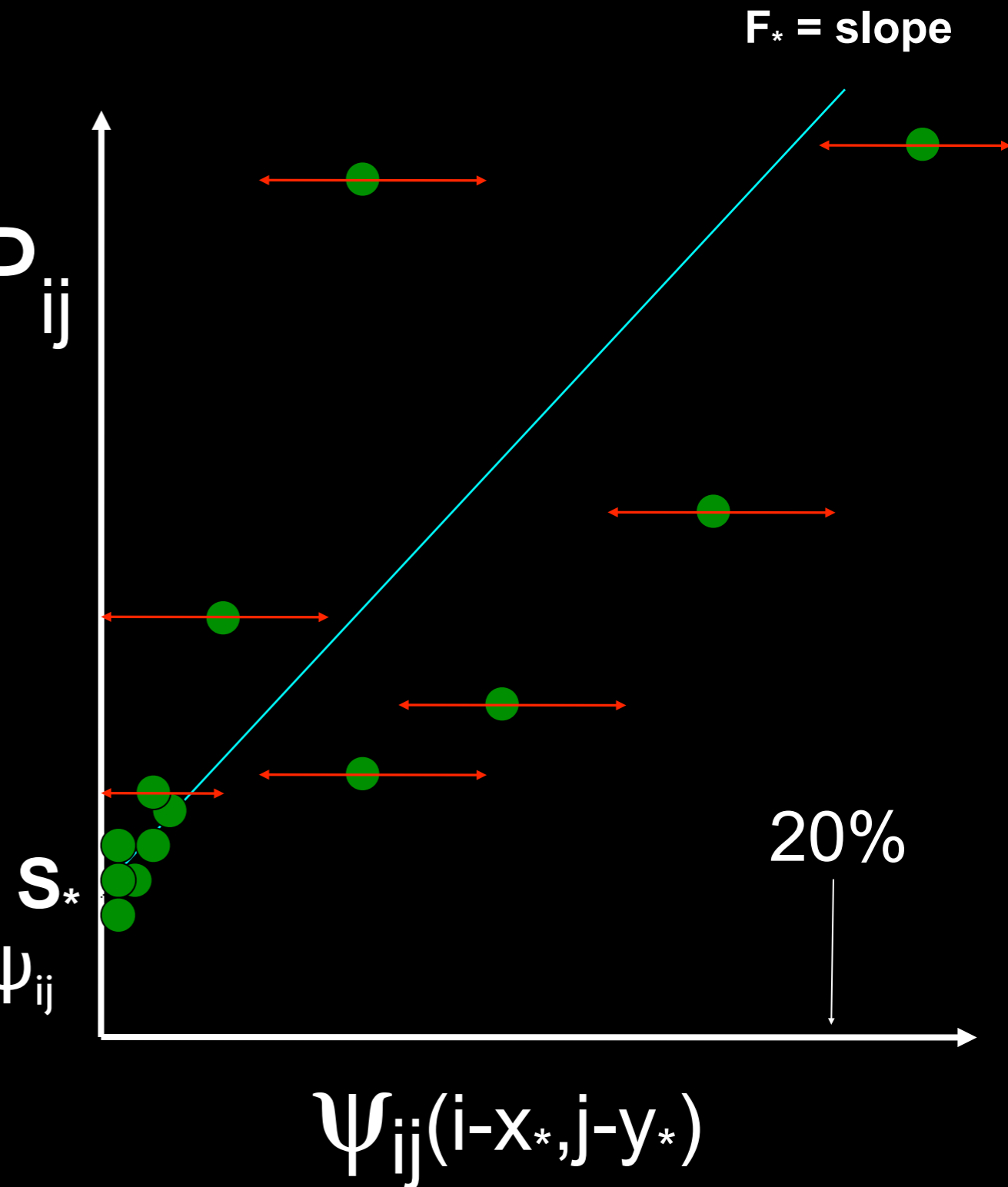
## How to use the PSF:


 $P_{ij}$ 

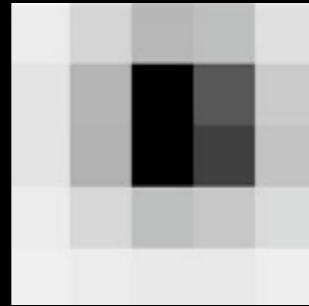
Fitting for Flux and position:

$$P_{ij} = S + F_* \times \psi_{ij}$$

- Nice, linear equation!
  - $P$  in  $S_*$ ,  $F_*$ , not  $(x_*, y_*)$
- Sky from outer annulus
- For given  $(x_*, y_*)$ , get  $F_* = \sum (P_{ij} - s) / \psi_{ij}$
- Find optimal  $(x_*, y_*)$



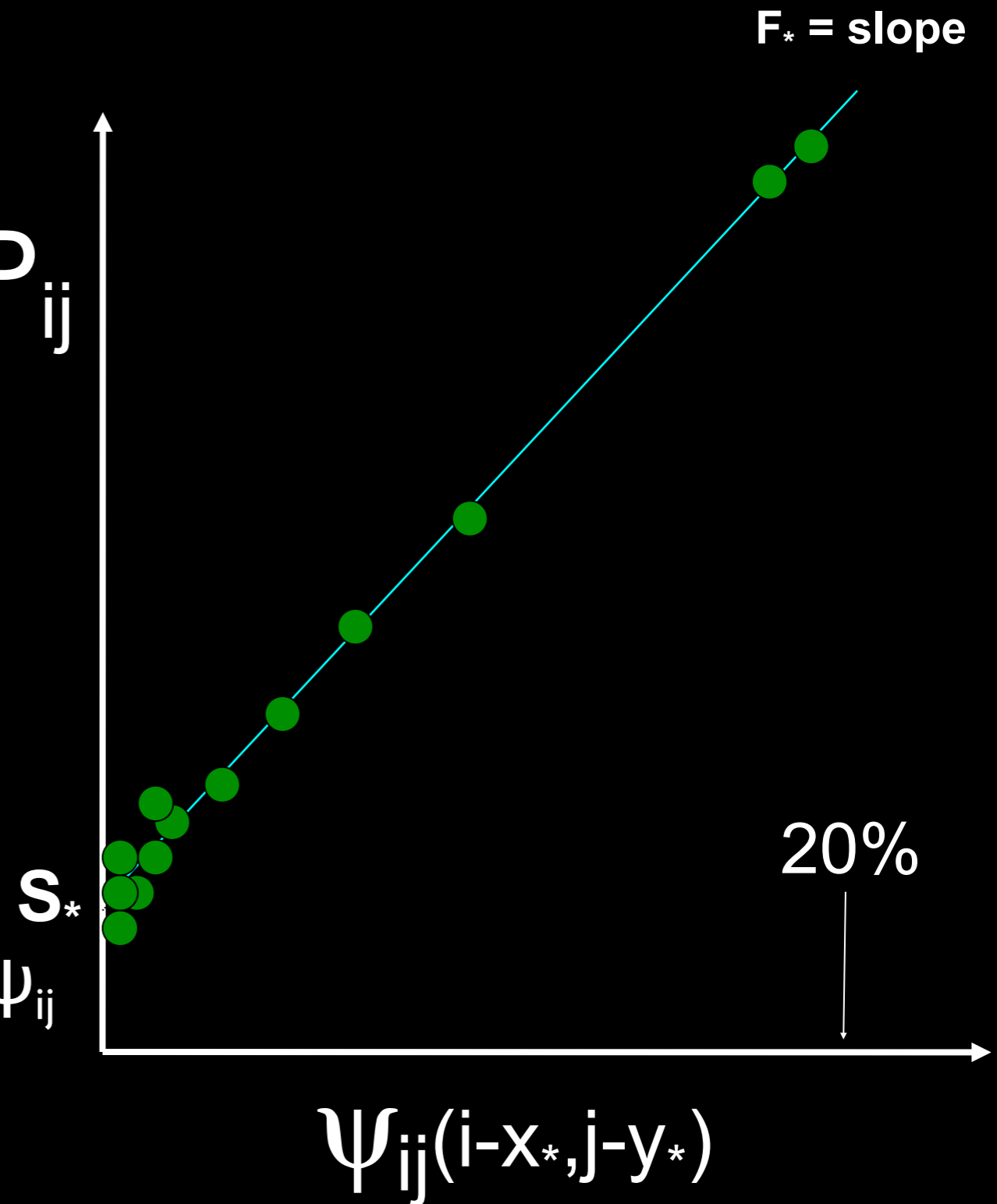
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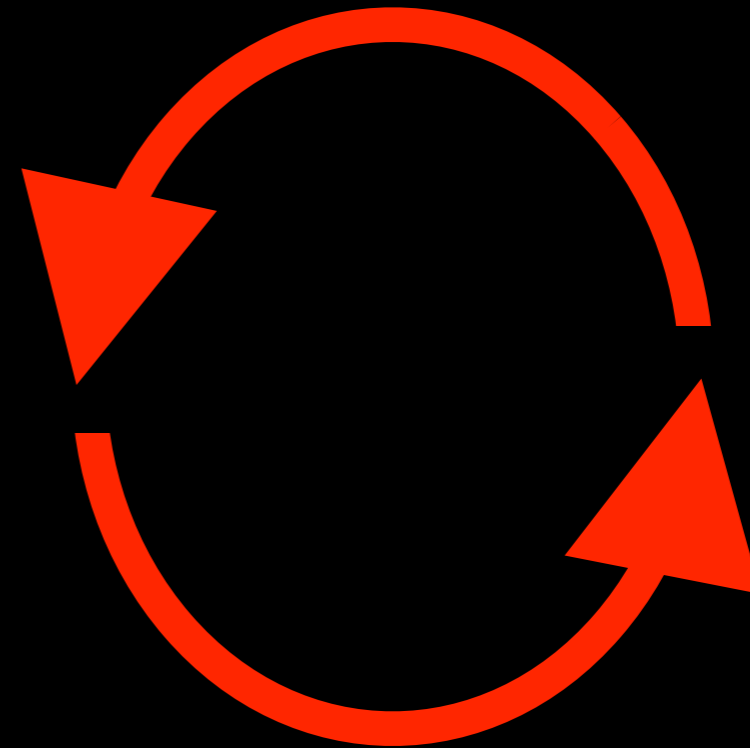
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## PSF: Finding vs. Using

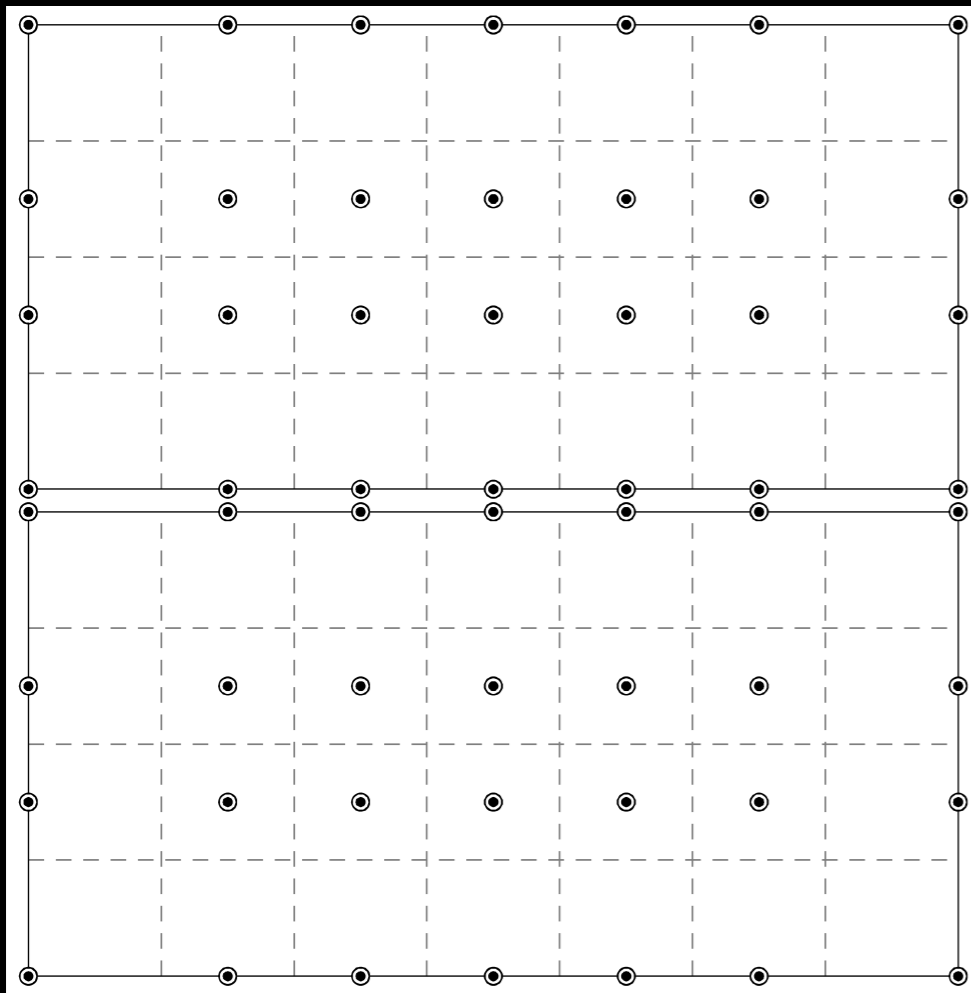
- **Degeneracy:**
  - Finding  $\psi_{\text{EFF}}$  requires  $(x_*, y_*, f)$
  - Finding  $(x_*, y_*, f)$  requires  $\psi_{\text{EFF}}$
- **Iteration**
  - Dithers break the degeneracy!



