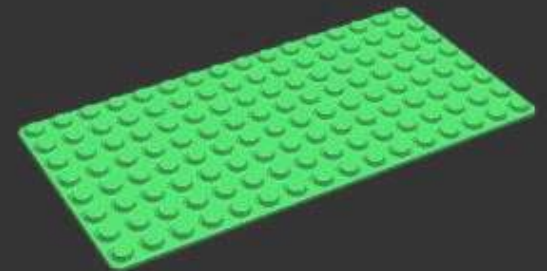


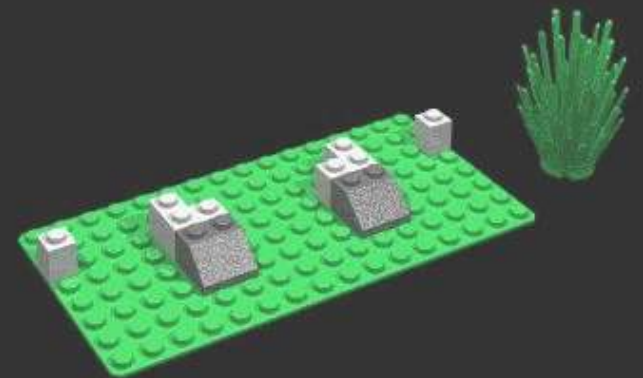
# THE STRUCTURE OF GALAXY CLUSTERS from optical observations

Andrea Biviano  
INAF / Oss. Astron. Trieste



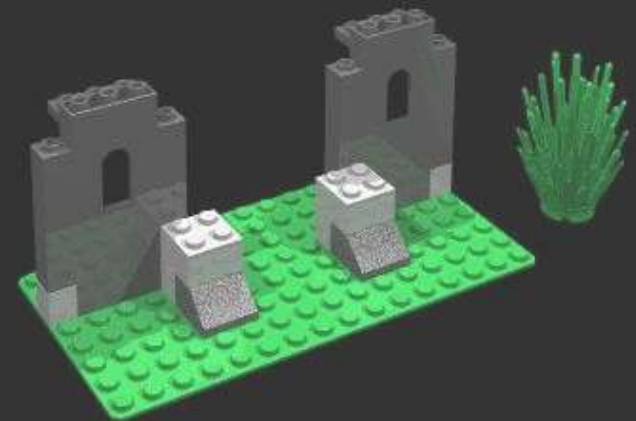
# from optical observations... ...lensing excluded!

*(see talks by Treu, Kneib, Reiprich...)*

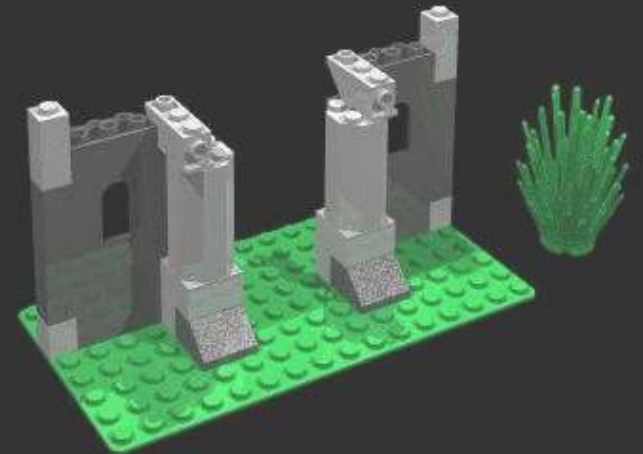


# Plan of the review talk:

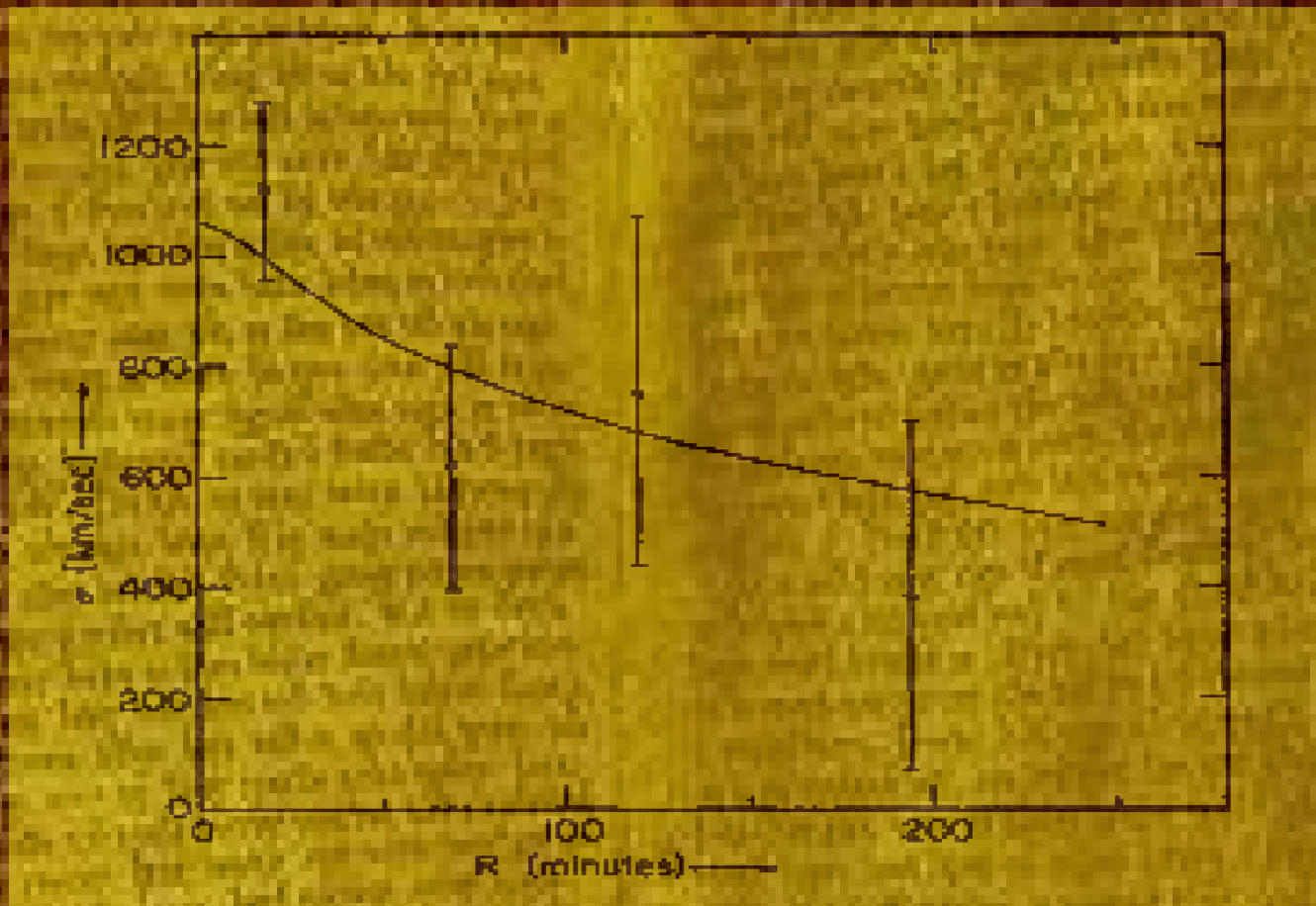
- Mass profile
- Mass-to-light profile,  
i.e. the relative distribution of dark matter and galaxies
- Orbital structure
- Shape
- Substructure
- Scaling relations  
i.e.  $M/L$  vs. the halo mass or  $M$  vs.  $N_{gal}$   
or the fundamental plane of  
galaxy clusters properties



# Mass profile



# Historical



Model fit to Coma velocity dispersion profile  
from Rood et al. (1972)

# Scientific motivations

- Is the mass profile universal?
- Does it depend on the halo mass?
- How does it evolve?  
*...constrains theories of structure formation*
- What is its form?  
*...constrains nature of dark matter*

# M(<r) from the Jeans analysis

(e.g. Binney & Tremaine 1987)

Assumes dynamical equilibrium of the system

$I(R)$  and  $\sigma_v(R) \leftrightarrow v(r), \sigma_r(r), M(<r)$ , through  $\beta(r)$

or, more generally:  $f_p(R,v) \leftrightarrow \Phi(r) + f(E,L^2)$

Mass – orbits degeneracy: given  $R,v$   
the  $M(<r)$  solution depends on  $\beta(r)$

( $\beta(r) \equiv 1 - \sigma_t^2/\sigma_r^2$ , velocity anisotropy profile)

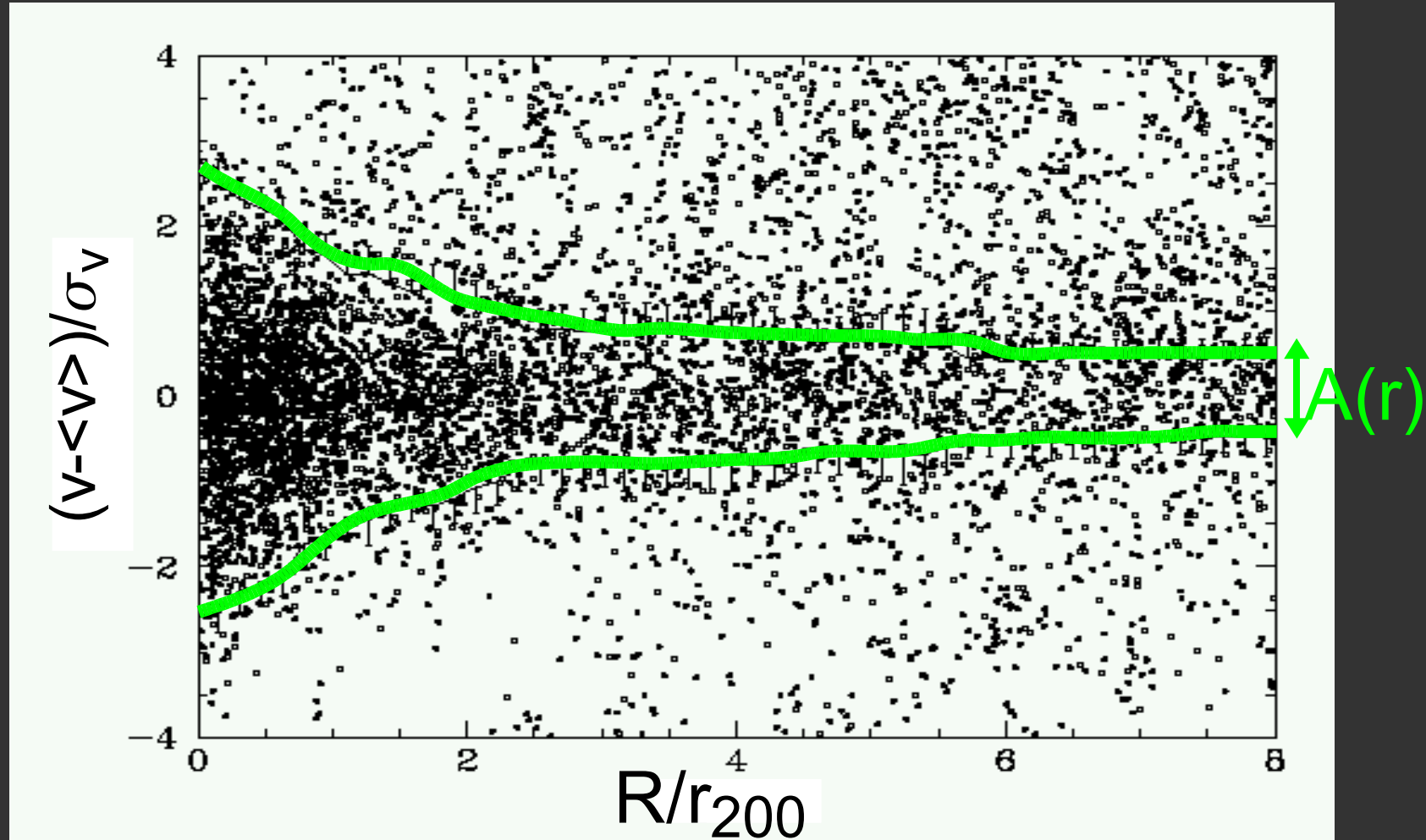
Possible solutions to the problem include:

- analysis of the shape of the velocity distribution
- use of several tracers of the cluster potential

# M(<r) from the caustic method:

(Diaferio & Geller 1997) Num.sims. predict cluster dynamics dominates v-field around cluster, i.e. (R,v) caustic amplitude A(r) is a measure of  $\Phi(r)$ , independently of dynamical state

(from Rines et al. 2003)



$A(r) \rightarrow \Phi(r)$  through  $F(\Phi, \beta, r) \approx \text{const} \dots$  only at large radii