# Higher-level PSF issues:

- Spatial variability:

2(7x4) PSF array for  
WFC3/UVIS F438W





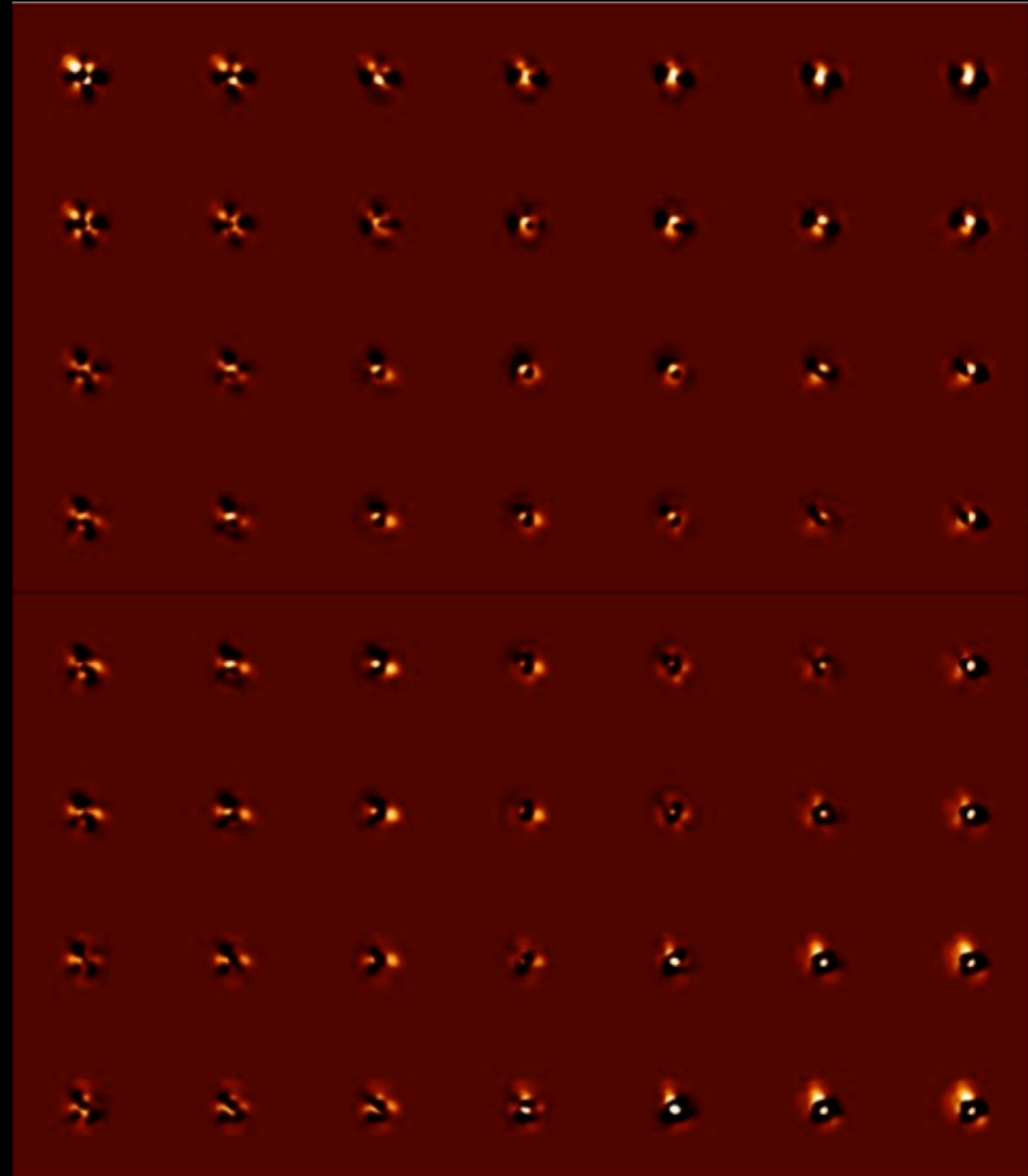
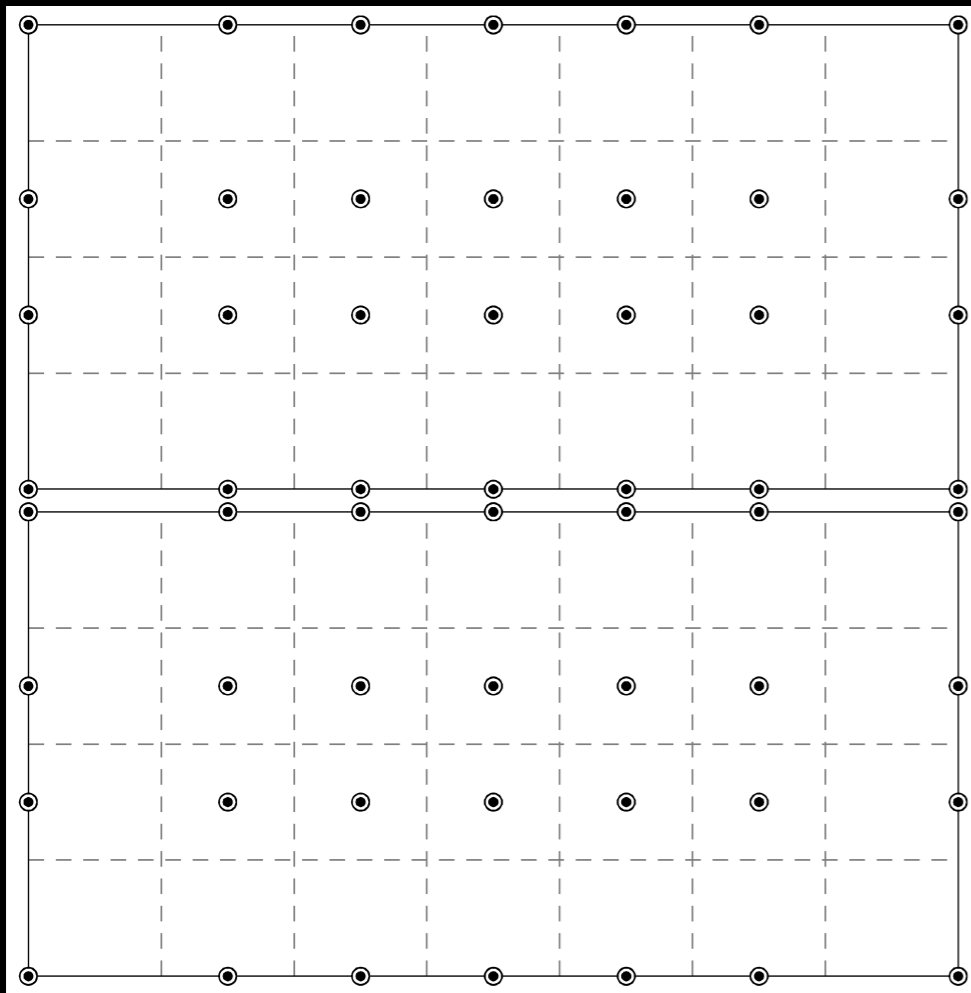


## Higher-level PSF issues:

- Spatial variability:

Core intensity varies by  $\pm 10\%$   
over scales of  $\sim 500$  pixels.

- Time variability (breathing)



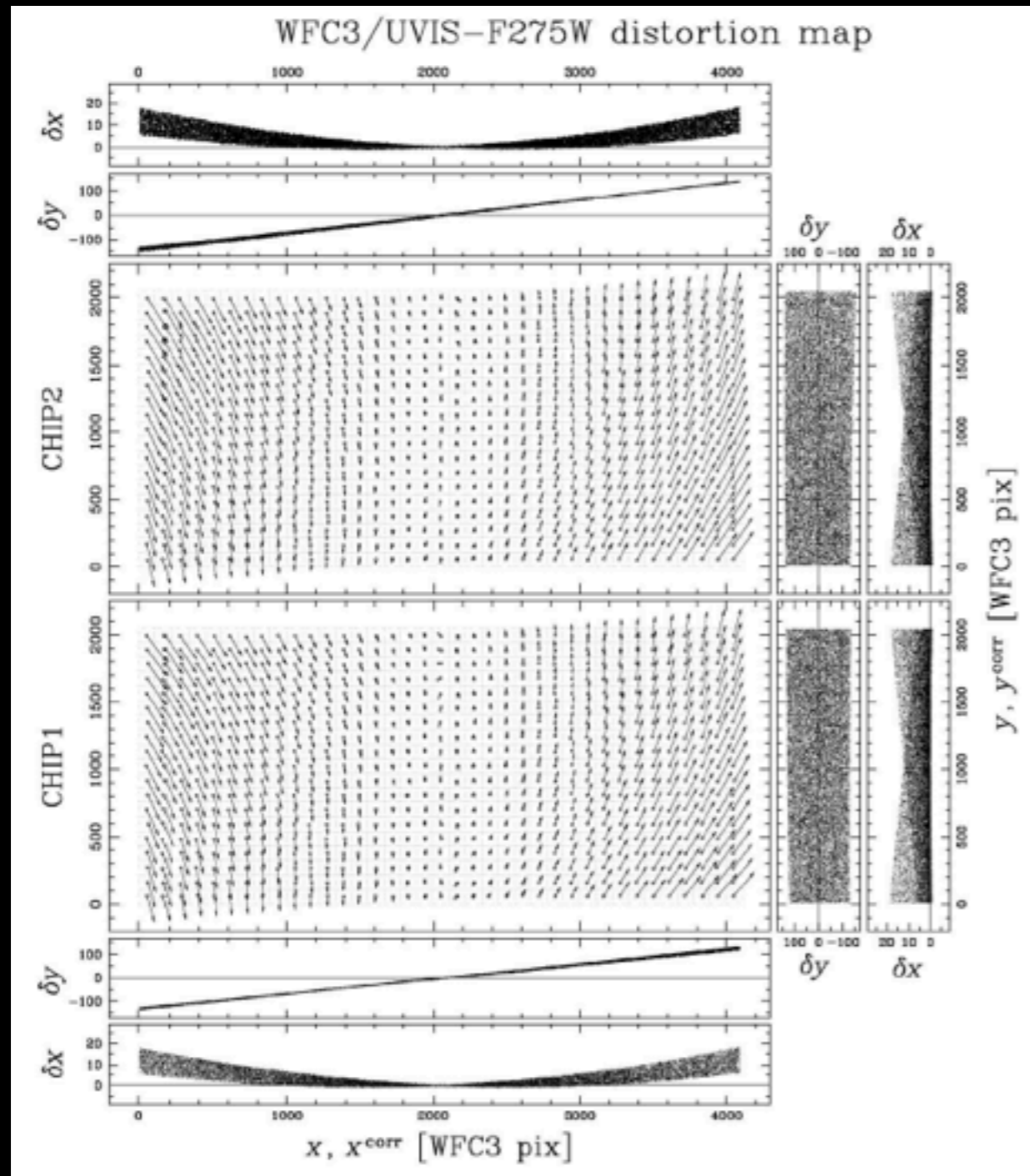
## ISSUES#2: Geometric Distortion

**Why?** Fewer reflections, better throughput

- Linear “skew”: 500 pixels over 2000 px  
→ Parallelogram pixels
- Non-linear: 50 pixels over 2000 px
- Filters introduce distortion ( $\sim 0.1$  pixel)
- Detector “stitching” defects
  - WFPC2: every 34.1333<sup>th</sup> row 3% shorter
  - ACS/WFC: pattern every 68.2666<sup>th</sup> column
  - WFC3/UVIS: 2-D zones
- CTE losses...
  - ACS Solution now available (WFC3 one on the way)