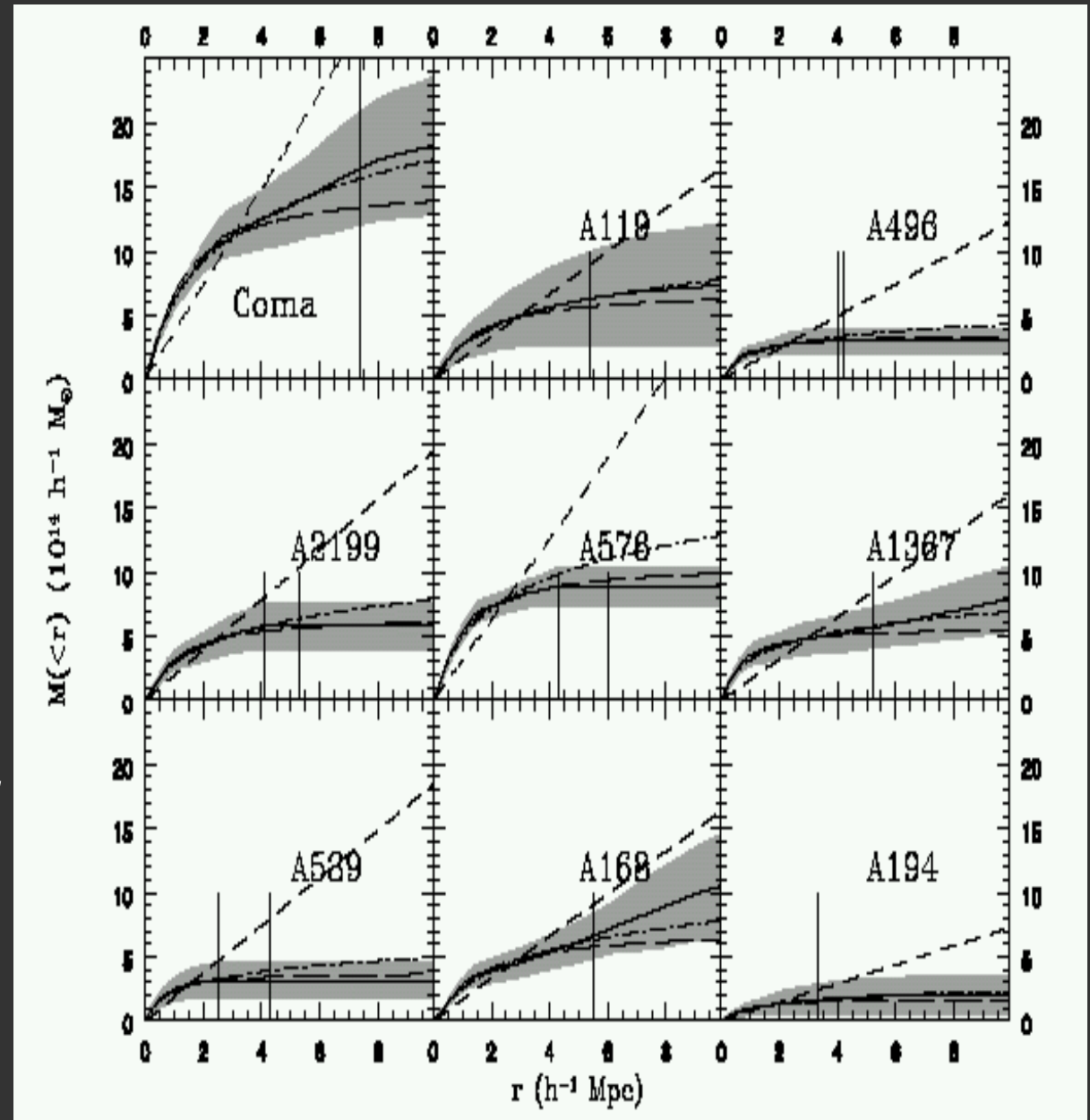


# M(<r) results: CAIRNS & Coma

Rines et al. 00,03,04  
9 nearby clusters

Best fit  $\rho(r) \sim r^{-1}$  for  $r \sim 0$ ,  
and  $r^{-3}$  or  $r^{-4}$  for large  $r$   
NFW with  $5 \leq c \leq 17$

Other results on Coma:  
(Merritt & Saha 93,  
Geller et al. 99, Rines et al. 01,  
Tokas & Mamon 04)  
 $\rho(r) \sim r^{-1}$  or  $r^{-2}$  for  $r \sim 0$ ,  
and  $r^{-3}$  or  $r^{-4}$  for large  $r$   
NFW with  $8 \leq c \leq 10$



Short-dashed: isoth., long-dashed: Hernquist, dash-dotted: NFW

# M(<r) results: 2dFGRS

(B. & Girardi 03): 1345 member gals at  $r \leq 2 r_{200}$   
in 43 non-interacting nearby clusters

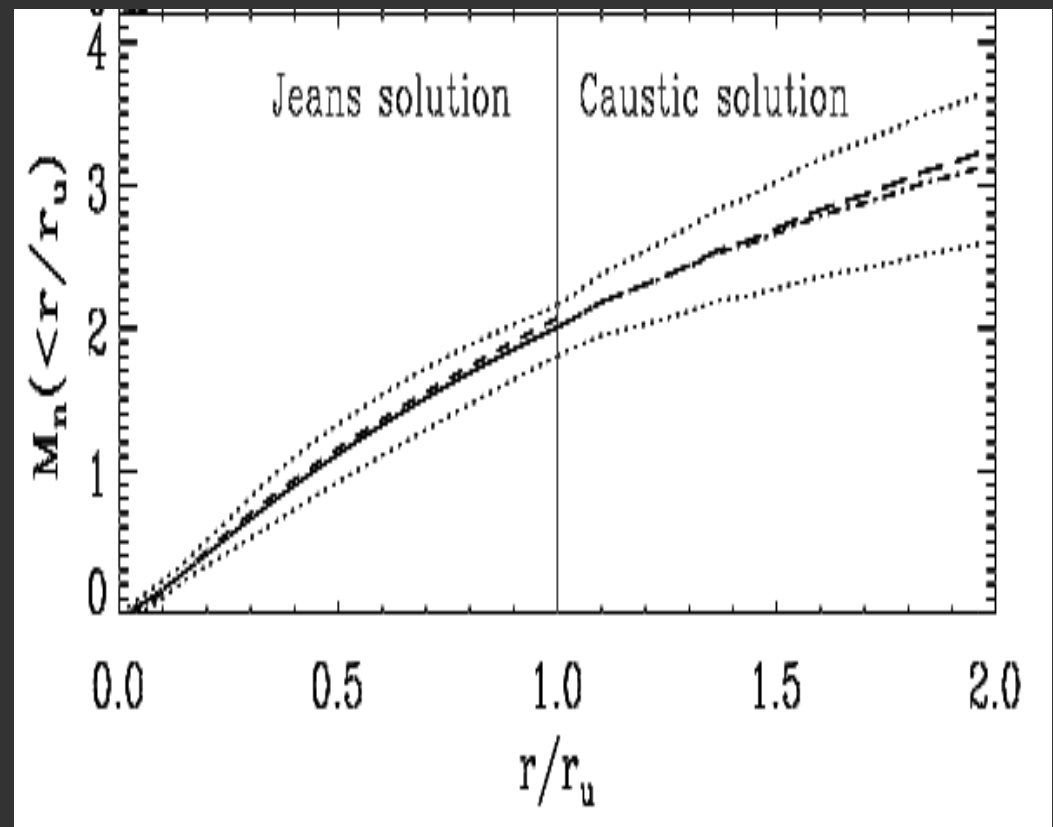
*Combine the Jeans and the Caustic methods*

$$\rho(r) \propto (r/a)^{-\xi} (1+r/a)^{\xi-3}$$

best-fit  $\xi=1.4$

NFW  $c=5.6$  also OK,  
cored profiles only OK if  
core radius small  $< 0.1 r_{200}$

The caustic solution shows  
that the Jeans solution  
is also valid at large  $r$ ,  
i.e.  $\rho(r) \sim r^{-3}$



# M(<r) results: ENACS *(Katgert, B. & Mazure 04)*

3056 member gals at  $r \leq 1.5 r_{200}$  in 59 nearby clusters

Jeans method applied on raw smoothed data – no model

*Several tracers of the potential used*

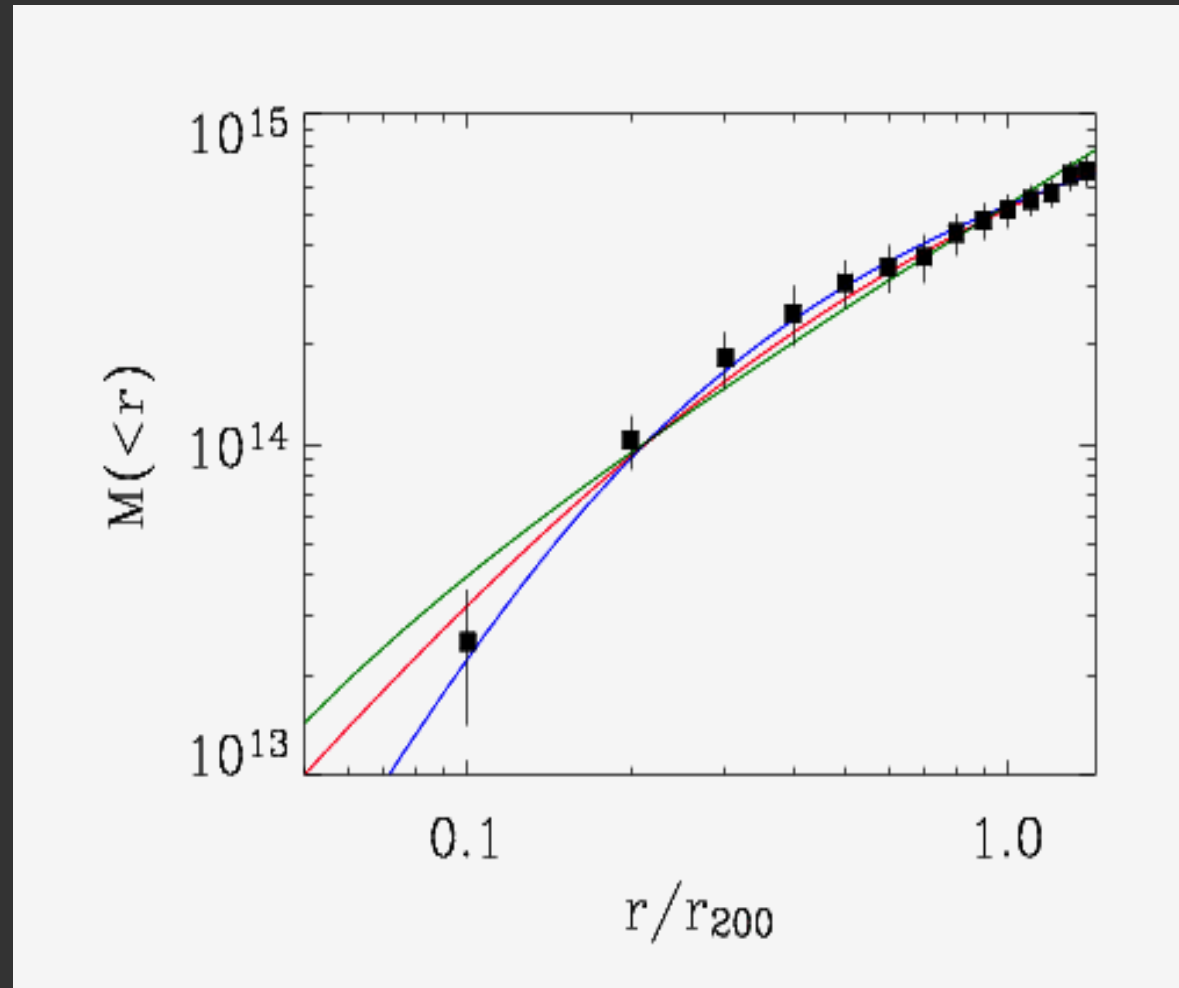
$$\rho(r) \propto r^{-2.4 \pm 0.4} \text{ at } r=r_{200}$$

Fitting models:

NFW  $c=4 \pm 2$ ,

Burkert 95  $r_{\text{core}}=0.15 r_{200}$

Isothermal gives poor fit



# $M(<r)$ results: ENACS *(Katgert, B. & Mazure 04)*

3056 member gals at  $r \leq 1.5 r_{200}$  in 59 nearby clusters

Jeans method applied on raw smoothed data – no model

*Several tracers of the potential used*

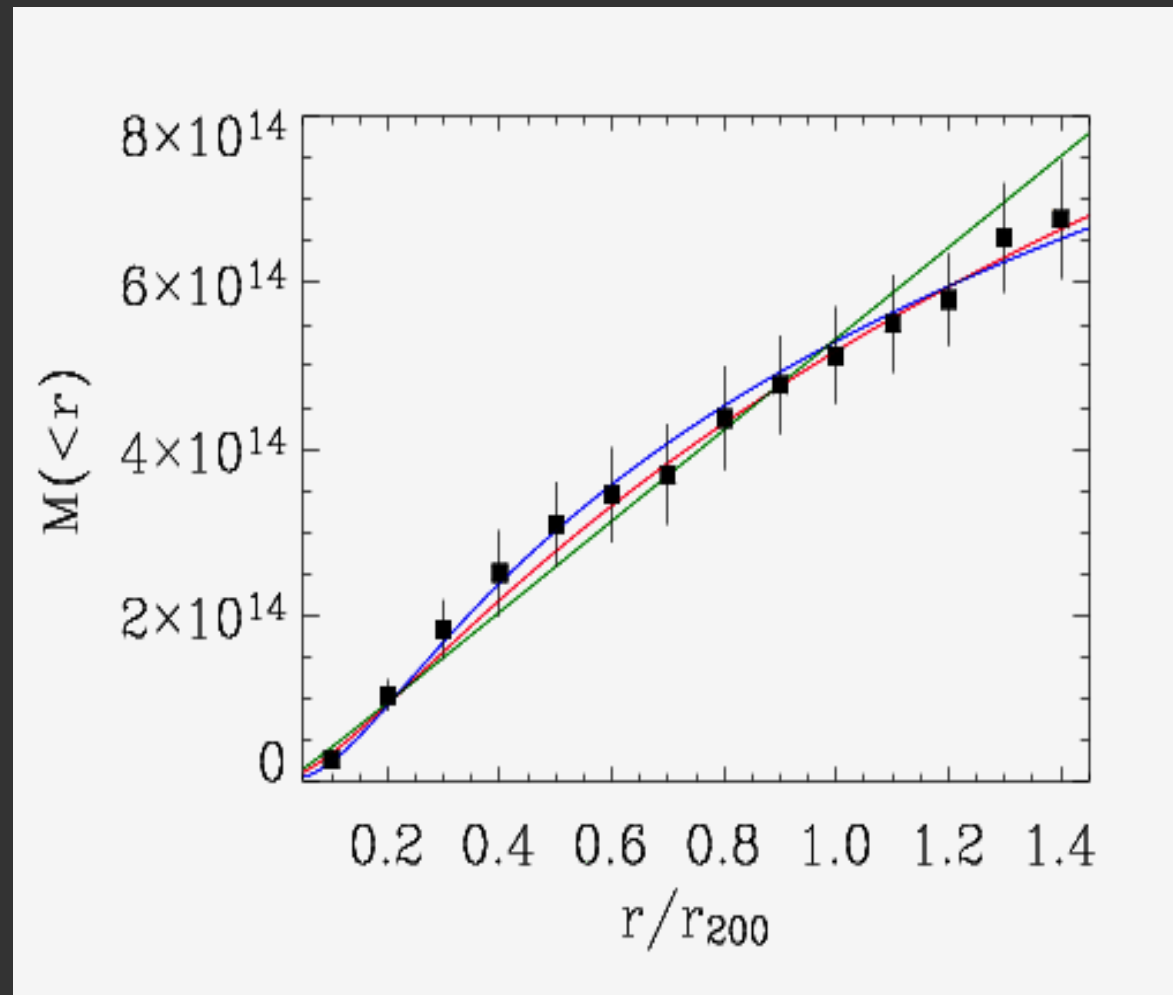
$$\rho(r) \propto r^{-2.4 \pm 0.4} \text{ at } r=r_{200}$$

Fitting models:

NFW  $c=4 \pm 2$ ,

Burkert 95  $r_{\text{core}}=0.15 r_{200}$

Isothermal gives poor fit



# M(<r) results: Groups

*(Mahdavi et al. 99, 04; Carlberg et al. 01)*

Conflicting results so far!