**Need empirical approach:** plot everything against everything else...

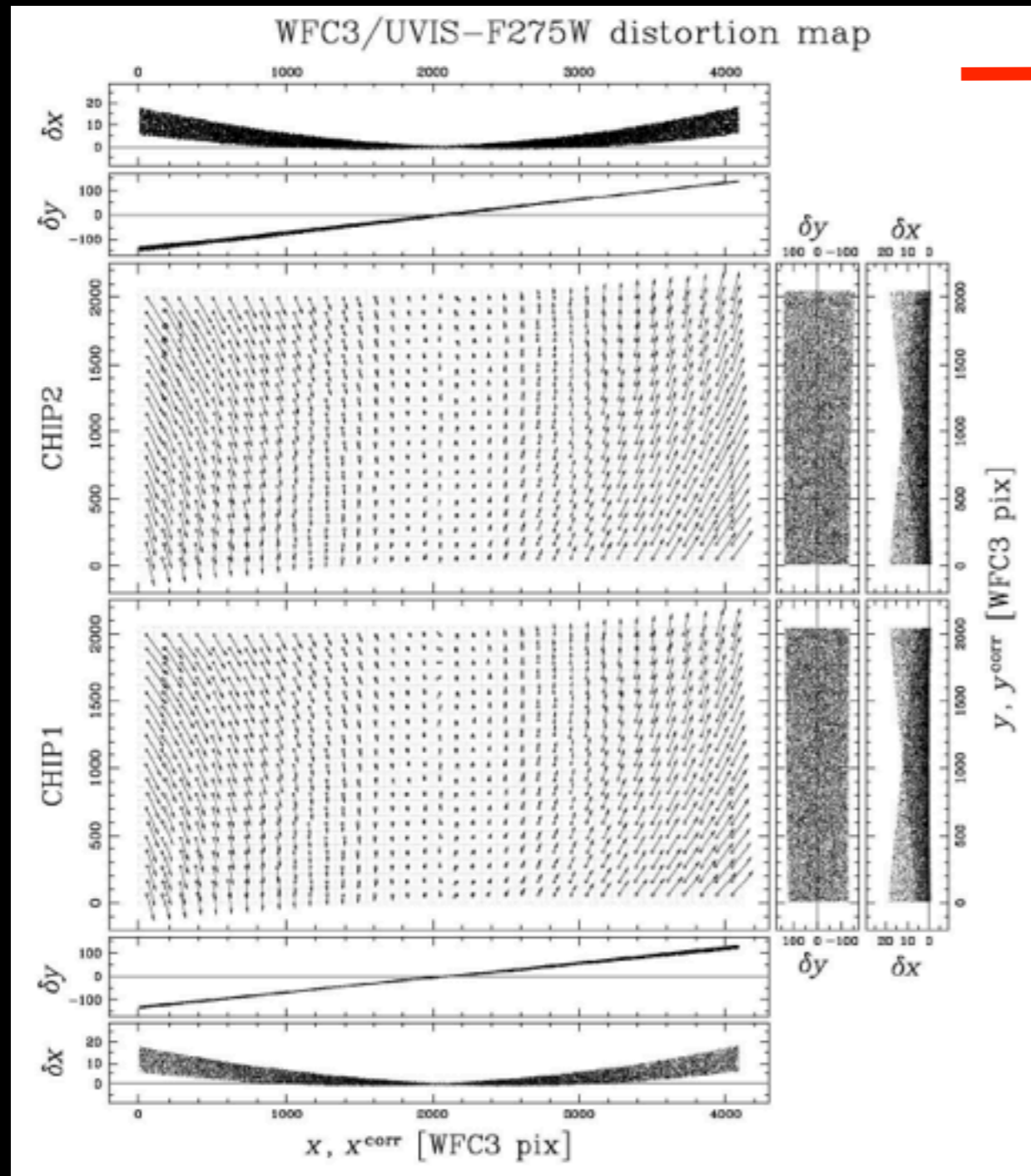
# WFC3/UVIS Geometric-Distortion Correction



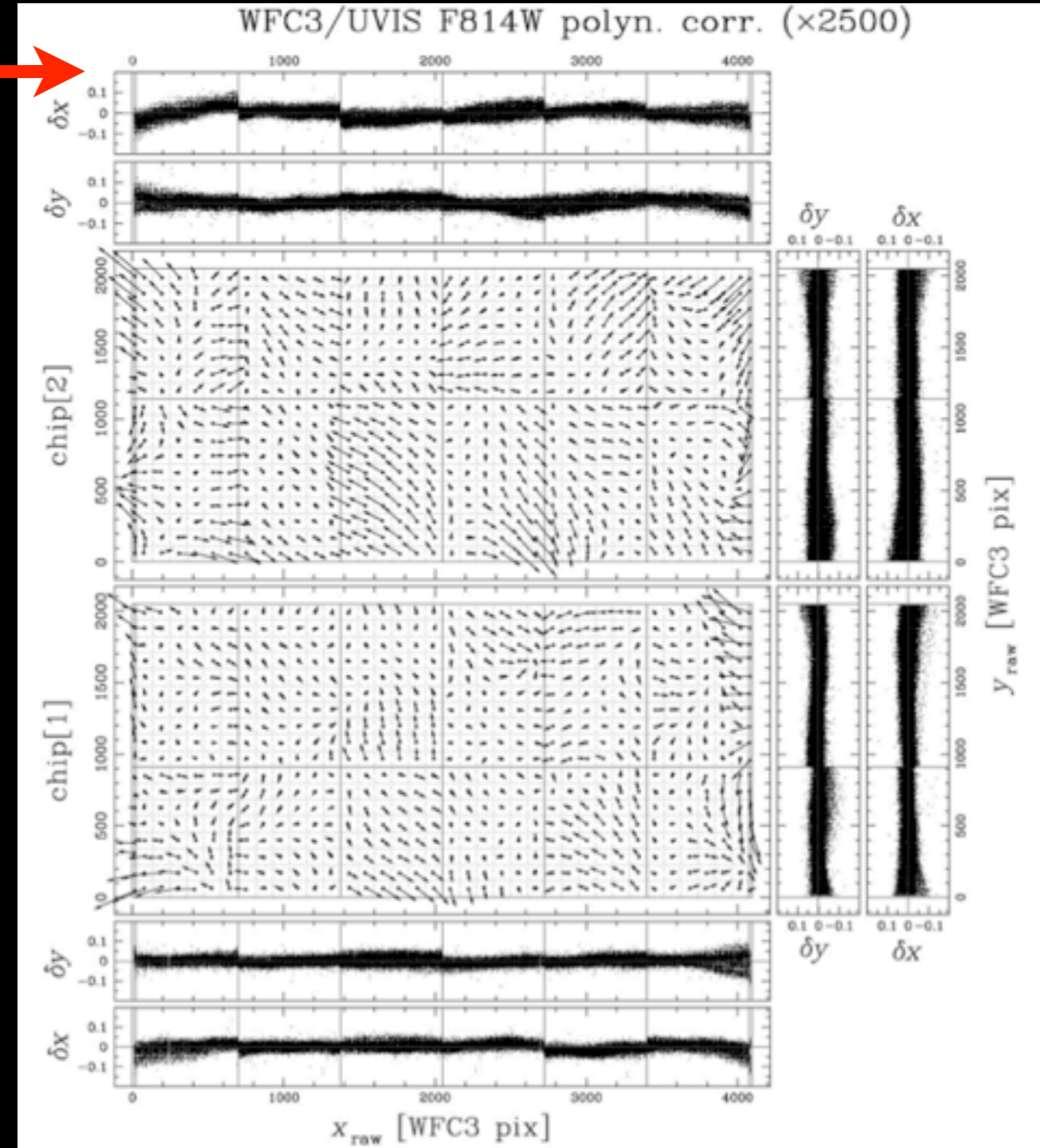
Bellini & Bedin 2009, PASP, 121, 1419

# WFC3/UVIS Geometric-Distortion Correction

## auto-calibration & polynomial solution



Bellini & Bedin 2009, PASP, 121, 1419

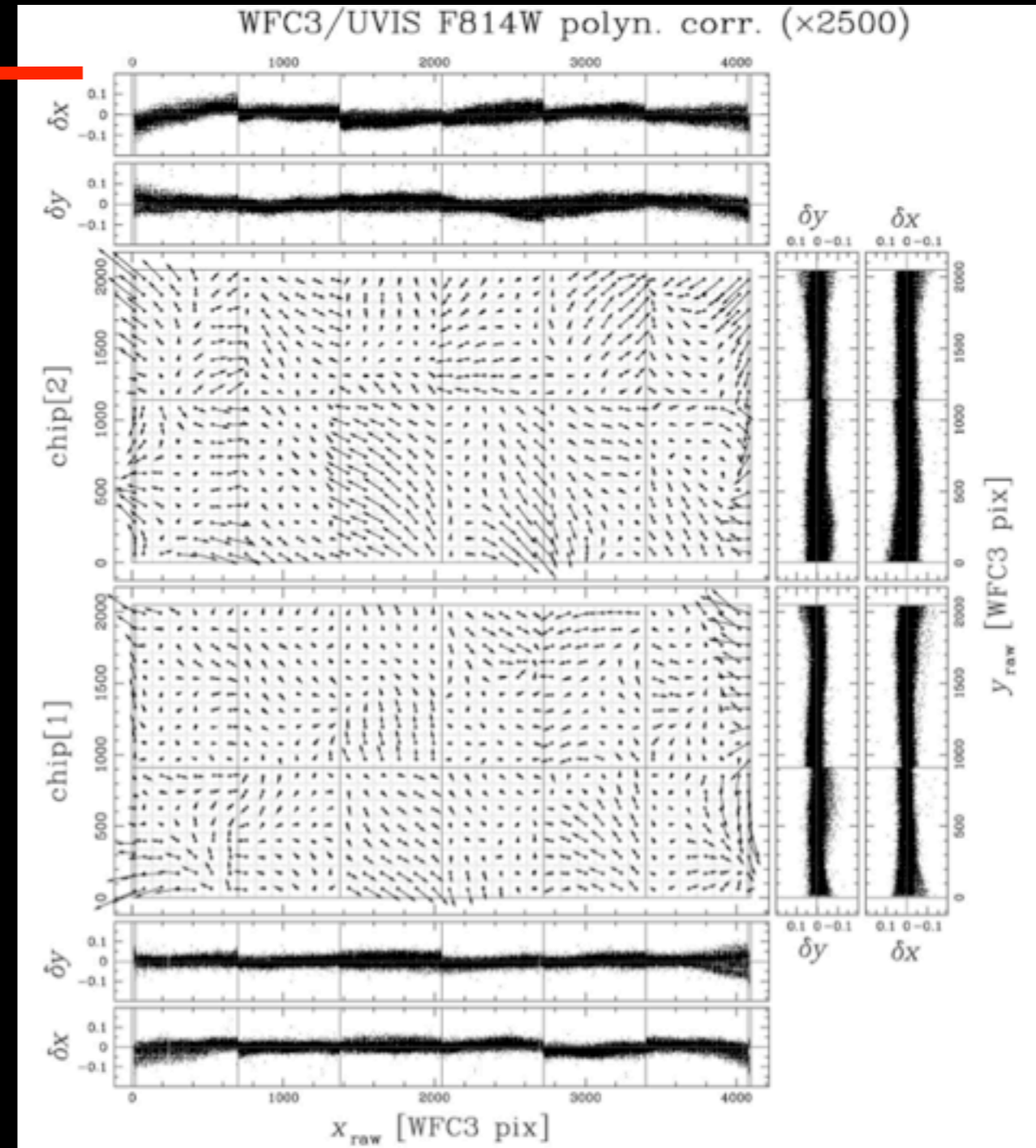
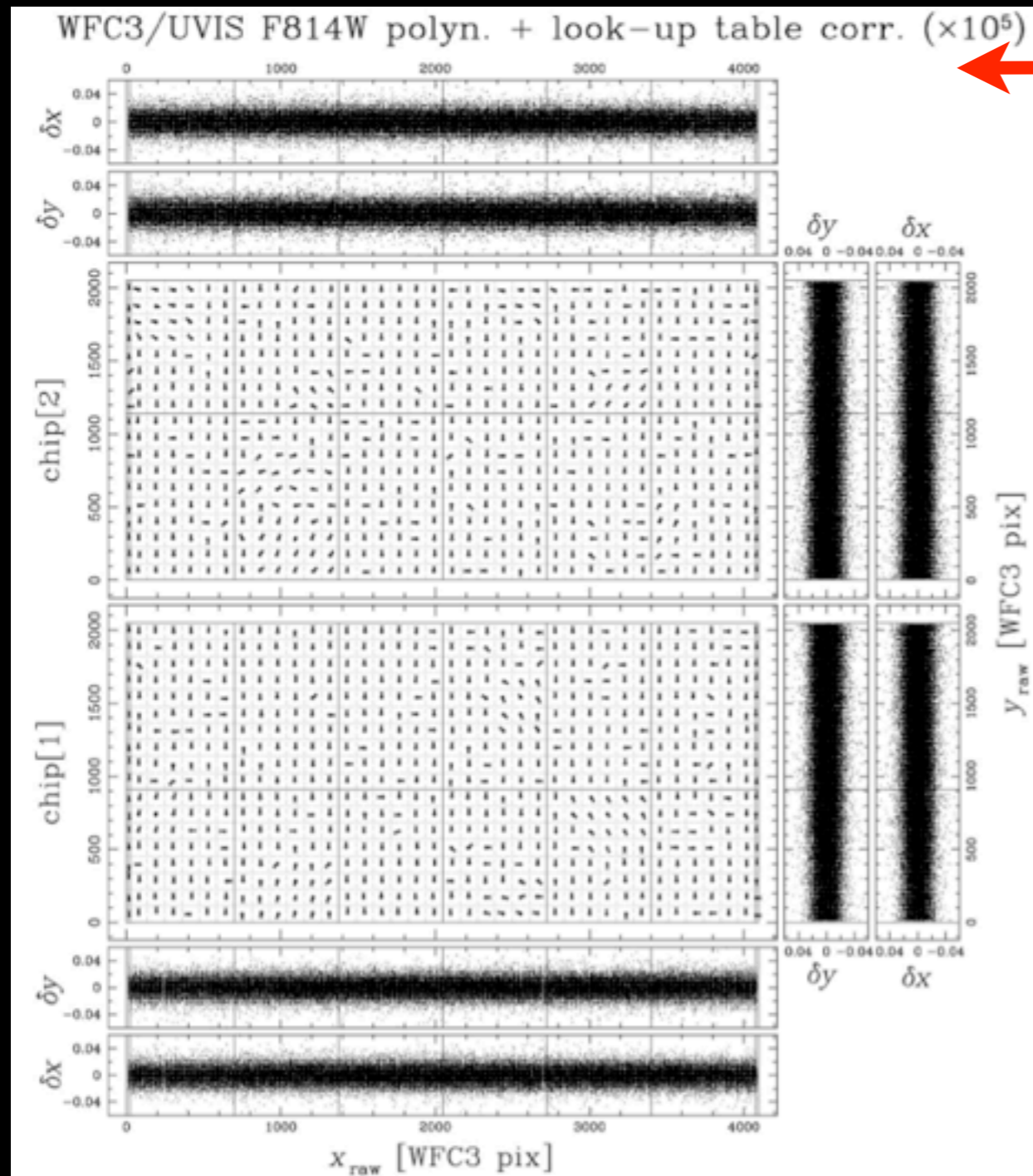


Bellini, Anderson & Bedin 2010, PASP, 123, 622



# WFC3/UVIS Geometric-Distortion Correction

## Table of residuals correction



Astrometric flat-field to the  $< 0.01$ -pixel level

Bellini, Anderson & Bedin 2010, PASP, 123, 622

## ISSUES#3: Transformations

### All *HST* astrometry is differential astrometry

- Guide-star precision  $\sim 0.5''$  (improved from  $1.5''$ !)
- No reference stars in typical field
- We never know the true pointing

### Always need to define a local reference frame

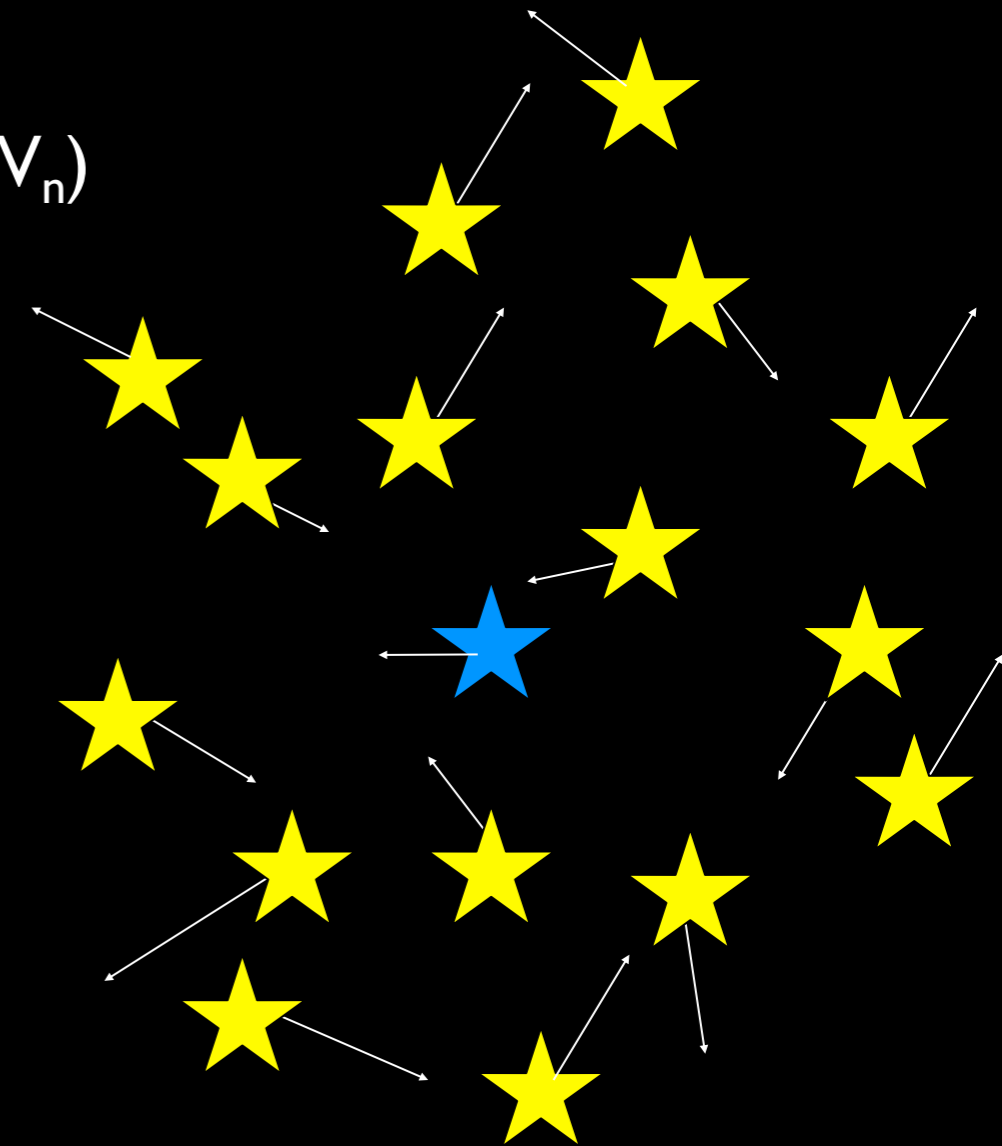
- Pixels/positions have only relative meaning
- Choosing a frame
  - \* Base it on a population of objects (3+) in the frame
  - \* Must know a priori something about the population
    - absolute  $\mu = 0$  (galaxies)
    - average  $\mu = \text{same}$  (clusters)
    - average  $\mu = \text{unchanging}$  (field)

# ISSUES#3: Transformations

## Errors in the transformations:

- “Point” associations are not perfect:  $(X_n, Y_n ; U_n, V_n)$ 
  - Stars’ measurement error
  - Proper motions (dispersion)
  - “Fuzzy handles” for galaxies/faint stars
- Distortion not perfectly removed

Make transformations more **local**



$$\rightarrow V_{\text{SYST}} = \sigma/\sqrt{N}$$

**ISSUE#1: Undersampling/PSFs**

**ISSUE#2: Distortion**

**ISSUE#3: Transformations**

**Good News!: All manageable issues**

**Undersampling/PSFs:**

- Ways to model accurately, get 0.01-pixel positions
- Libraries available, usually sufficient

**Distortion:**

- Stable, models available, small variations,  $\approx 0.01$  pixel

**Transformations:**

- Can optimize for program

**Bad news...: No one-size-fits-all solutions...**



# Science with HST proper motions

## IMBHs

- Many advantages vs. Line-of-Sight velocity studies
  - no spectra required (more/fainter stars, better statistics)
  - individual star measurements vs. integrated light
  - two components of velocity are measured (constrain velocity-dispersion anisotropy)
  - if LoS are known for some stars → 3D velocity dispersion anisotropy, better models (Schwartzchild)

## GC dispersion profiles

- PMs for nearly all stars, especially in the concentrated central regions
  - better constrains of structure, dynamics, evolution of GCs

## Geometric distances

## GC rotations

## Absolute motions

## Microlensing applications

...



Introduction



part I



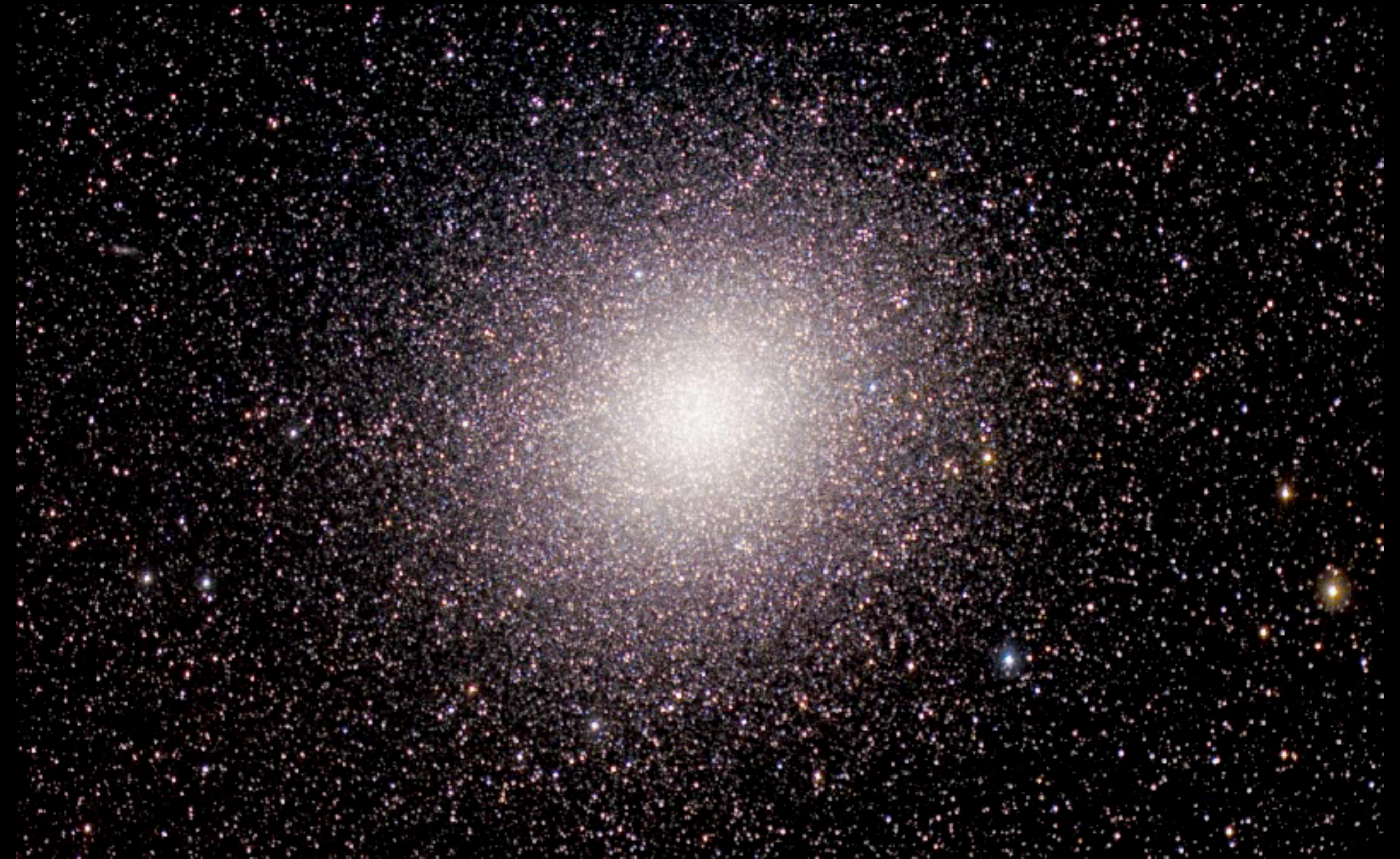
part II



part III



Conclusions



Courtesy by Jay Anderson

WFI → ACS → WFC3 → PM







## 23 GCs:

5 (PI: Chandar)

4 (PI: Brown)

3 (PI: Ford)