Hernquist profile?  $\rho(r) \sim r^{-2}$  at all radii? inner core +  $\rho(r) \sim r^{-1.75}$ ?

Result depends on groups sample, not all groups  
are dynamically virialized structures

*(Giuricin et al. 88, Diaferio et al. 93,  
Mamon 95, Mahdavi et al. 99)*

# M(<r) results: GEMS groups

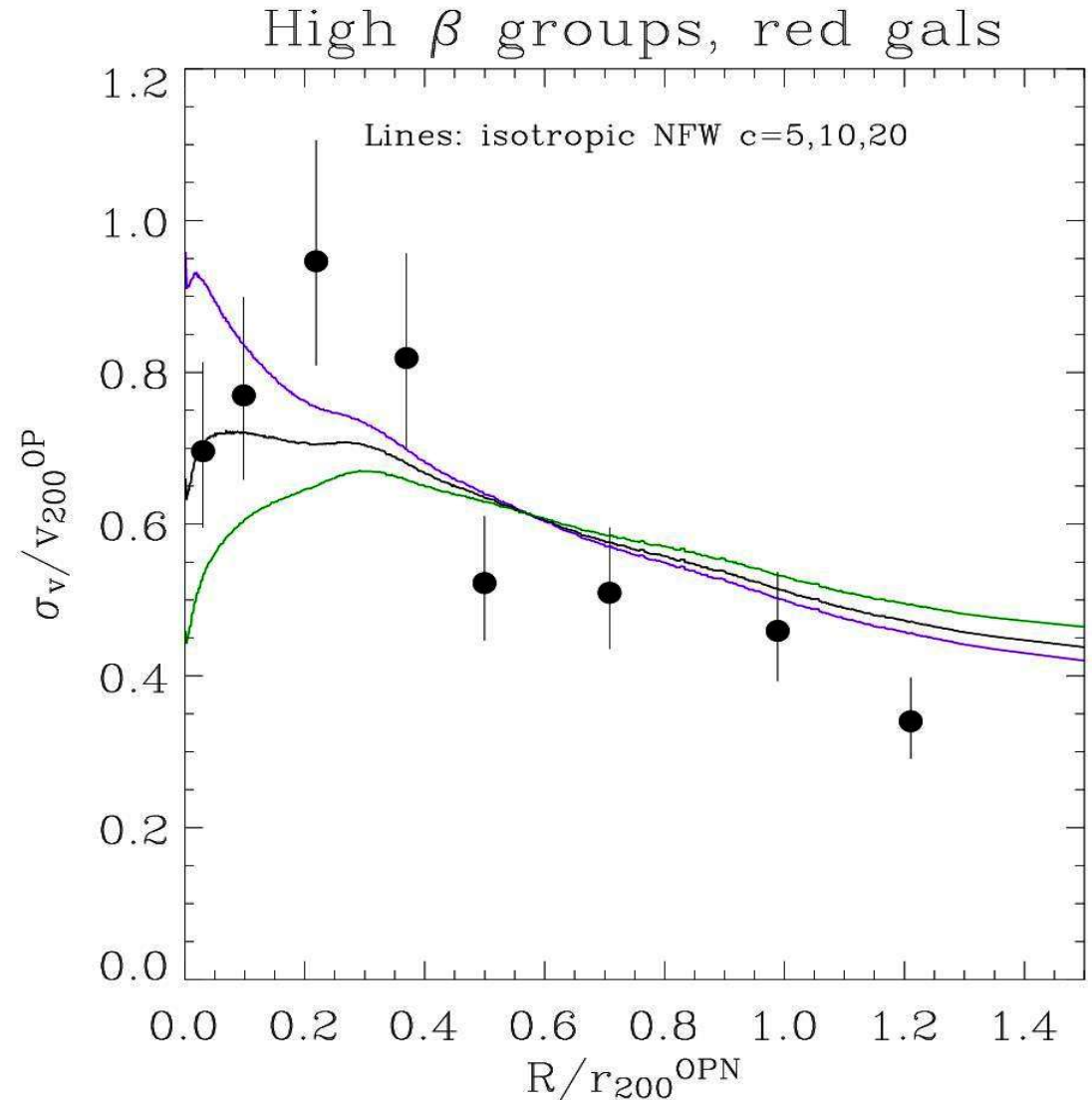
(B., Mamon, Ponman, et al. in preparation)

Two classes of groups?

(see also *Mahdavi et al. 99*)

high- $\beta_{\text{spec}}$  : virialized!

low- $\beta_{\text{spec}}$  :  
projection,  
collapsing,  
tidally affected,  
or ...  
dynamically  
evolved?



# M(<r) results: evolution

**CNOC:** (*Carlberg et al. 97, van der Marel et al. 00*)

16 clusters at  $z=0.17-0.55$

Best fit  $\rho(r) \sim r^{-\xi}$  :      for  $r \sim 0$ :       $0.7 \leq \xi \leq 1.2$ ,

for  $r$  large:       $3 \leq \xi \leq 4$

Best-fit NFW:  $c=4-5$

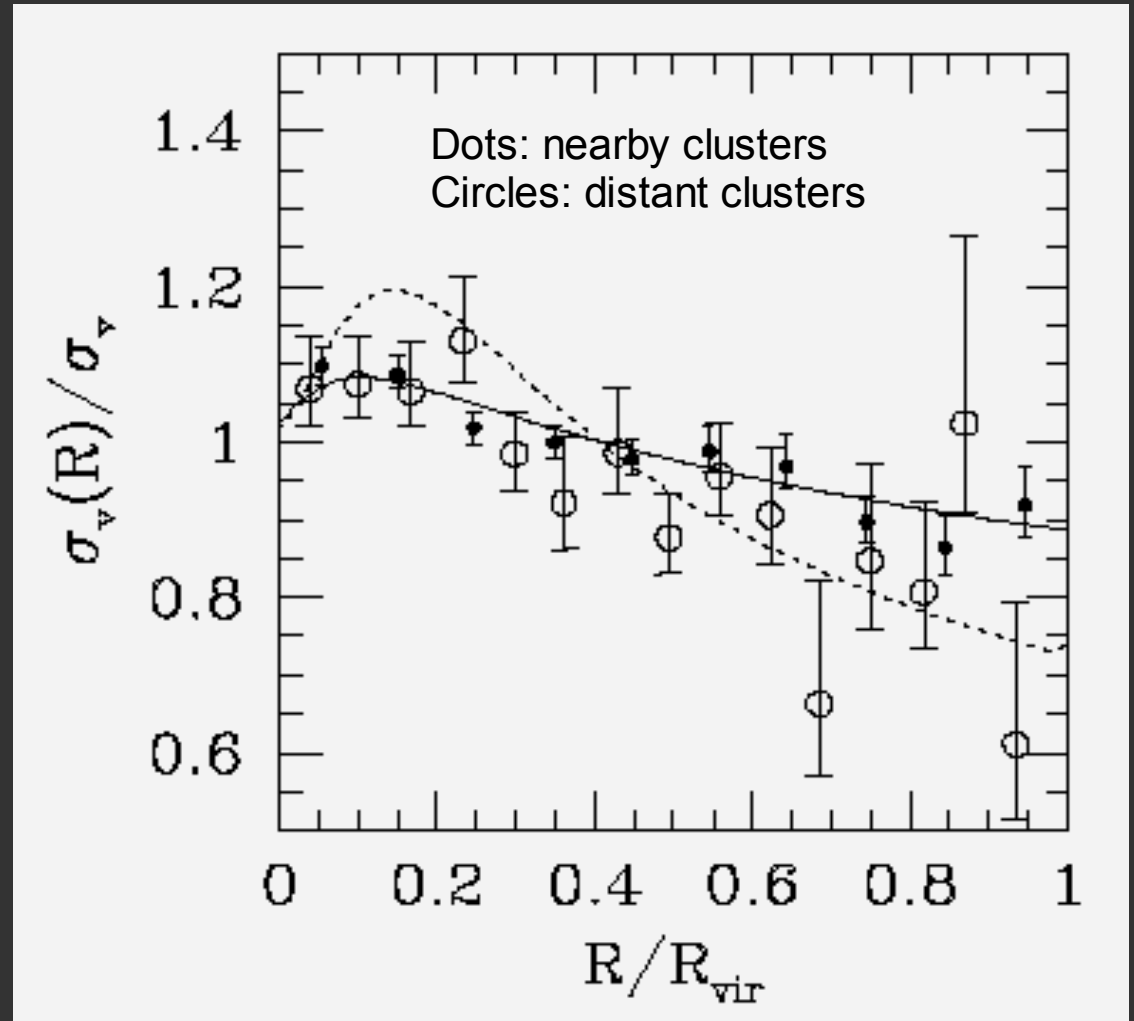
Mass profile is similar to that found in nearby clusters

# M(<r) results: evolution

(*Girardi & Mezzetti 2001; also: Adami et al. 2001*)

No evolution  
in observed  
projected galaxy  
number density  
& l.o.s. velocity  
dispersion  
profiles out  
to  $z \simeq 0.4$

⇒ No evolution in M(<r)



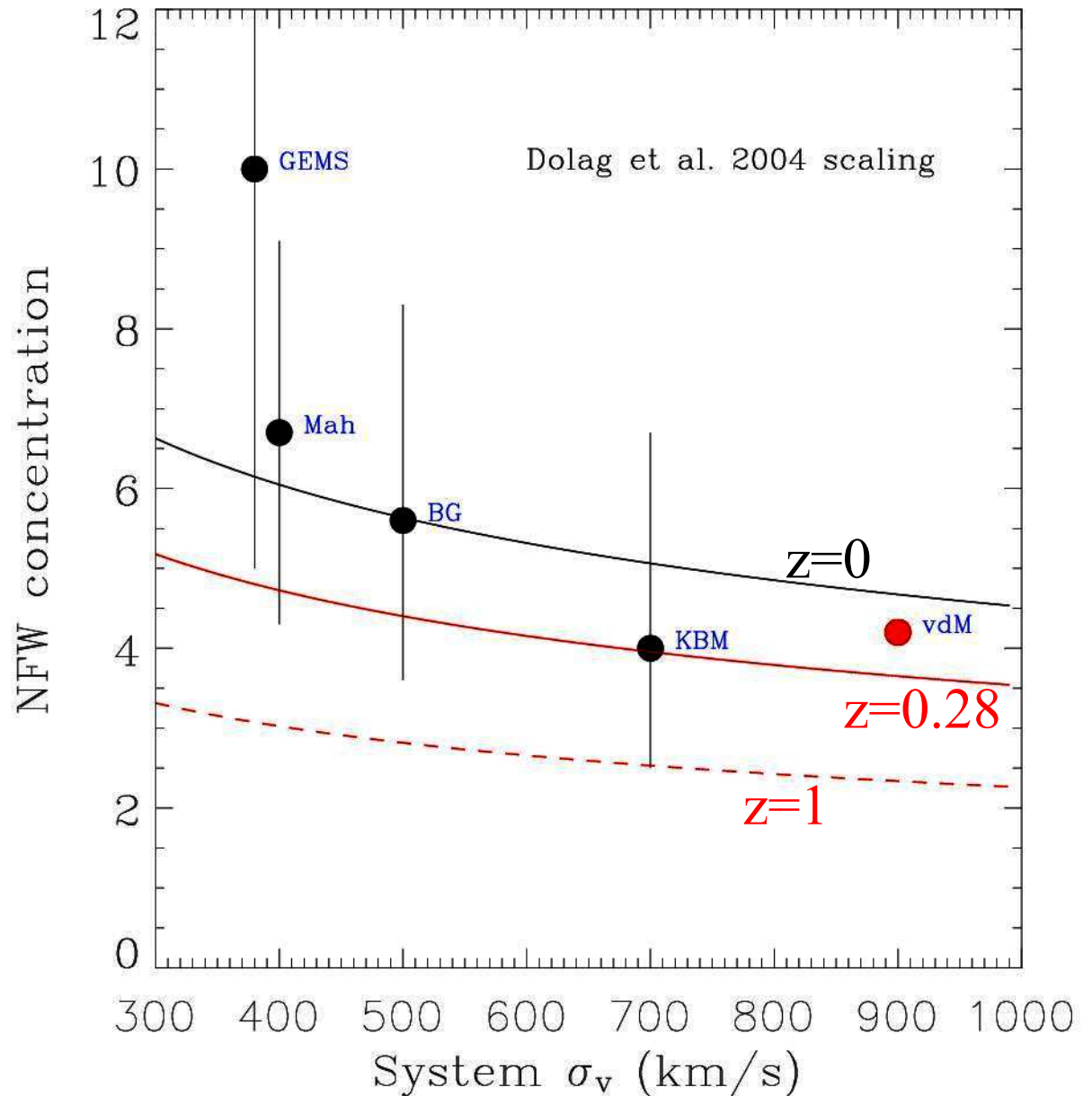
*More galaxies on radial orbits (infalling)?*



# M(<r) results: concentration vs. mass

(from:  
Mahdavi et al. 99,  
B. et al. in prep.,  
Katgert et al. 04,  
B. & Girardi 03,  
van der Marel et al. 00)

Can we hope to  
detect evolution  
of  $c=c(M)$  with  $z$ ?