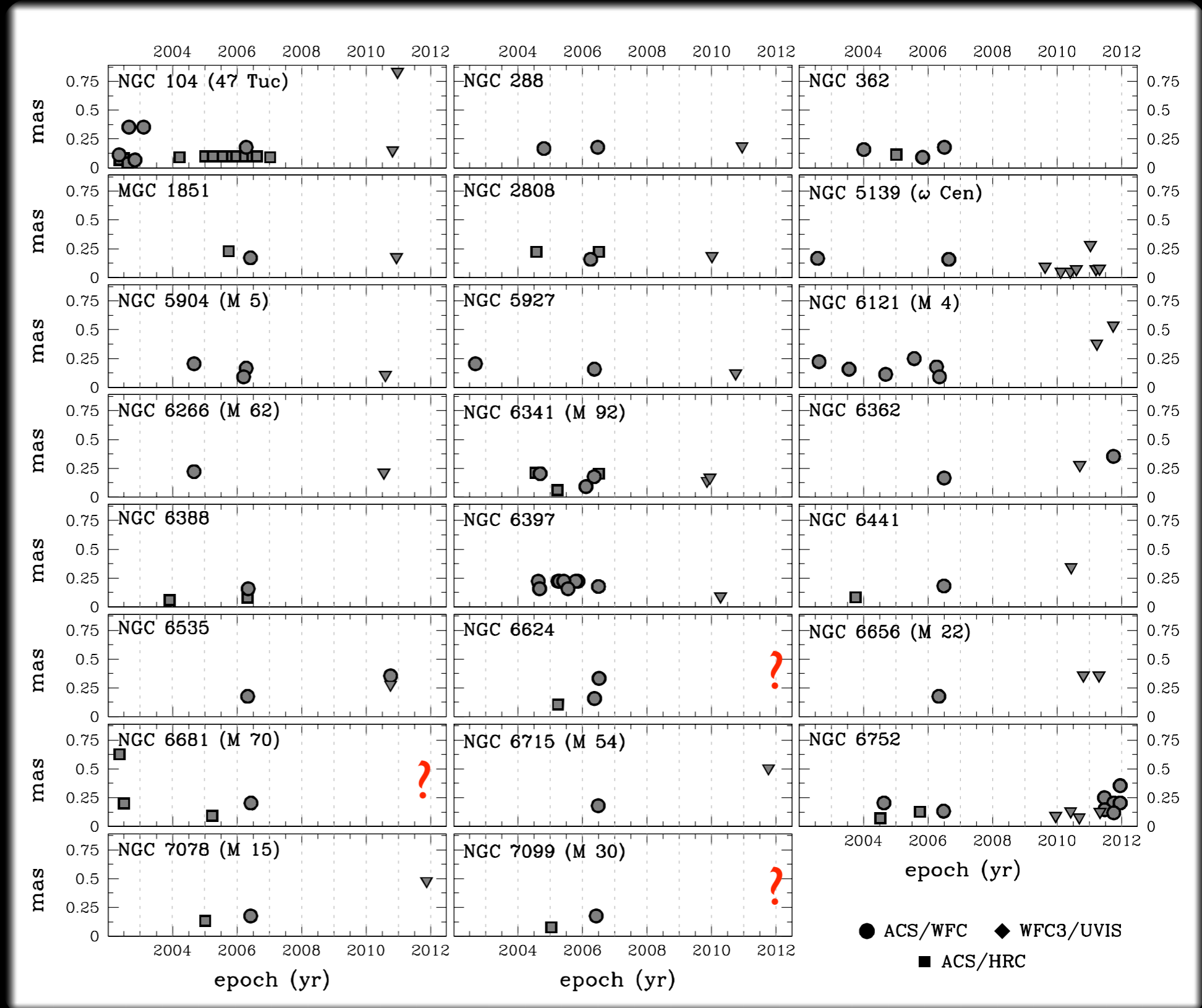
1 (PI: van der Marel)

10 from HST archive

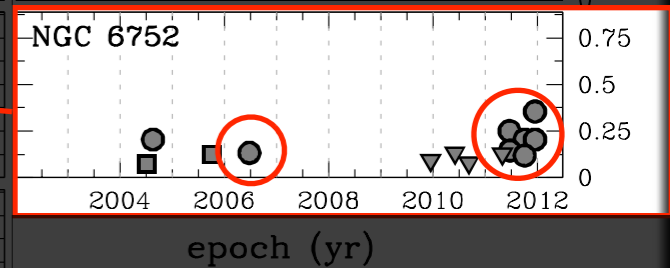
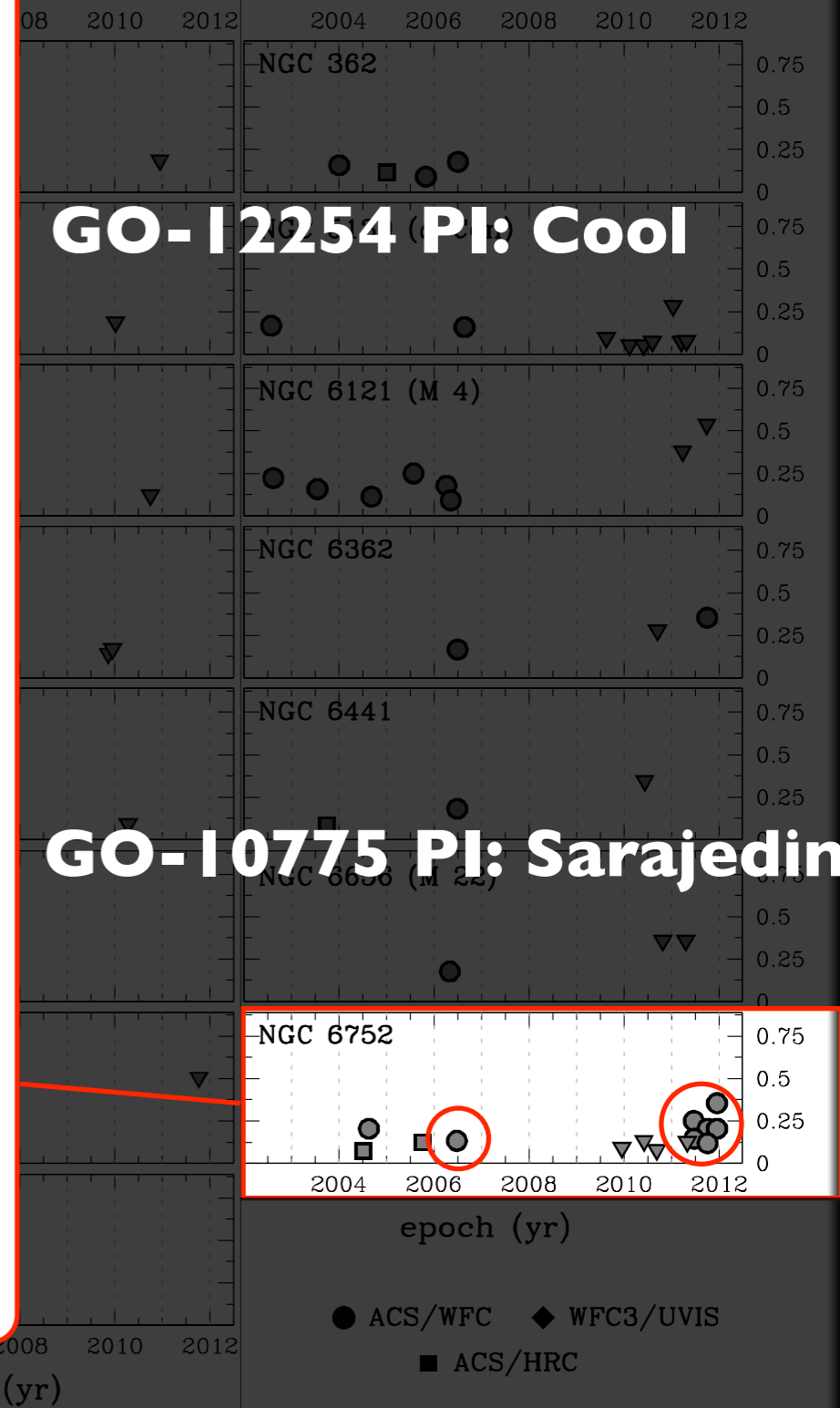
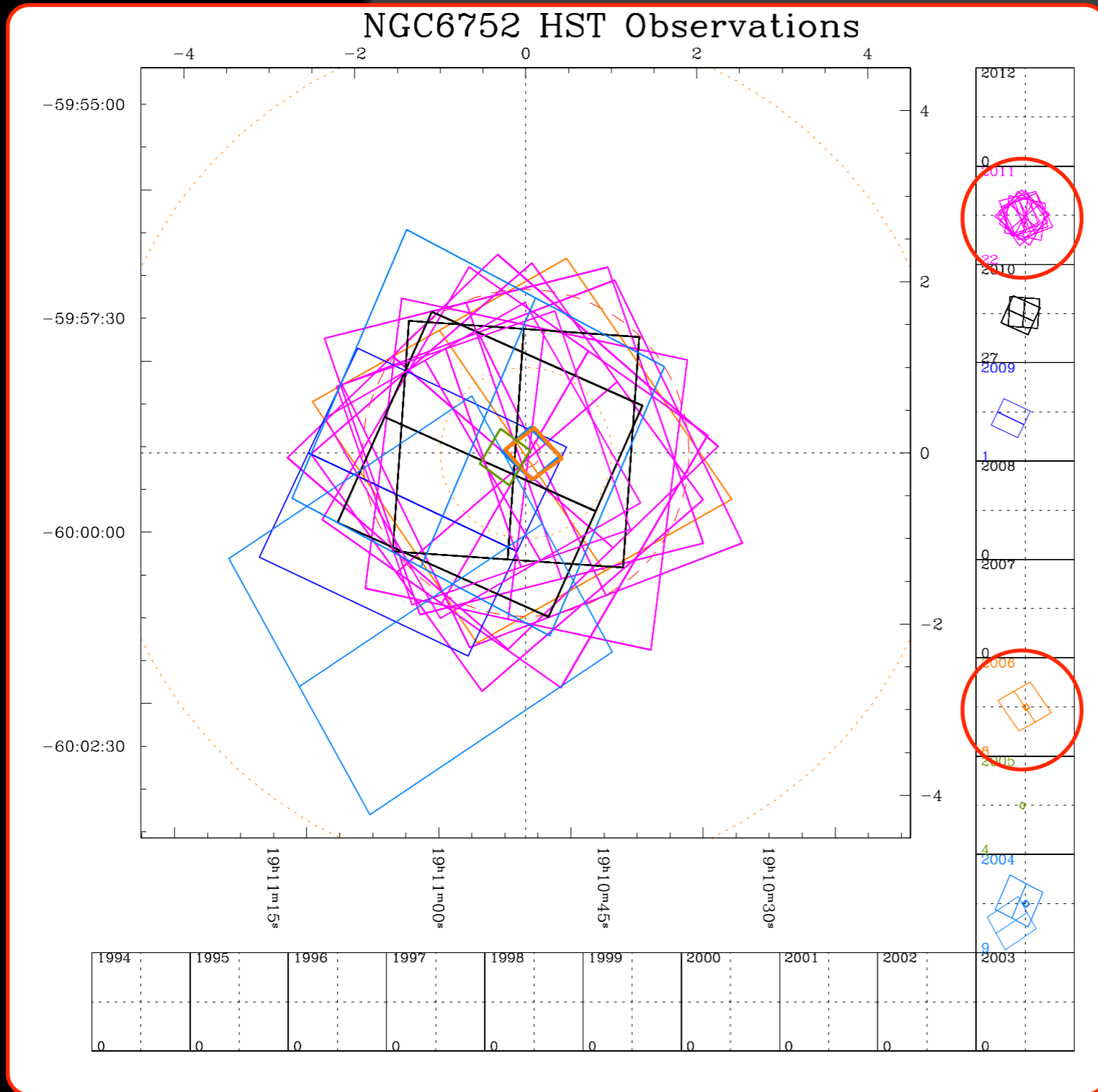
### Heterogeneous datasets:

- different epoch coverage
- different cameras
- different filters
- different S/N

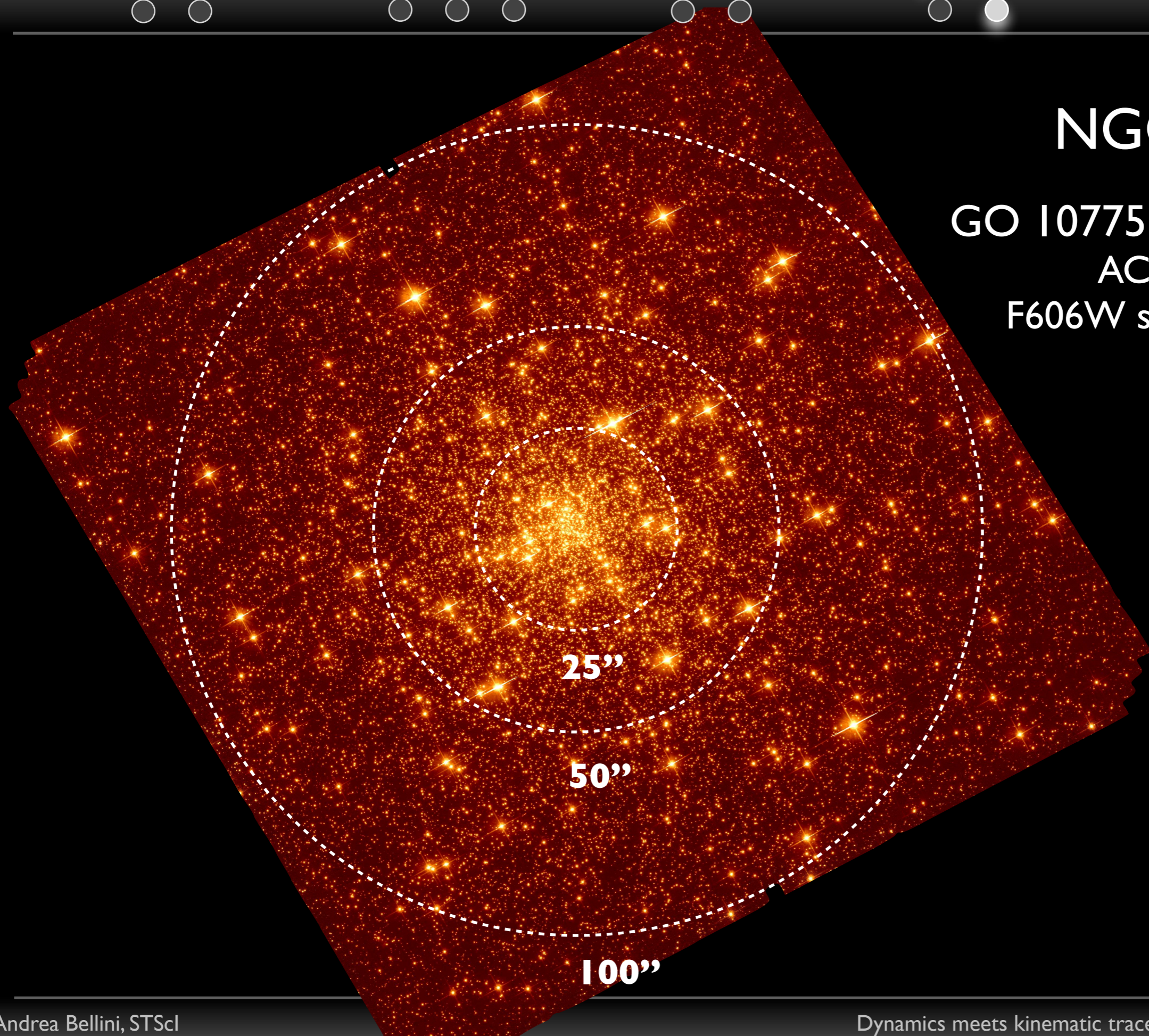
### Homogeneous reductions











# NGC 6752

GO 10775 (PI: Sarajedini)

ACS/WFC

F606W stacked image

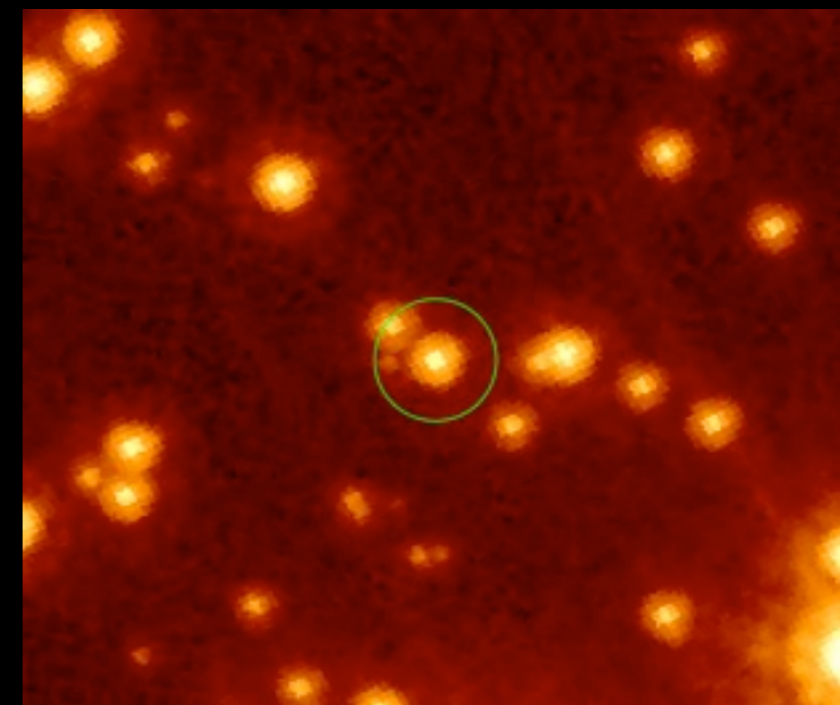
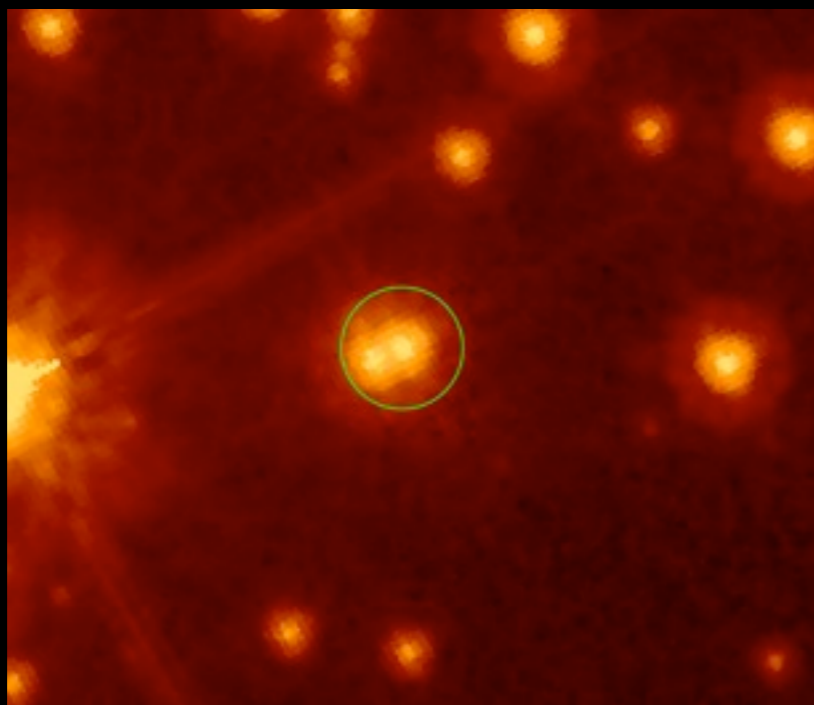
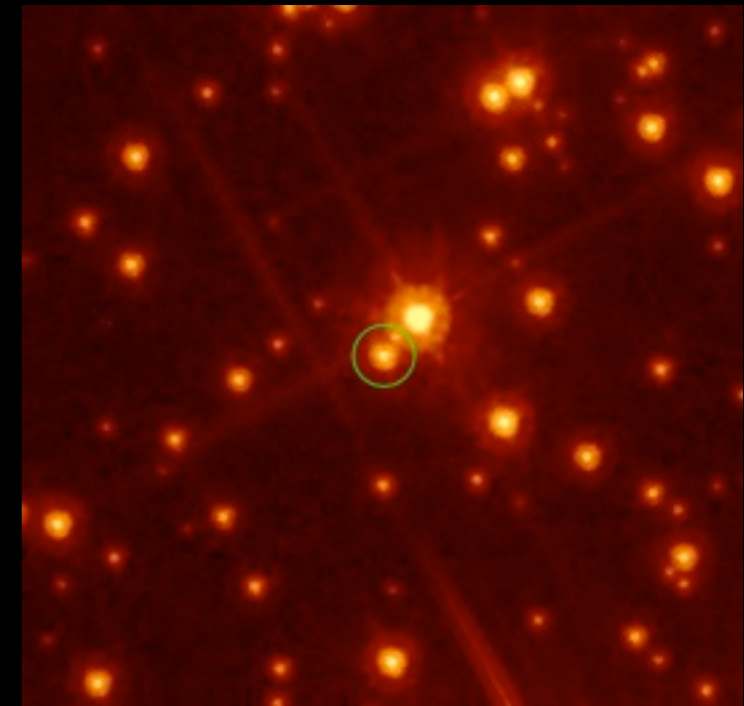
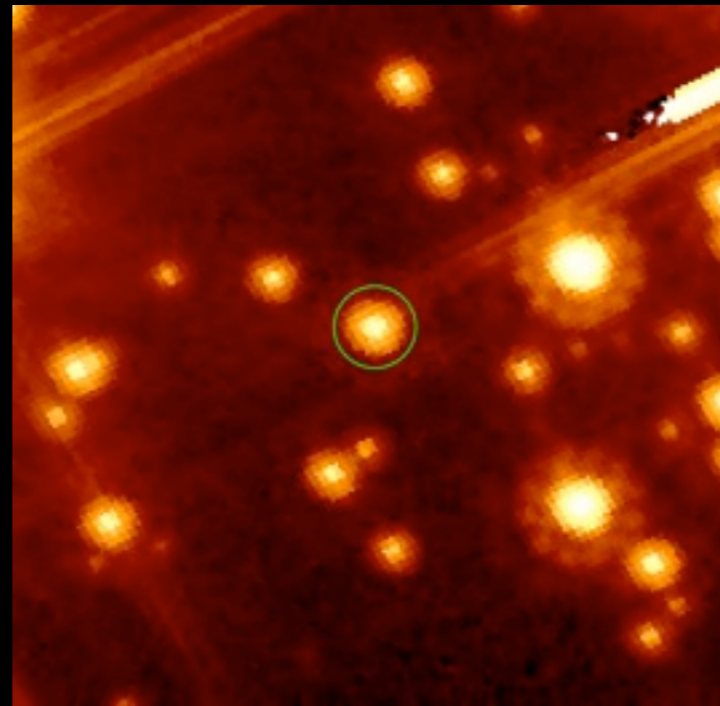
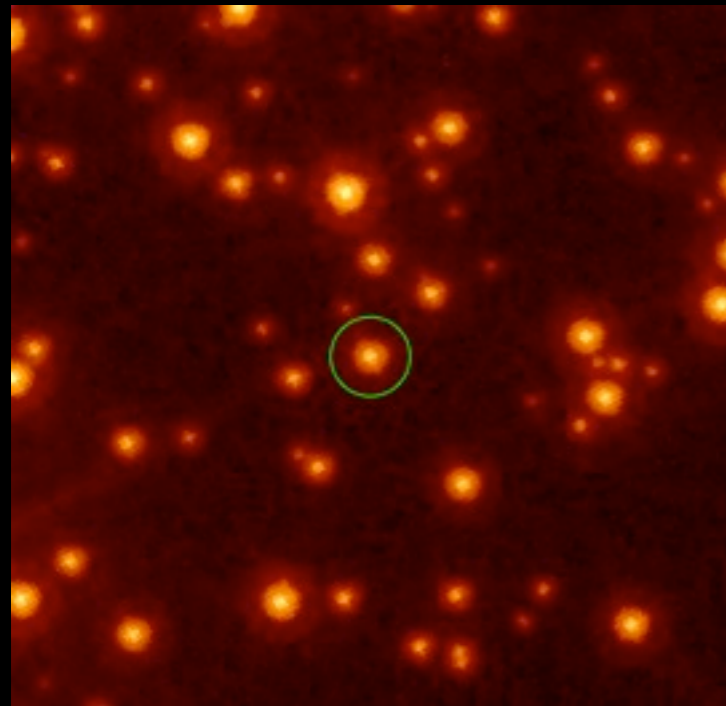
25''

50''

100''