# M(<r) results summary:

Mass density profile of galaxy clusters  $\rho(r) \propto r^{-\xi}$  :

poor constraints near  $r=0$  :  $0 \leq \xi \leq 2$

better constraints at large  $r$ :  $3 \leq \xi \leq 4$

→ NFW and Hernquist OK, isothermal ruled out

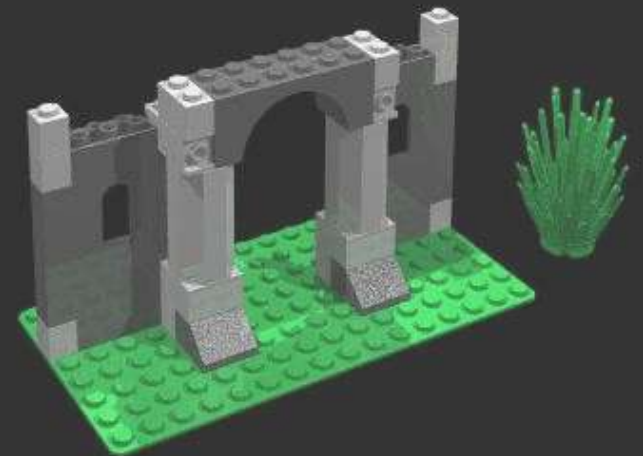
If NFW,  $c=c(M)$  has correct trend

If  $\xi=0$  near  $r=0$ , core radius is small,  $r(\rho=\rho_{0/2}) < 0.1 r_{200}$

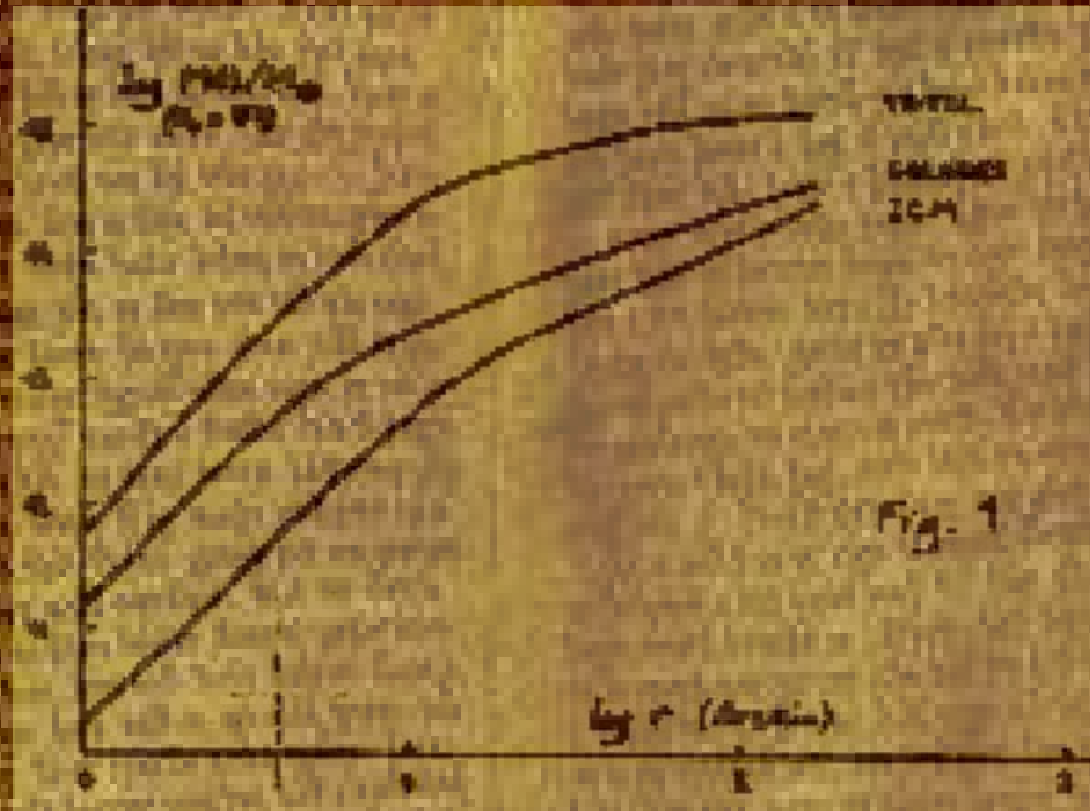
## *Progress:*

- ◆ mass profile of galaxy groups
- ◆ mass profile evolution, check that  $c(M) \downarrow$  with  $z$

# Mass-to-light profile



# Historical



Relative distribution of total mass, mass in galaxies and ICM mass in Coma, from Gerbal et al. (1984)

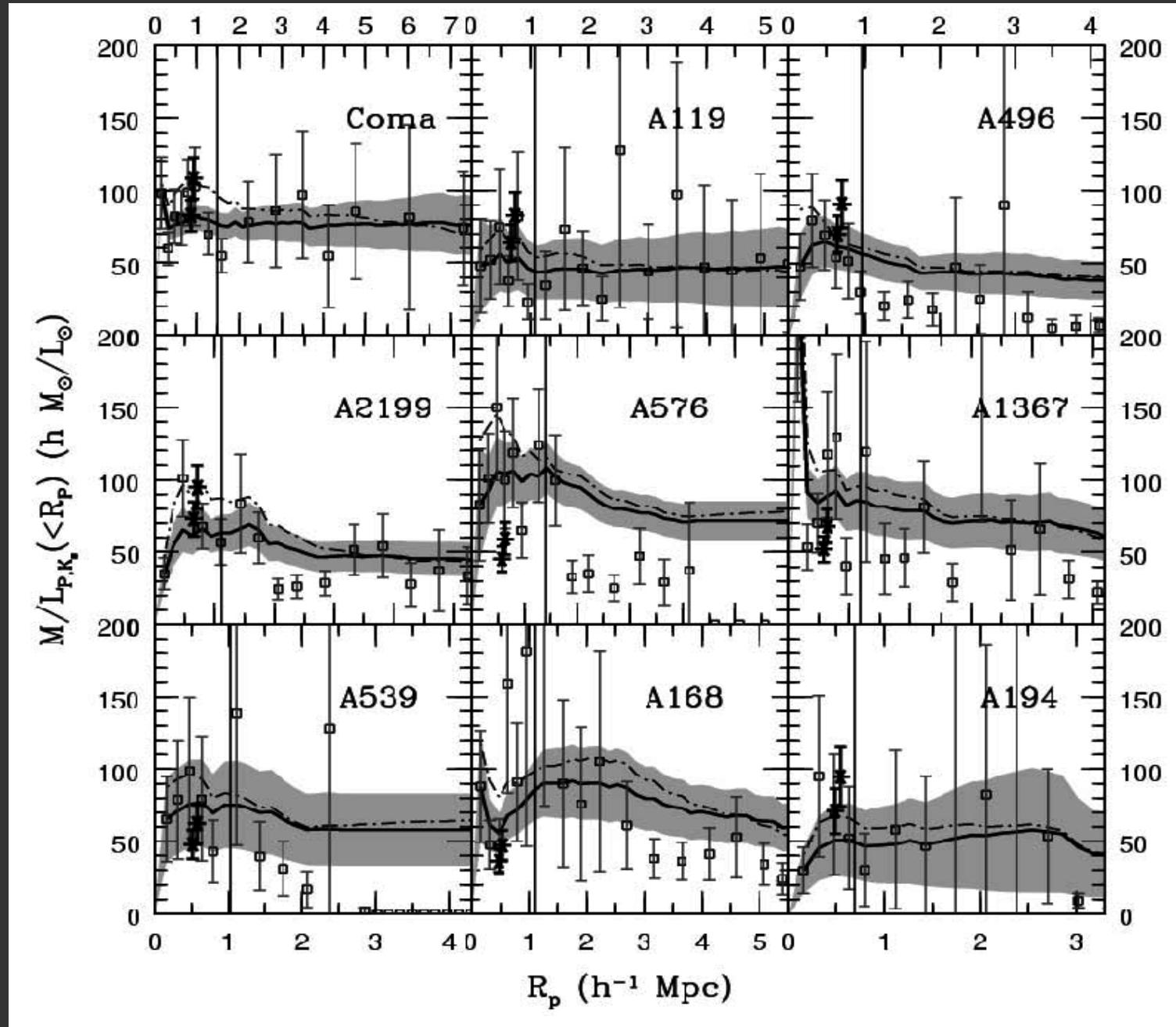
# Scientific motivations

- How do baryons settle in cluster potential?
- Is the galaxy distribution biased relative to dark matter?
- Relative importance of physical mechanisms:  
*dynamical friction, tidal stripping, merging...*

# M/L results: CAIRNS

*(Rines et al. 04)*

Flat M/L  
within  $r_{200}$ ,  
some excess  
of luminosity  
near the centre,  
mild decrease  
outwards,  
but  $\neq$  clusters  
have  $\neq$  trends,  
probably caused  
by projection  
effects

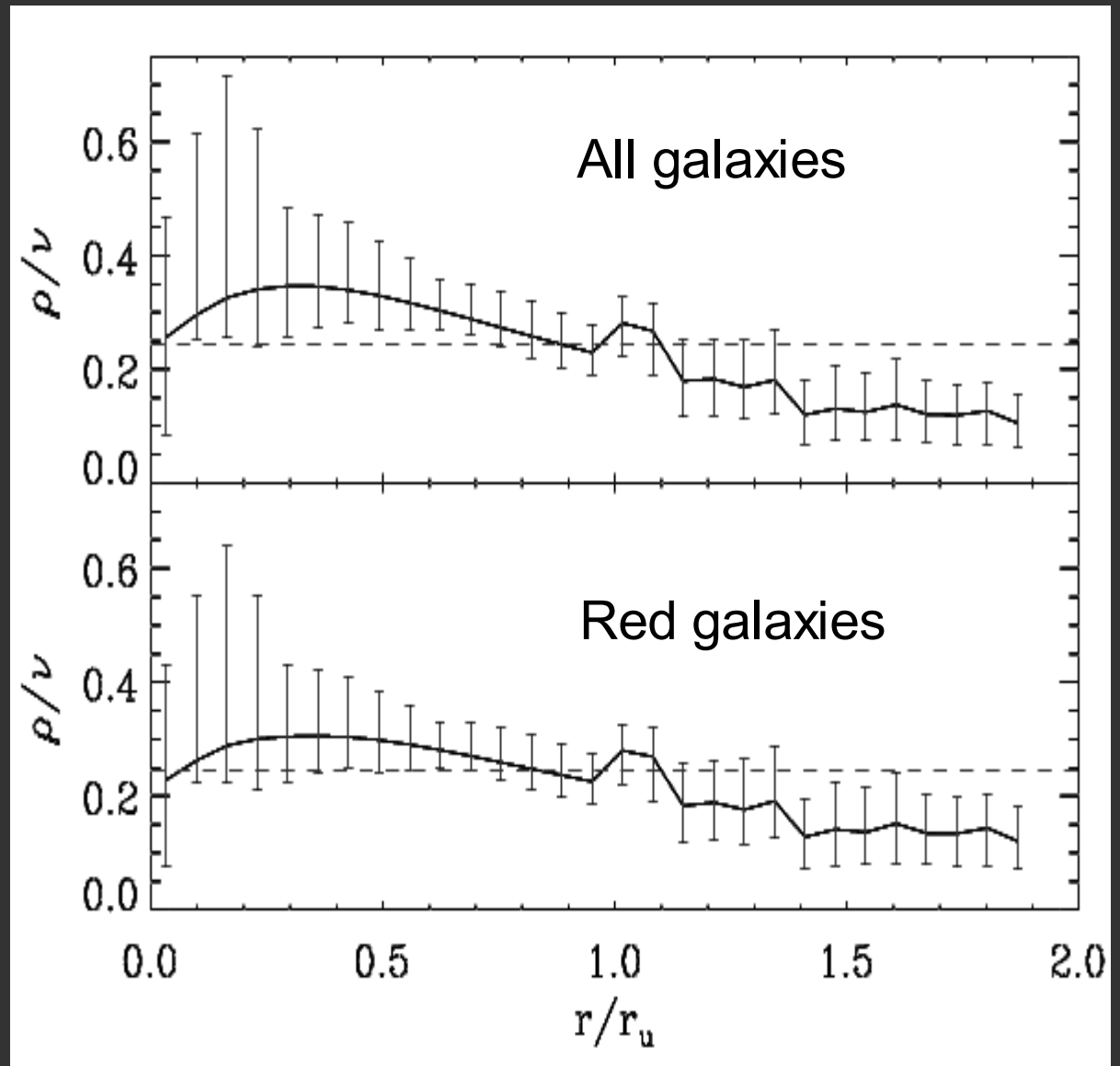


# M/L results: 2dFGRS

Averaging over several clusters allows to beat projection effects

Some central light excess and a slight decrease beyond  $0.3 r_{200}$ , mostly due to late-type galaxies

(B. & Girardi 03)