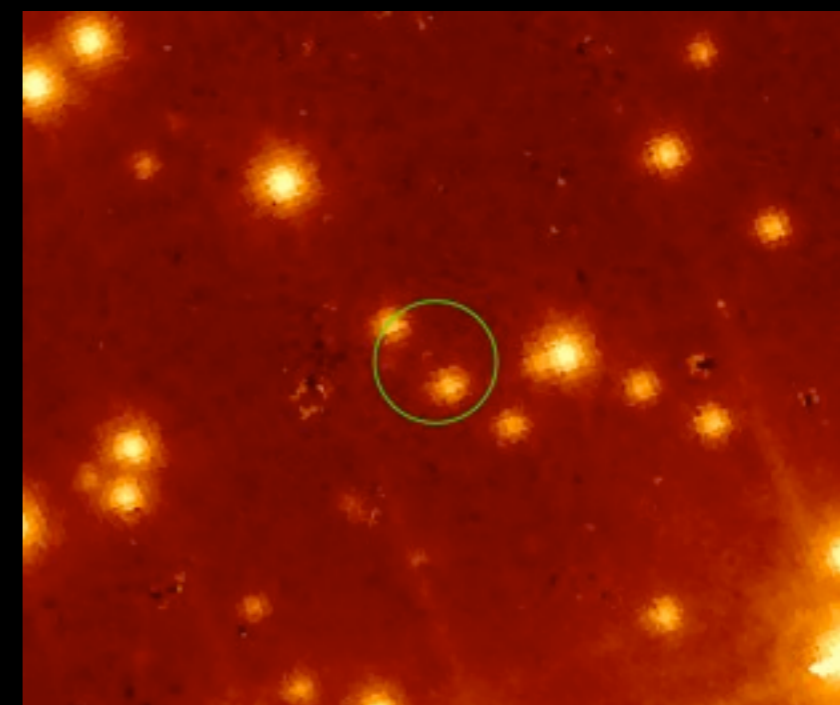
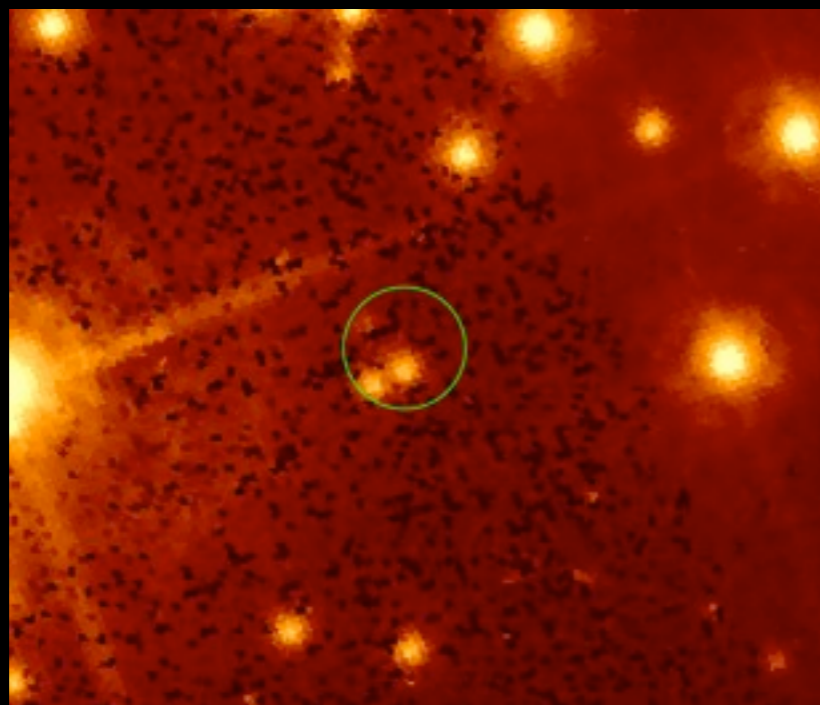
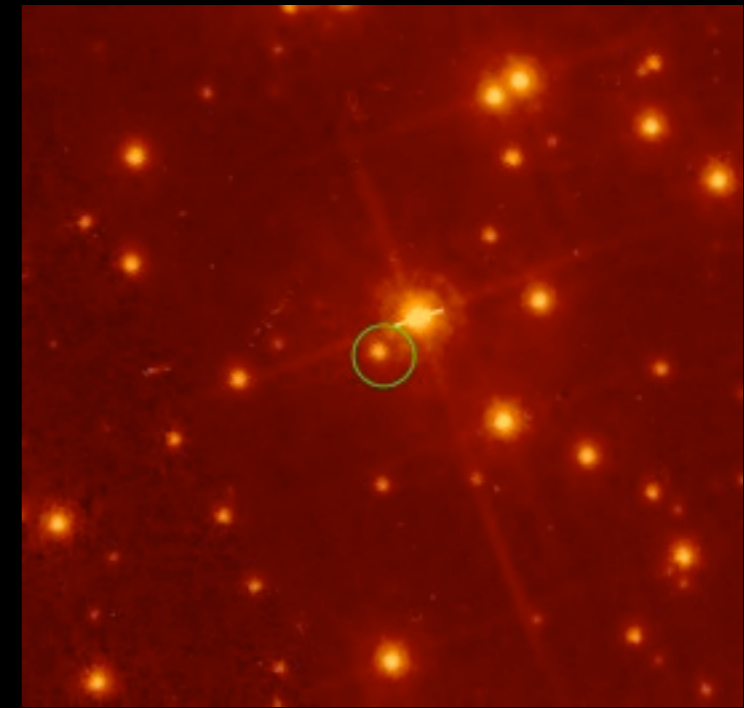
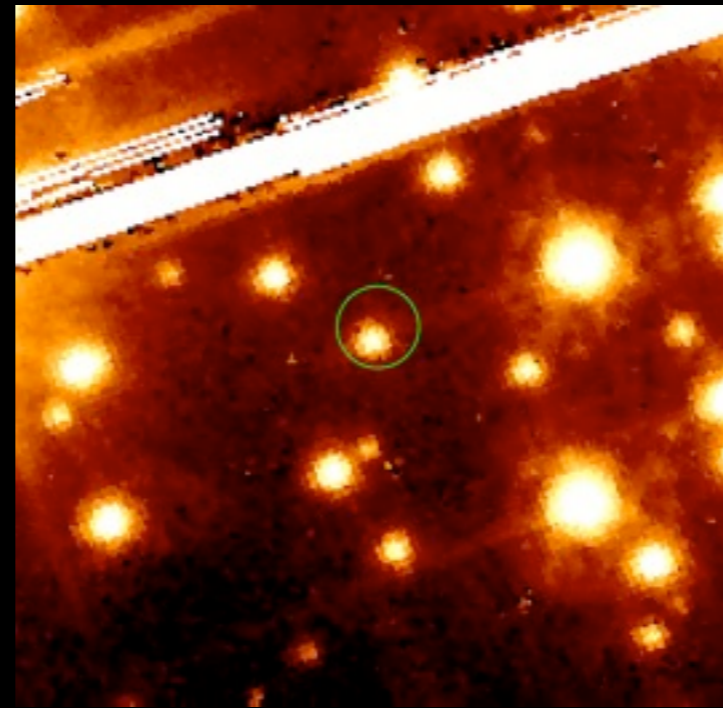
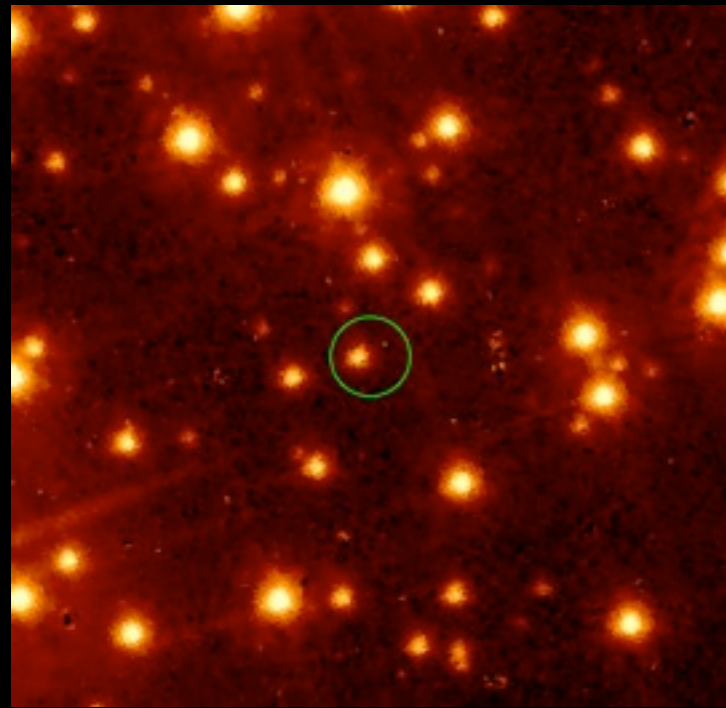


# Proper motion: Cluster and Field stars



blink!

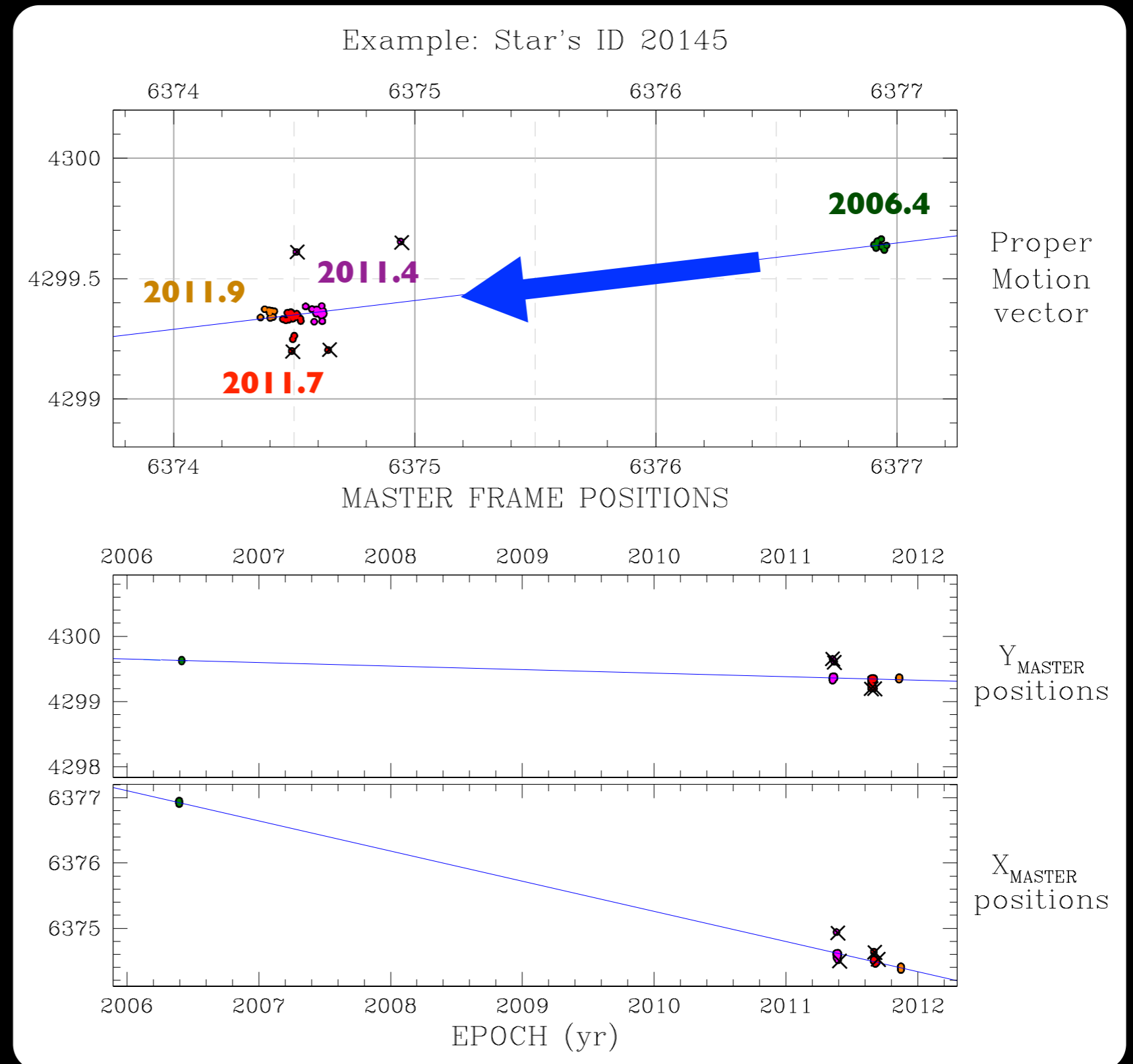
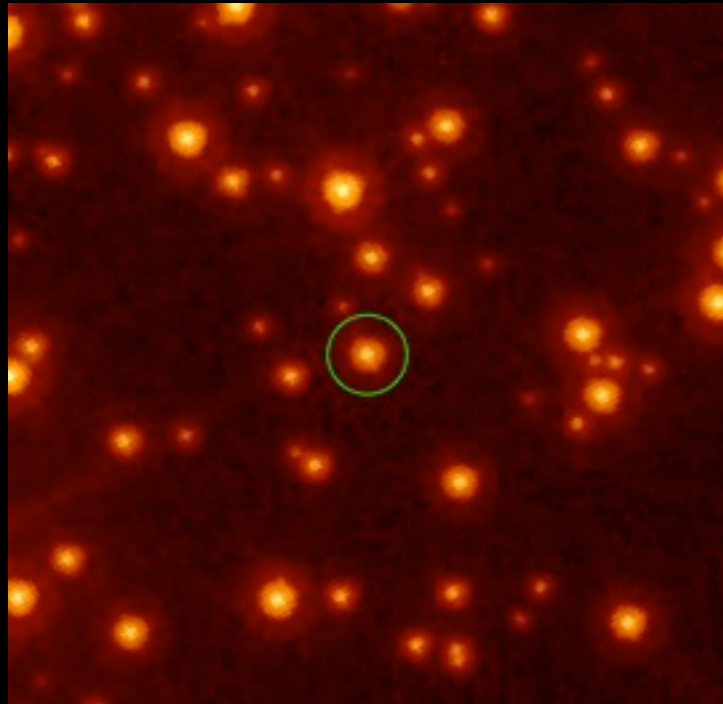
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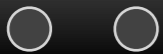