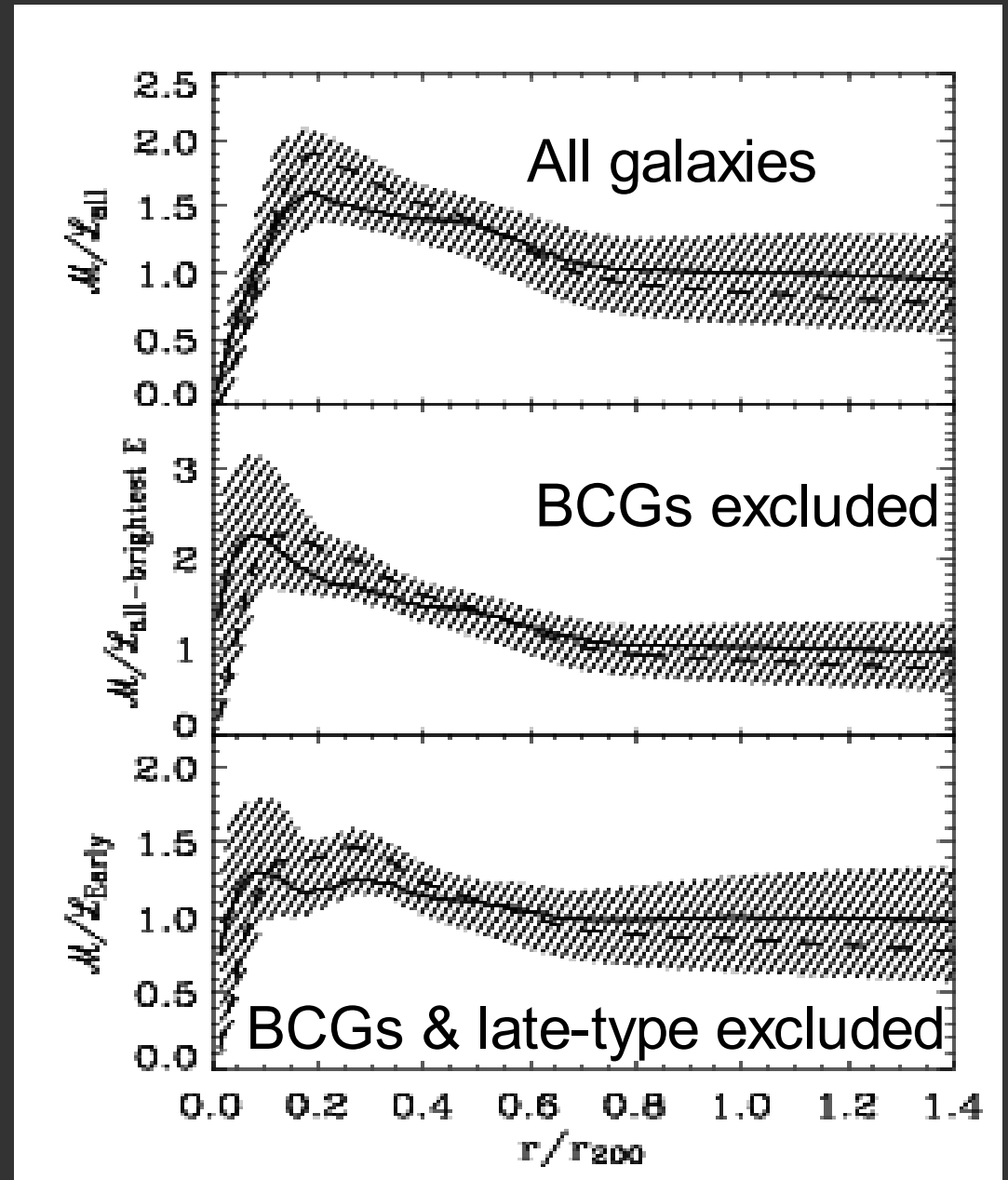


# M/L results: ENACS

Averaging over several clusters allows to beat projection effects

Some central light excess mostly due to BCGs, and a slight decrease beyond  $0.3 r_{200}$ , mostly due to late-type galaxies

(Katgert, B. & Mazure 04)





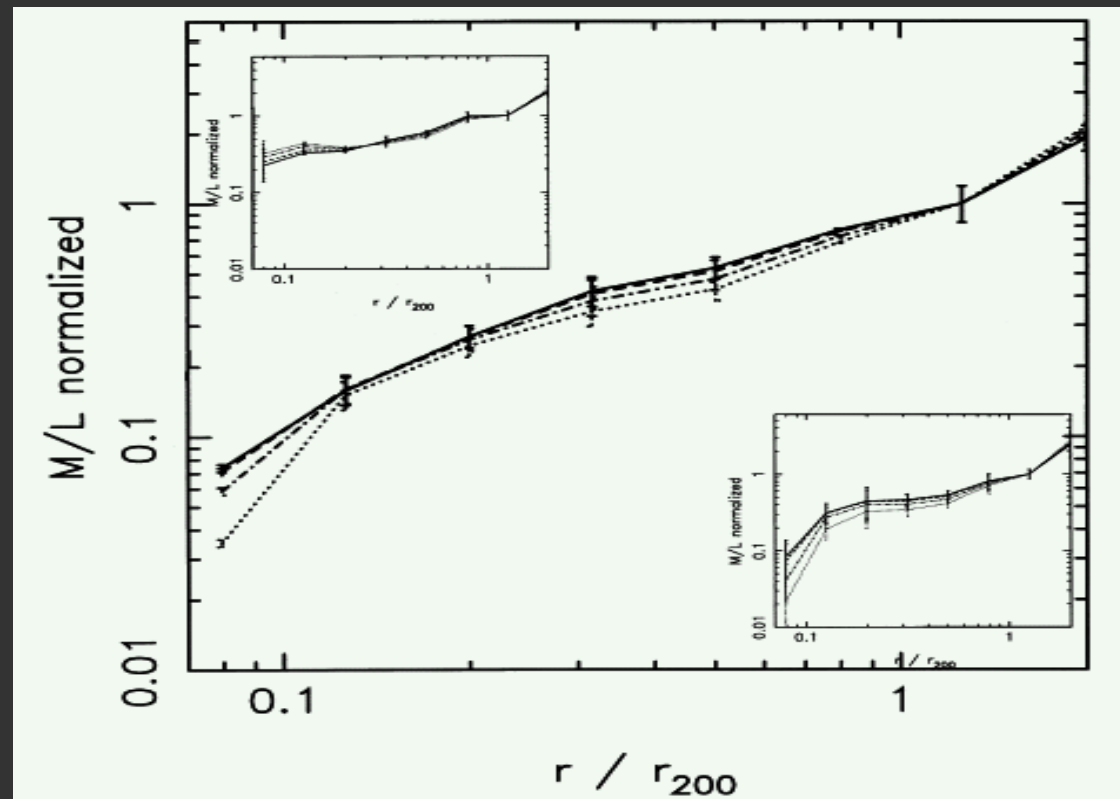
# M/L results: Groups

Conflicting results so far!

Constant M/L?  
(Mahdavi et al. 99)

↓  
...but only for 1/4  
of all groups,  
those with  
declining  
velocity dispersion  
profile!

... or steeply rising M/L?  
(Carlberg et al. 01)

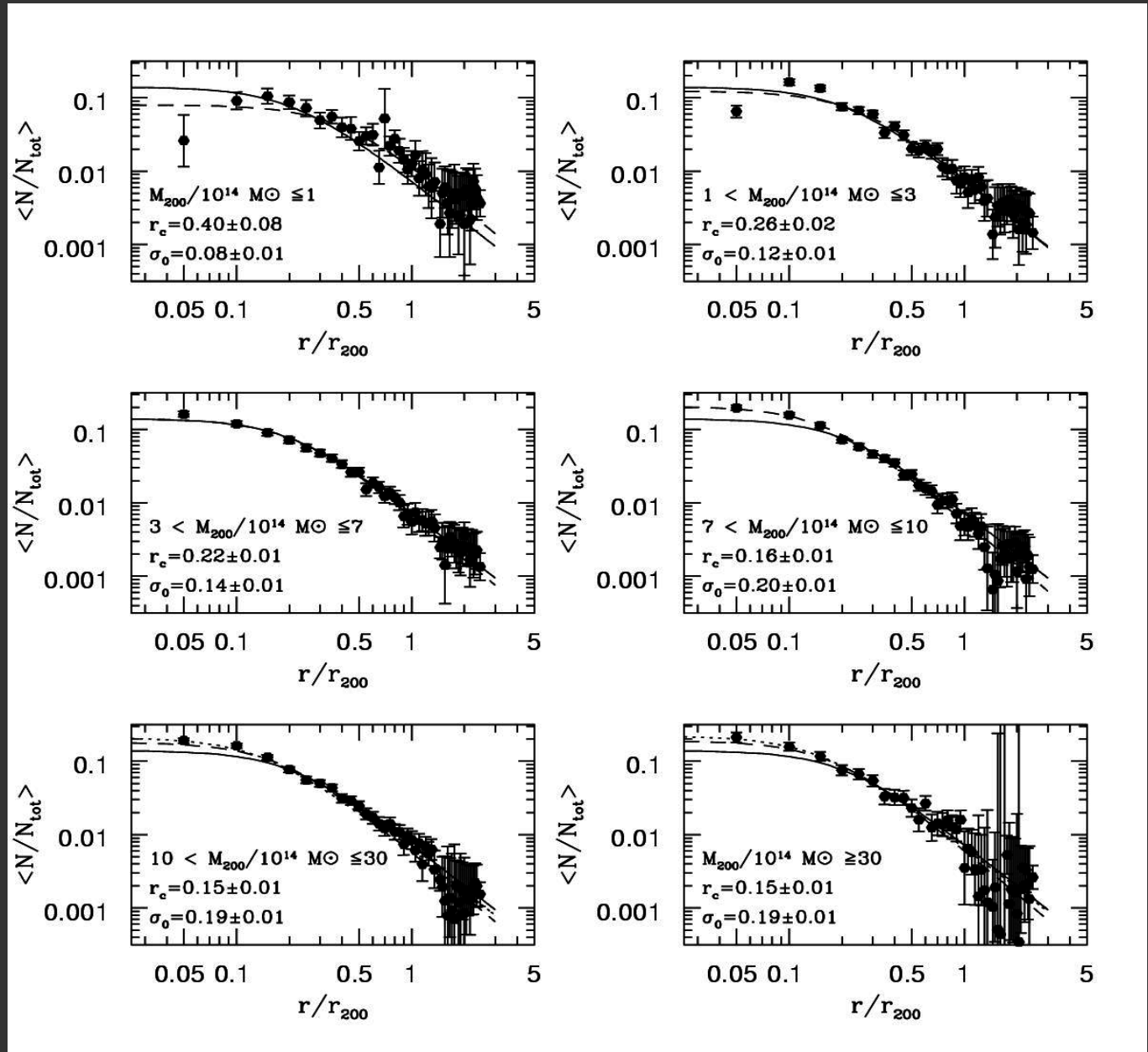


# M/L results: groups vs. clusters

Galaxies in groups have less peaked number density profiles than galaxies in clusters

*(Popesso et al. in prep.)*

→ M/L at  $r \rightarrow 0$  is larger in groups than in clusters

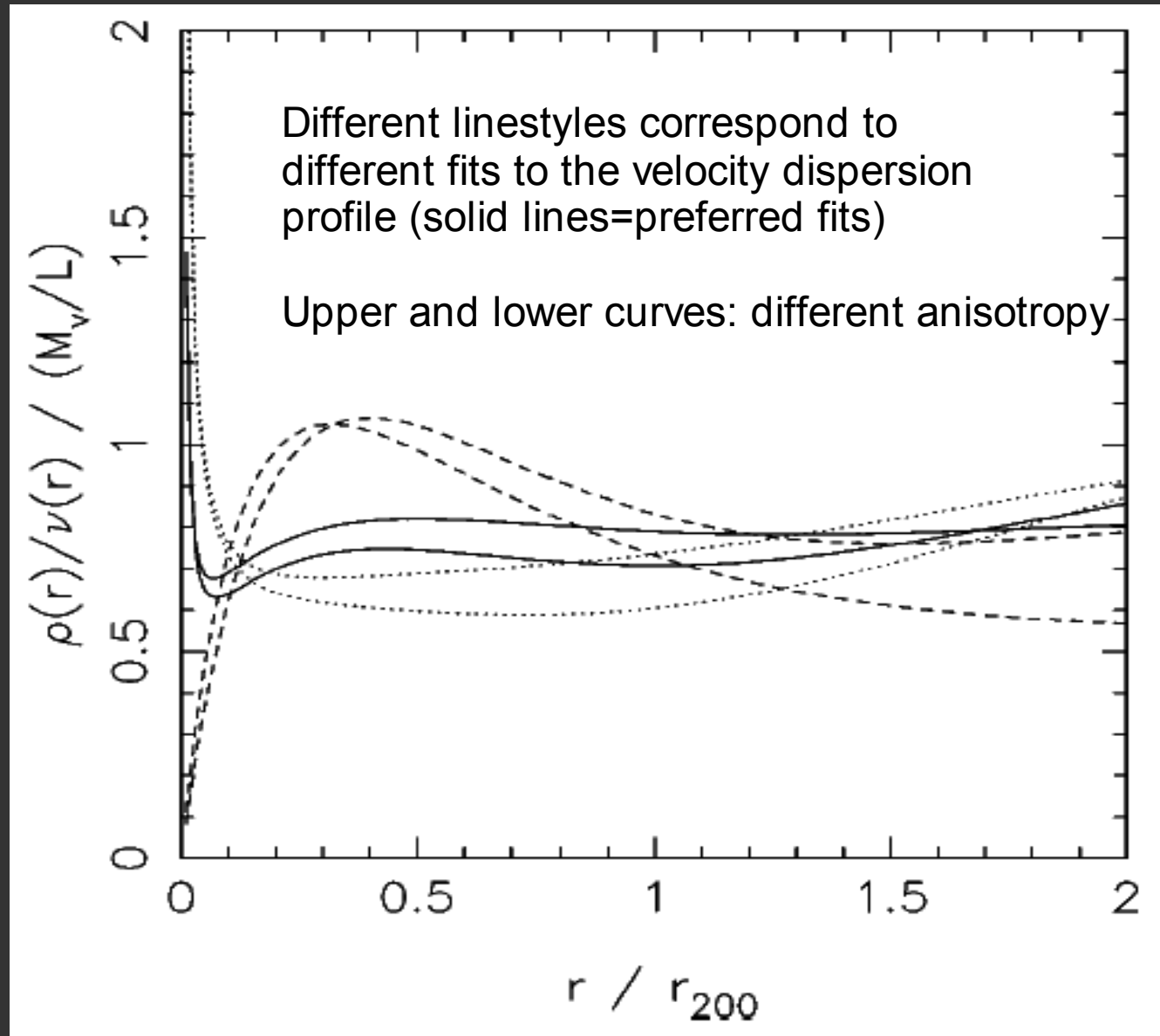


# M/L results: evolution

## CNOC

Flat M/L for  
 $\langle z \rangle = 0.3$  clusters?  
Less evidence  
for central  
luminosity  
excess

(Carlberg et al. 97)



# M/L results summary:

$z \simeq 0$

Evidence for excess light near the centre  
Mild M/L decreasing trend with radius (factor 2 at  $2 r_{200}$ )  
Early-type galaxies fair tracers of mass within  $r_{200}$

$z \simeq 0.4$

No central light excess (?)  
(central assembly of very bright galaxies still ongoing?)  
No decreasing M/L with radius (?)  
(more field galaxies yet to be captured?)

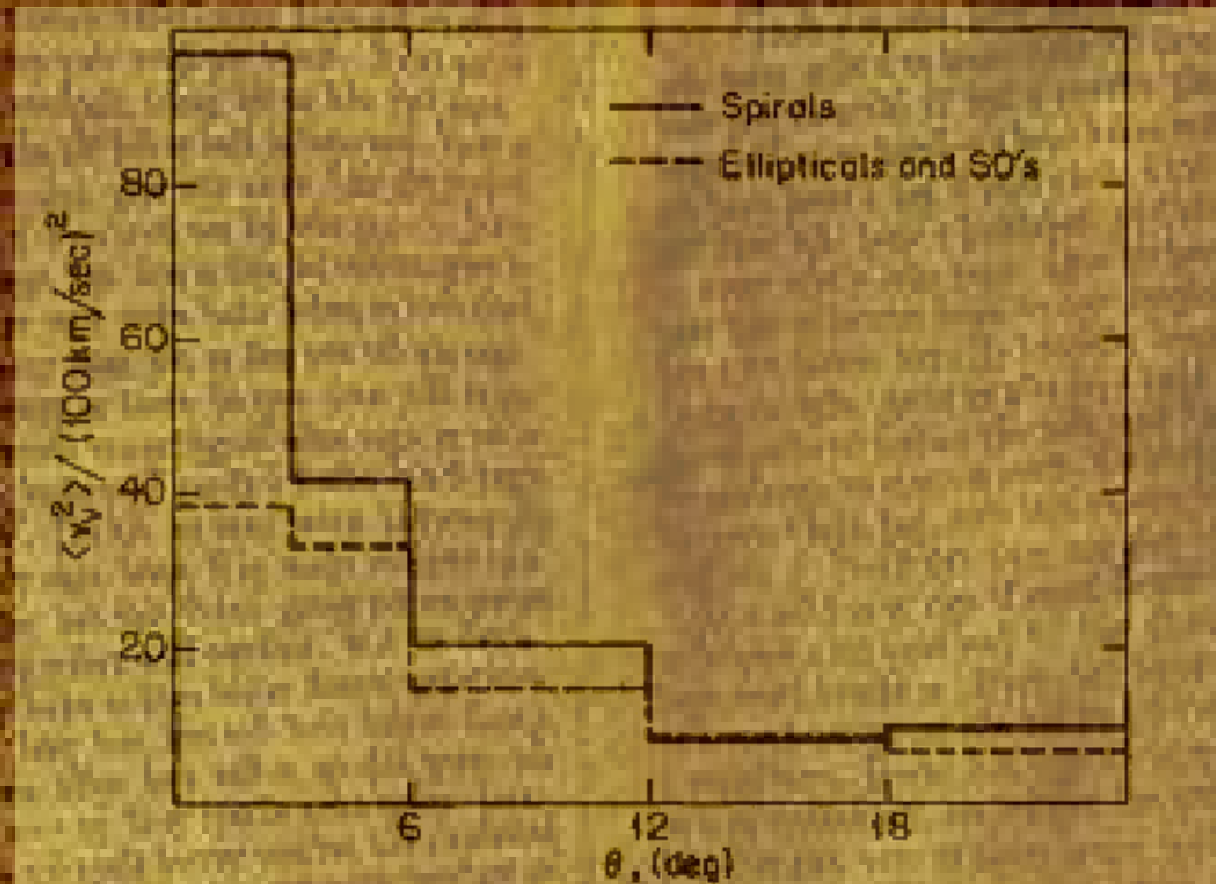
## *Progress:*

- ◆ mass-to-light profile of galaxy groups
- ◆ mass-to-light profile evolution with  $z$

# Orbital structure



# Historical

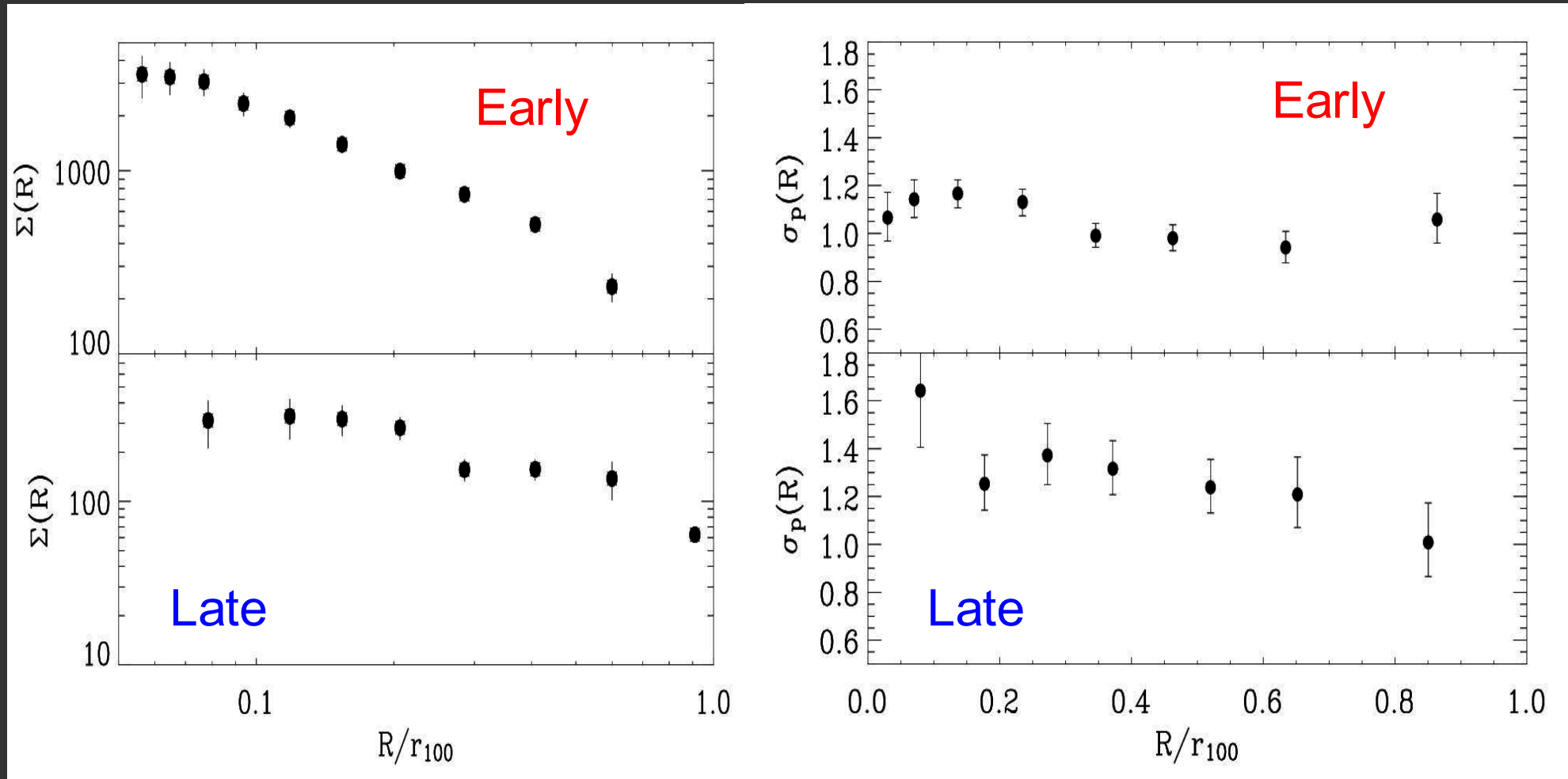


Velocity dispersion profiles of early- and late-type galaxies in Virgo from Hoffman et al. (1980)

# Scientific motivations

- **Test hierarchical accretion models**  
*accretion rate of field galaxies vs. redshift*
- **Test cluster galaxy evolution models**  
*orbits of cluster galaxies evolve as a result of  
e.g. selective tidal destruction of galaxies on  
radial orbits (e.g. Faltenbacher et al. 05)*

# Orbits results: ENACS *(B. & Katgert 04)*

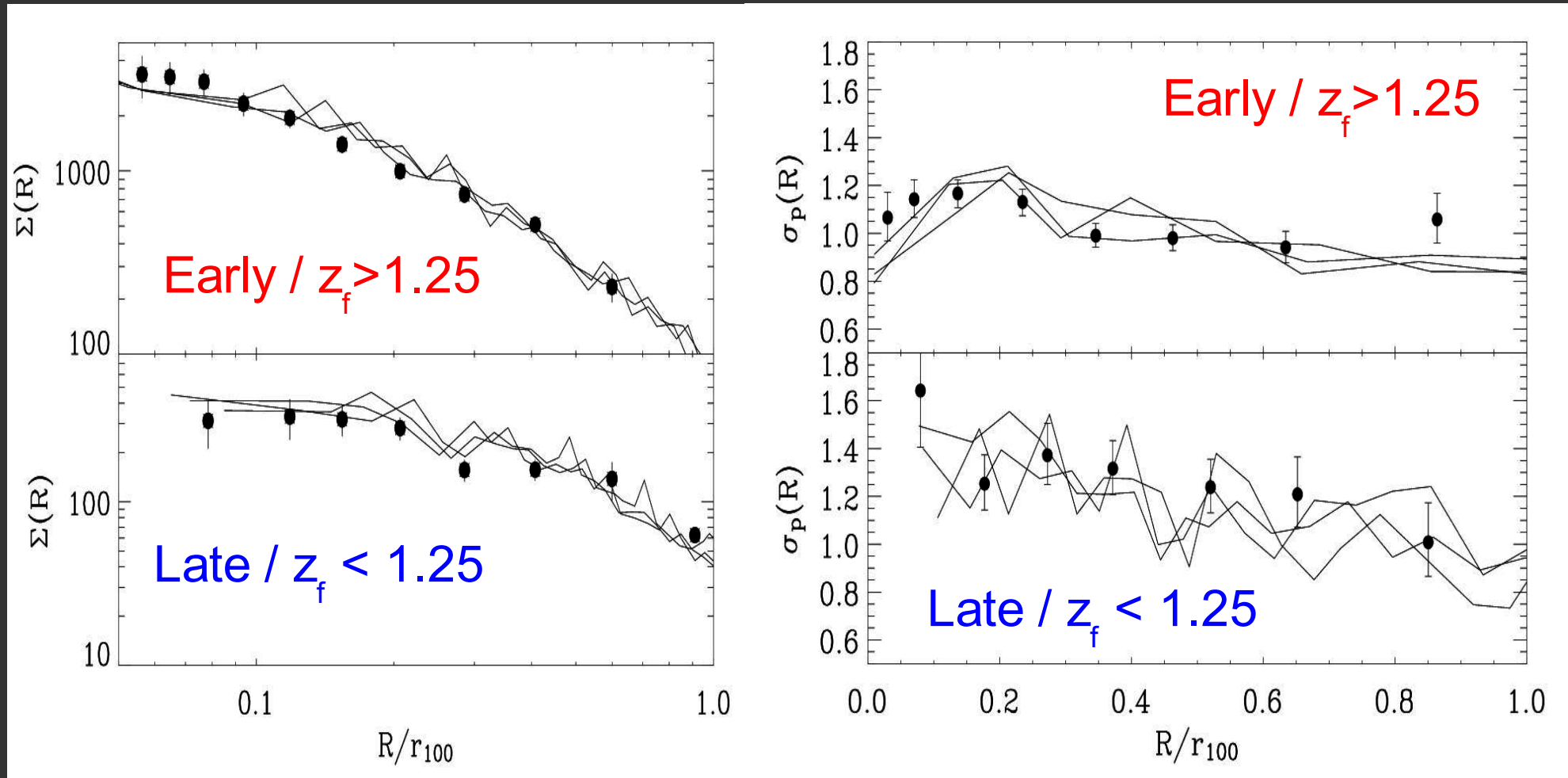


Early- and late-type cluster galaxies have  $\neq$  number density profiles  
and  $\neq$  velocity dispersion profiles

→ do they move with different orbits in the cluster potential?