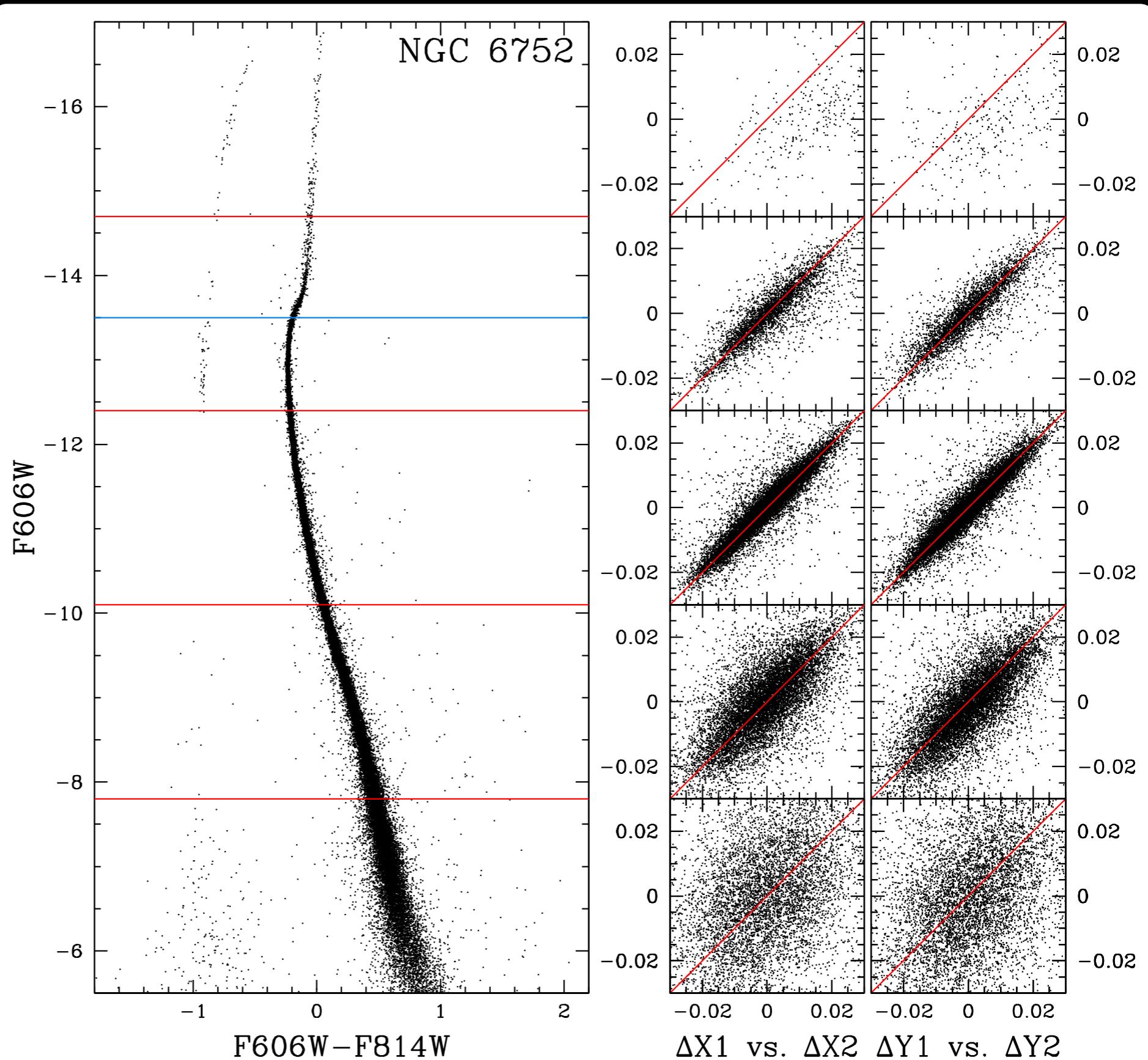
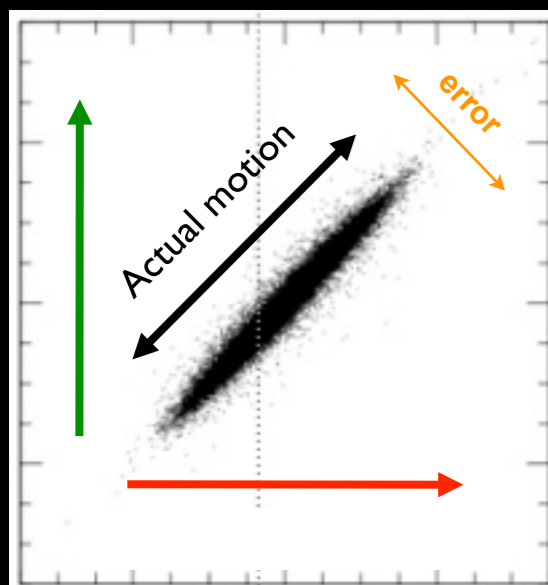
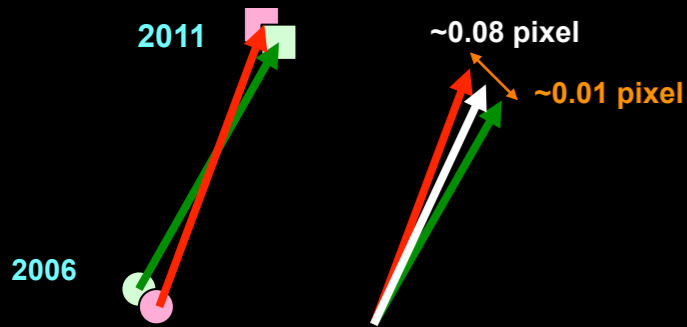
# Proper-Motion derivation (GO-10775 & GO-12254)

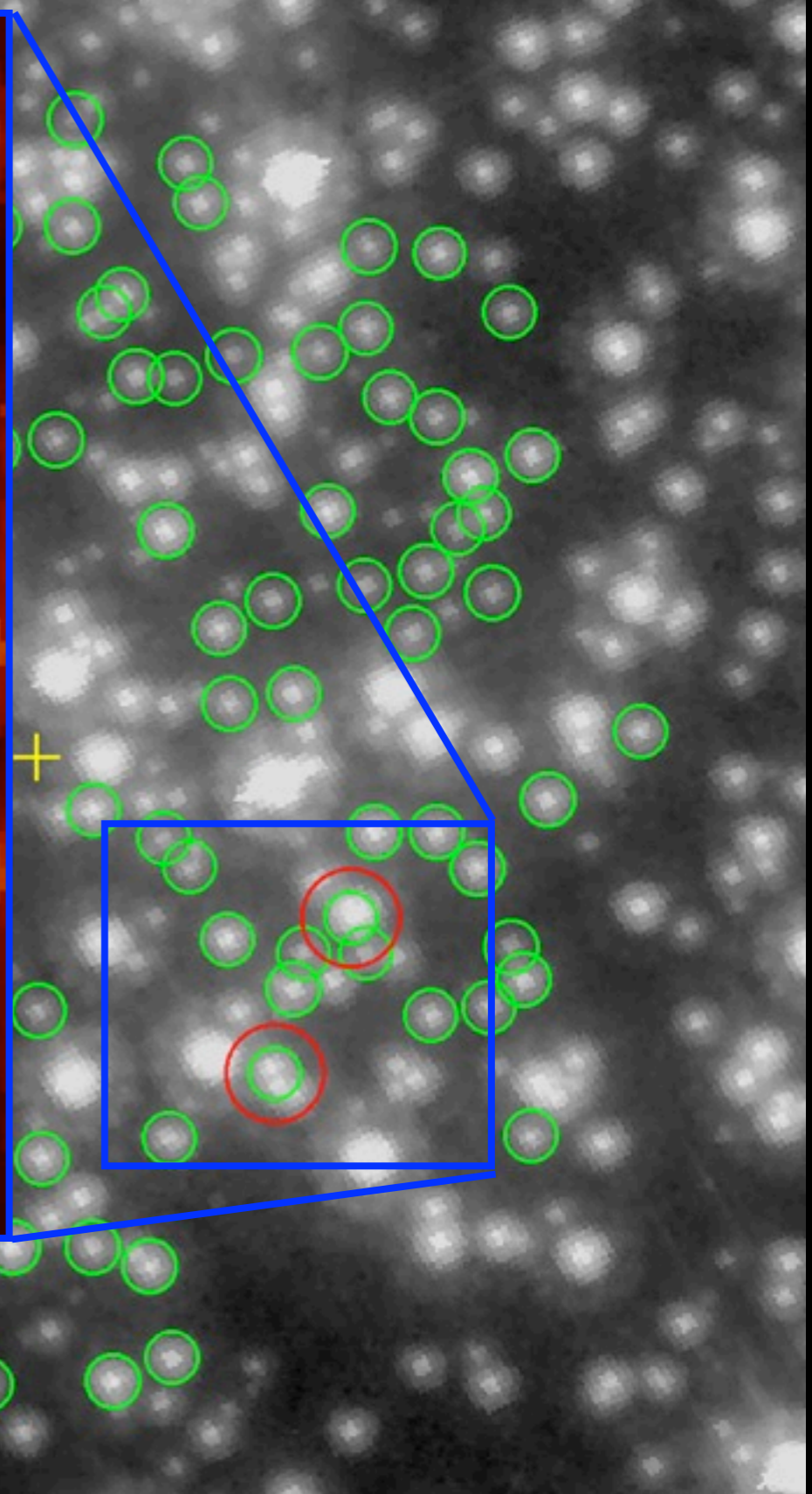
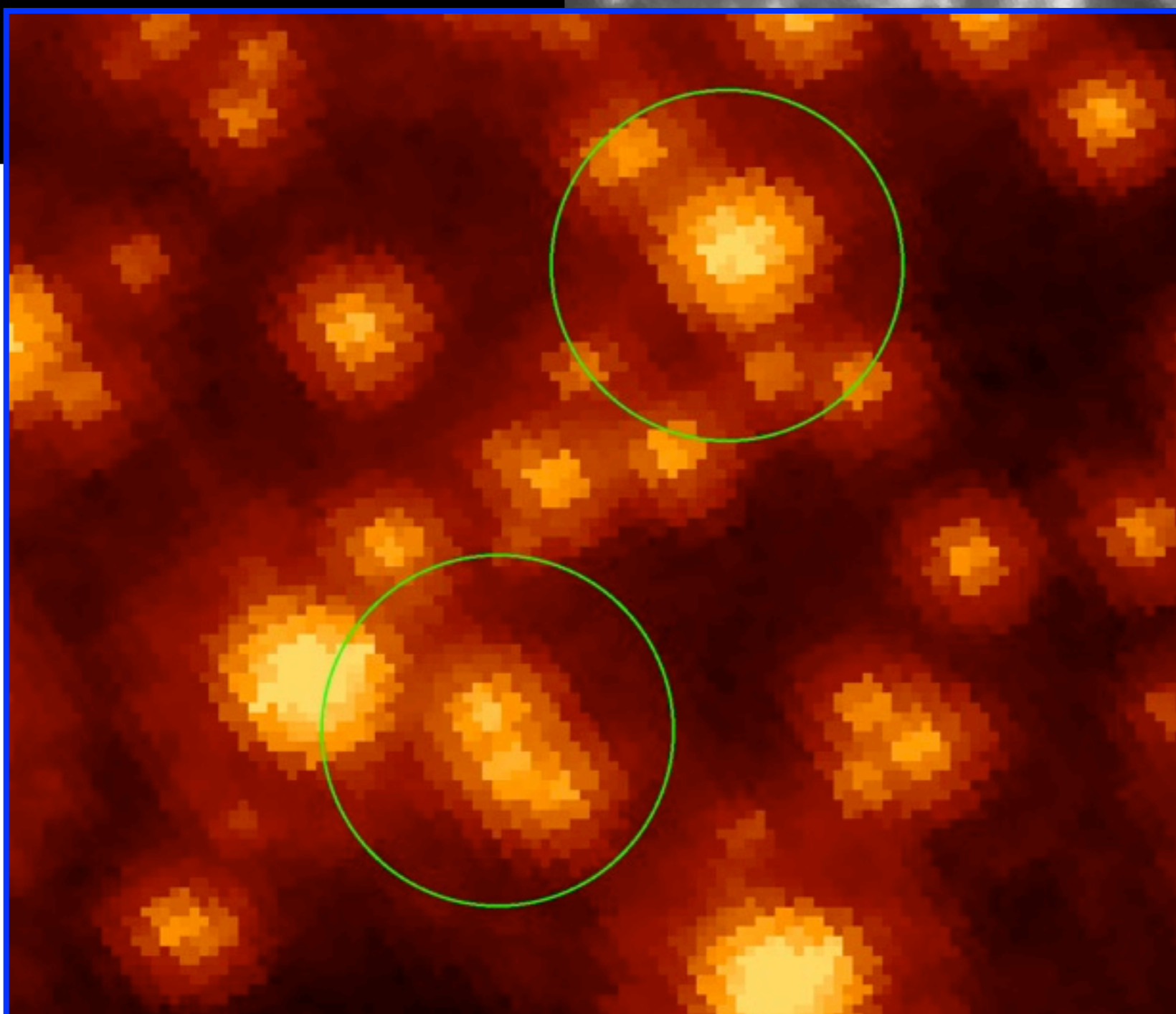




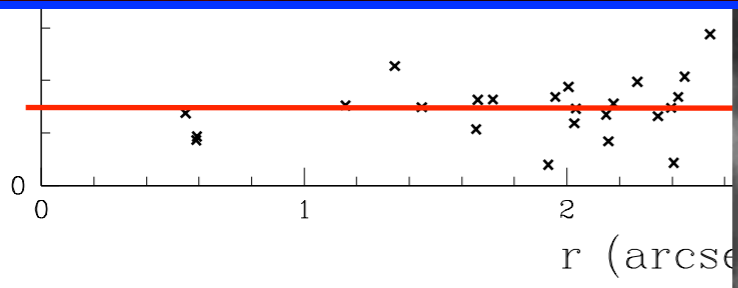


# High-quality Internal proper motions for several thousands stars





$\mu$



# Conclusions

High-precision astrometry with *HST* challenging but **DOABLE**

- undersampling (PSF)
- geometric distortion
- differential nature (local transformations)

Scientific projects with *HST*'s proper motions of GCs

- IMBHs
- dispersion profiles
- anisotropy
- rotation
- ...

Our project

- high-precision ( $\sim 2$  km/s per epoch) proper motions in the cores of 23 GCs
- preliminary results encouraging
- panchromatic proper-motion catalogs will be made publicly available