# Orbits results: ENACS vs. SIMULATIONS

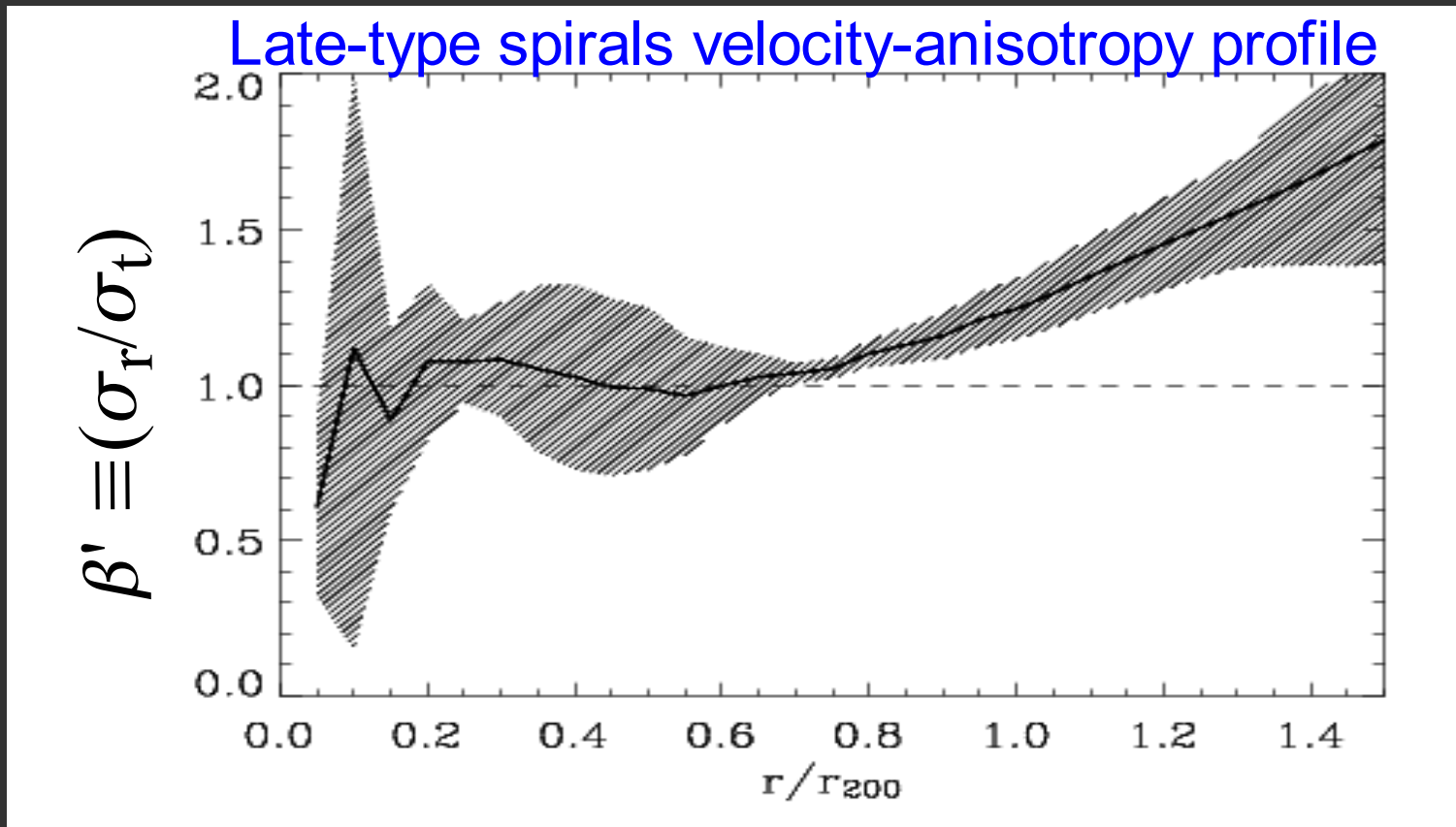


Numerical simulations can reproduce the early- and late-type cluster galaxies number density profiles and velocity dispersion profiles (B., Murante, Borgani, Dolag et al. in prep.)

→ allows better understanding of cluster galaxies evolution

# Orbits results: ENACS *(B. & Katgert 04)*

Early-type galaxies have nearly isotropic orbits,  
 $0.8 \leq \beta' \leq 1.05$  from the analysis of the velocity distribution

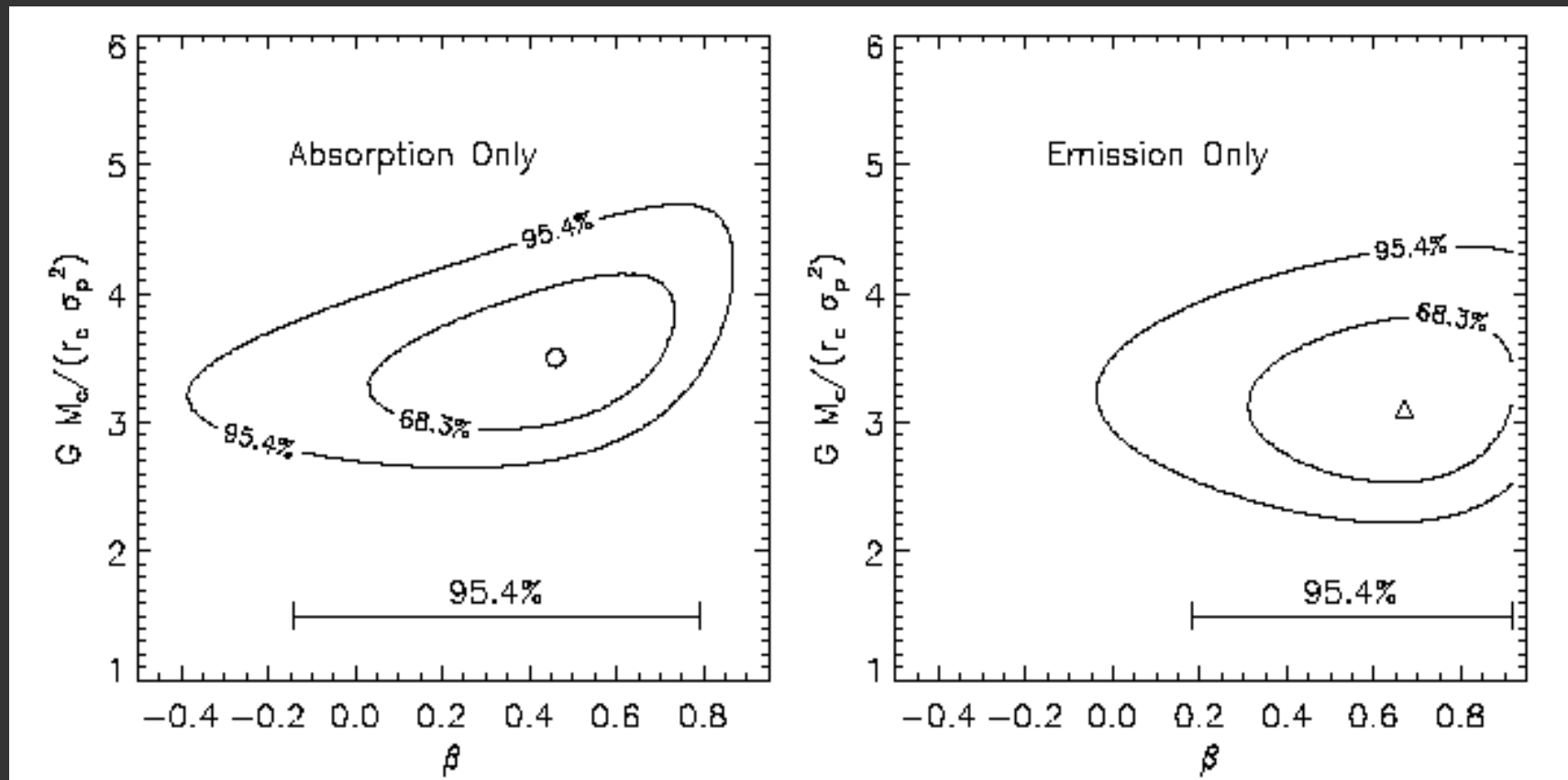


Late-type spirals are on increasingly radial orbits with radius  
while early-type spirals have nearly isotropic orbits,  
based on the Jeans-equation inversion

# Orbits results: groups *(Mahdavi et al. 99)*

Early-type galaxies have nearly isotropic orbits,  
late-type galaxies have moderate radial velocity anisotropy  
(constant anisotropy assumed)

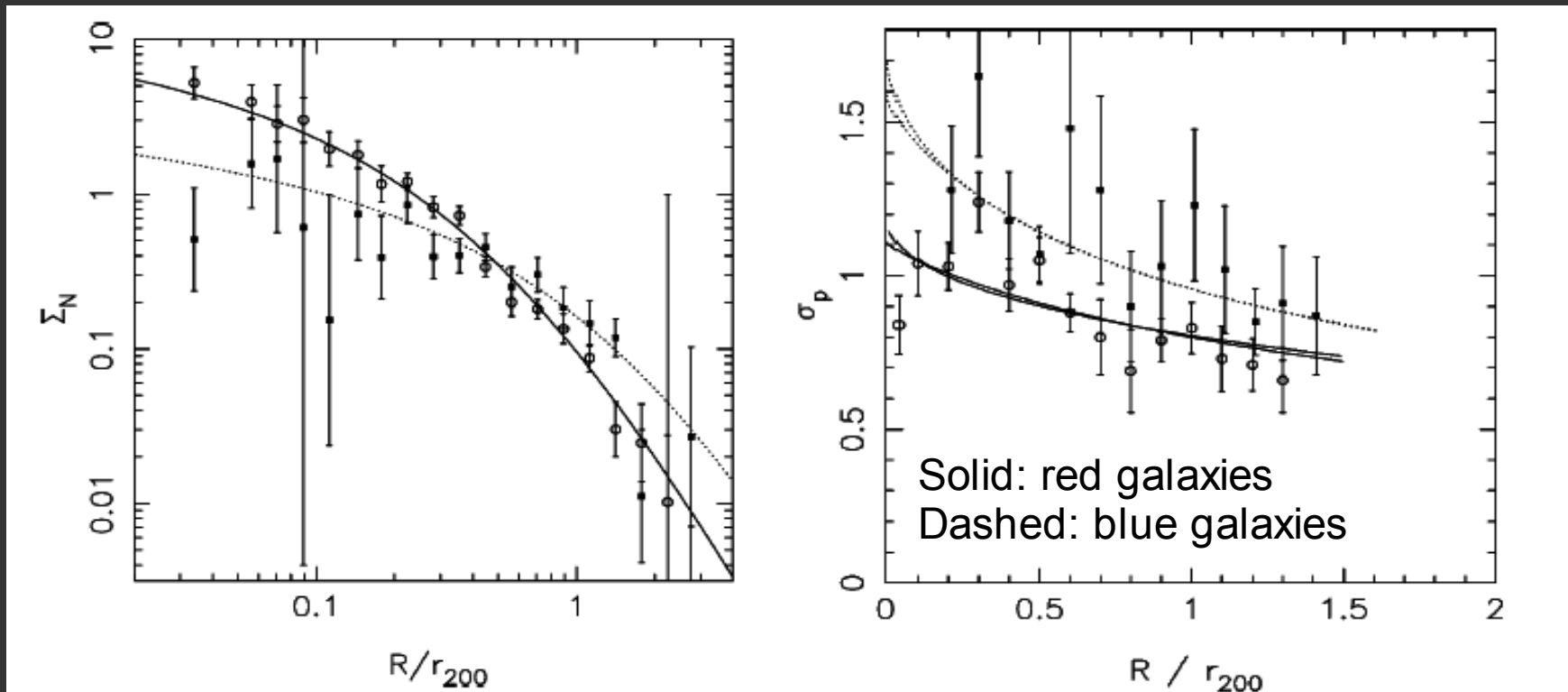
Mass



$$\beta \equiv 1 - (\sigma_t / \sigma_r)^2$$

# Orbits results: evolution; CNOC

(Carlberg et al. 97, van der Marel et al. 00)



Similar differences between red and blue galaxies distributions as seen in nearby clusters. Red galaxies shown to have  $0.74 \leq \beta' \leq 1.05$ , blue galaxies? Perhaps on more radial orbits

# Orbits results summary:

- ◆ Nearby clusters:

  - Early-type galaxies on isotropic orbits  
(probably also early-type *spirals*)

  - Late-type spirals (and Irr) on radial orbits,  $\beta(r) \uparrow$  with  $r$

- ◆ Similar results for nearby (virialized) groups

- ◆ Similar results for medium- $z$  clusters

  - Higher fraction of late-type galaxies

  - more radial anisotropy of the overall cluster population (?)

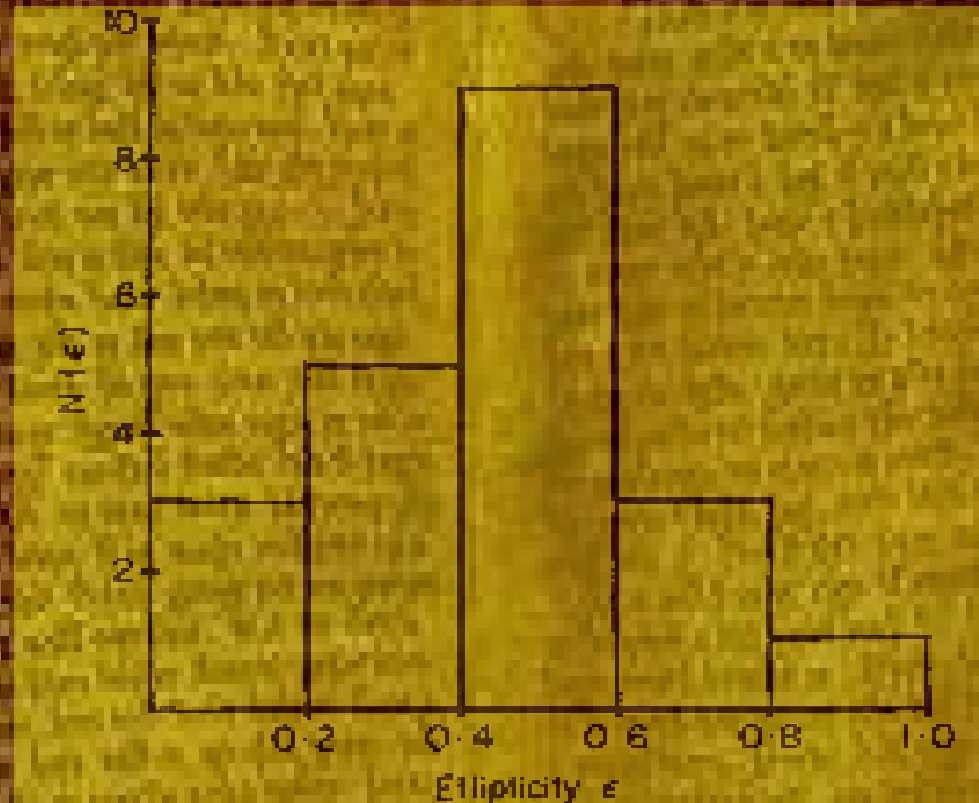
*Progress: orbital structure as a  $f=f(z)$*

*(constrain galaxy infall from the field  
and relation with BO effect, see Ellingson et al. 01)*

# Shape



# Historical



The distribution of galaxy clusters ellipticities  
from Carter & Metcalfe (1980)

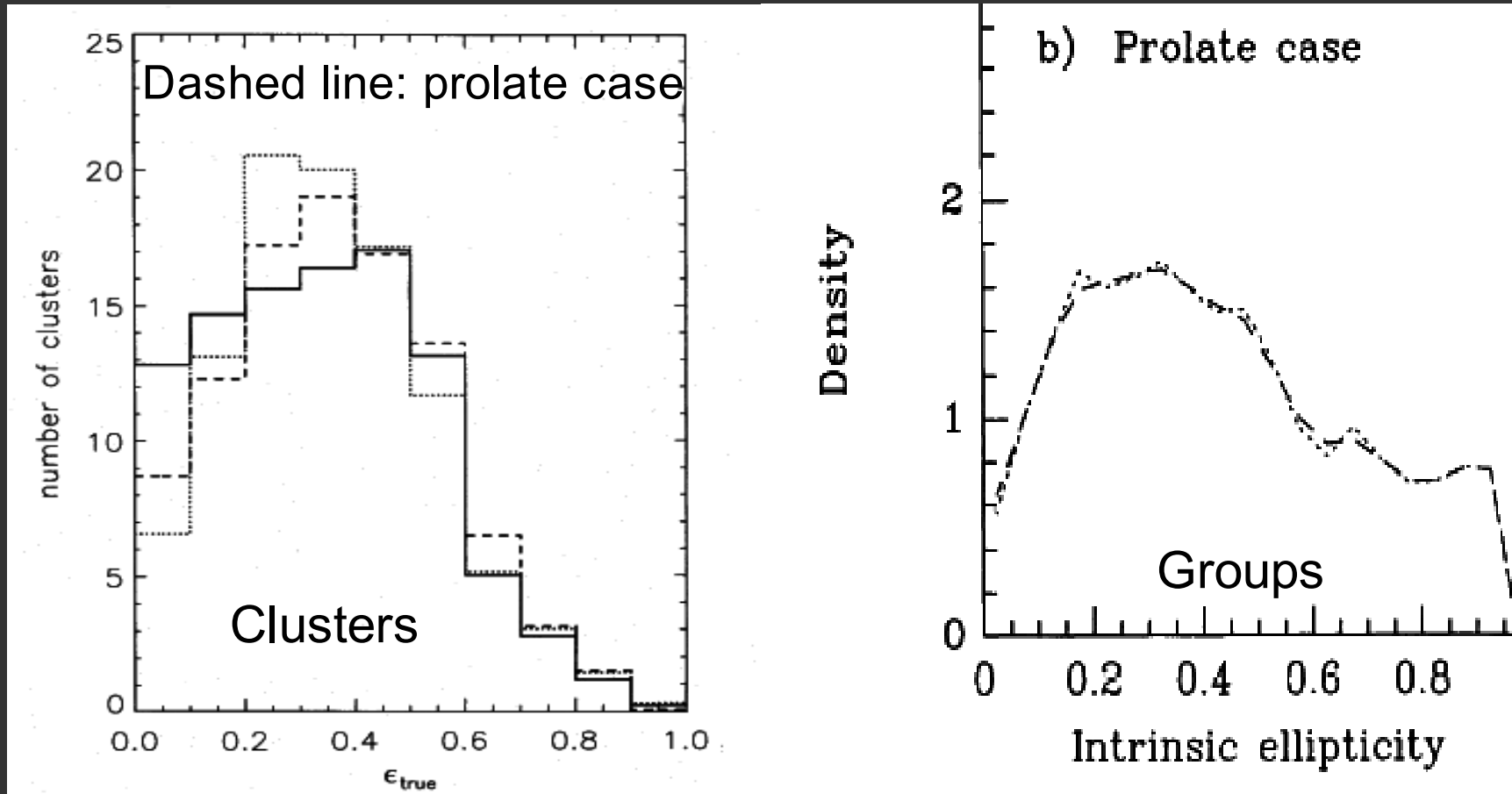
# Scientific motivations

- **Test hierarchical build-up models**  
*mechanisms of matter accretion from filaments*  
*Virialized haloes at given mass expected to evolve to more spherical shape as  $z \downarrow$  and evolution is faster for lower-mass haloes (e.g. Allgood et al. 05, Kasun & Evrard 05)*
- **Cluster mass estimates are affected by deviations from spherical shape**  
*(e.g. Piffaretti et al. 03, Gavazzi 05)*



# Shape results

Intrinsic ellipticity  $\epsilon \equiv 1 - (\text{minor axis}) / (\text{major axis})$

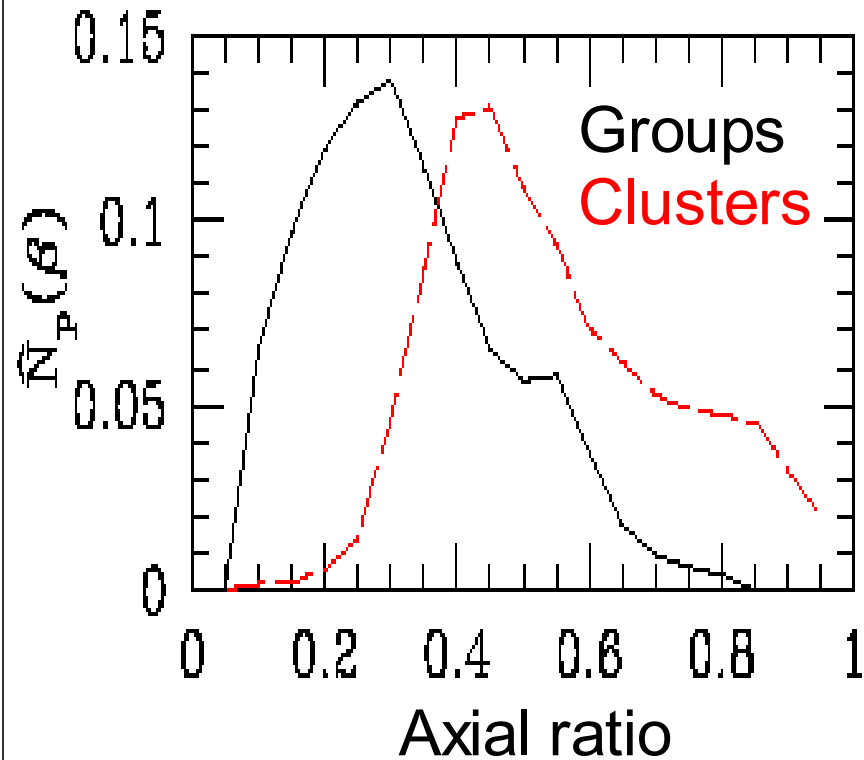
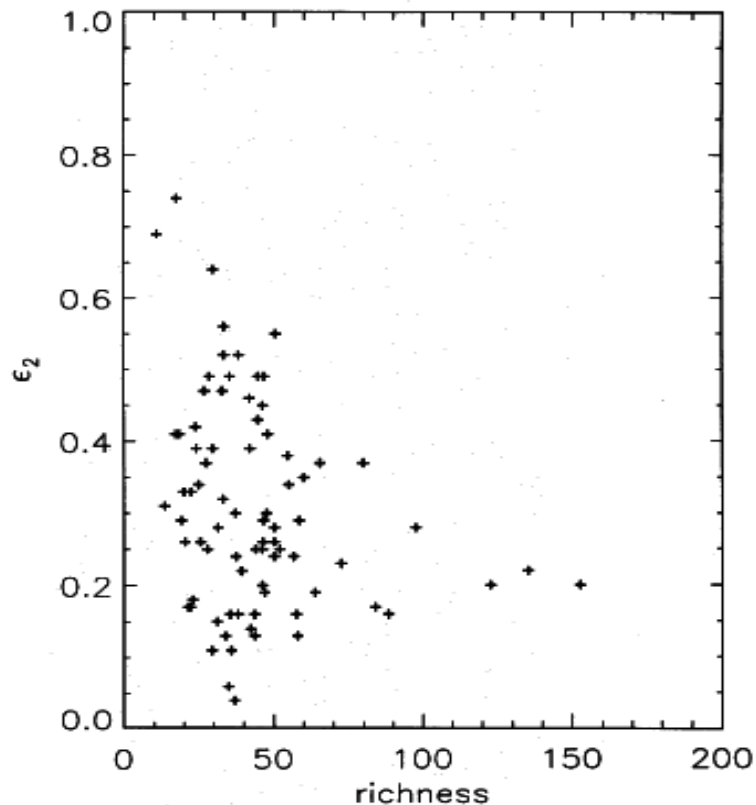


(de Theije et al. 95, Fasano et al. 93)

*Fraction of groups with  $\epsilon > 0.6$   
twice the corresponding cluster fraction*

# Shape results

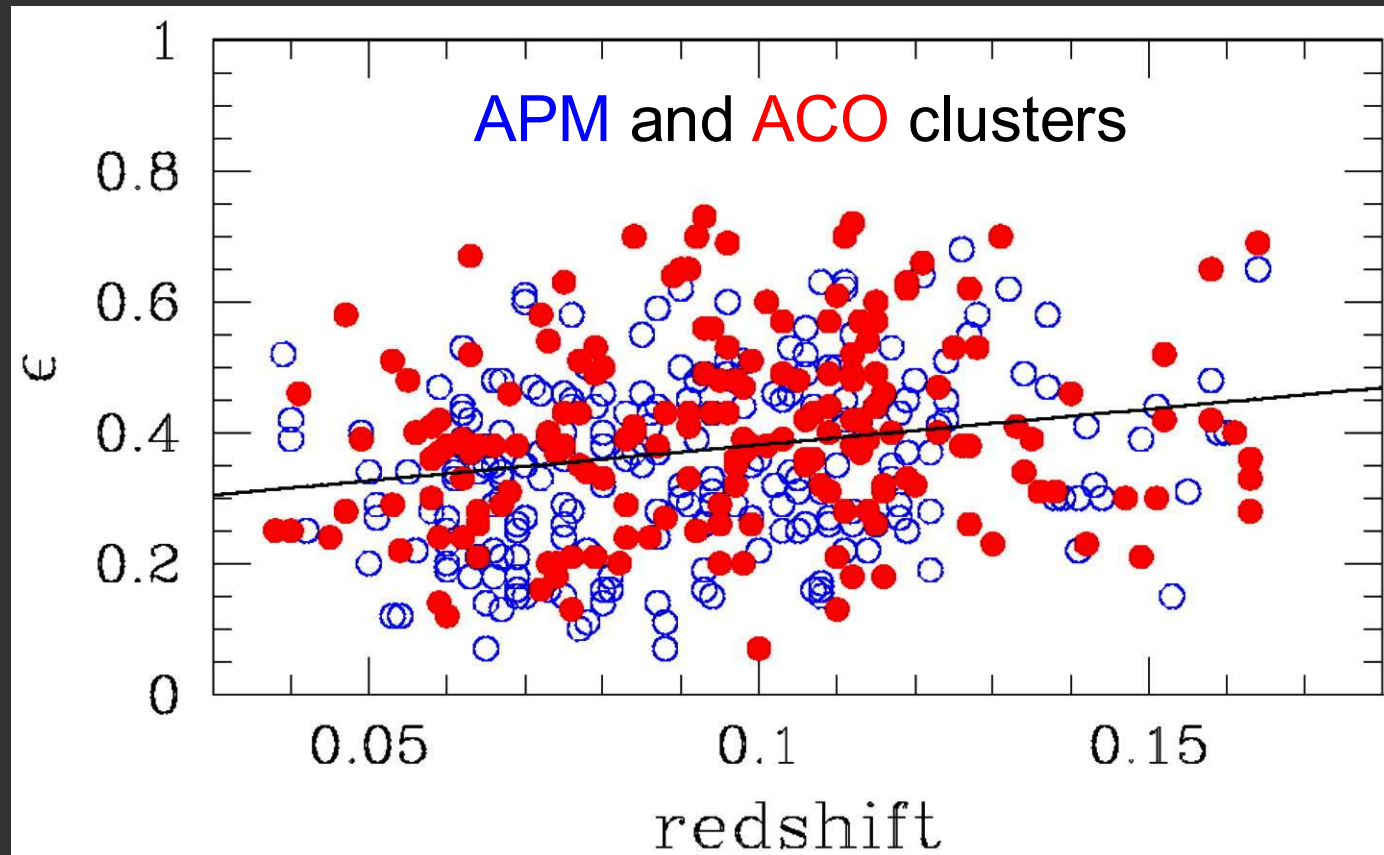
Ellipticity



*(de Theije et al. 95, Plionis et al. 04;  
consistent with Strazzullo et al. 05)*

Lower mass systems are less spherical,  
contrary to theoretical expectations  
*(but are we comparing apples and oranges?)*

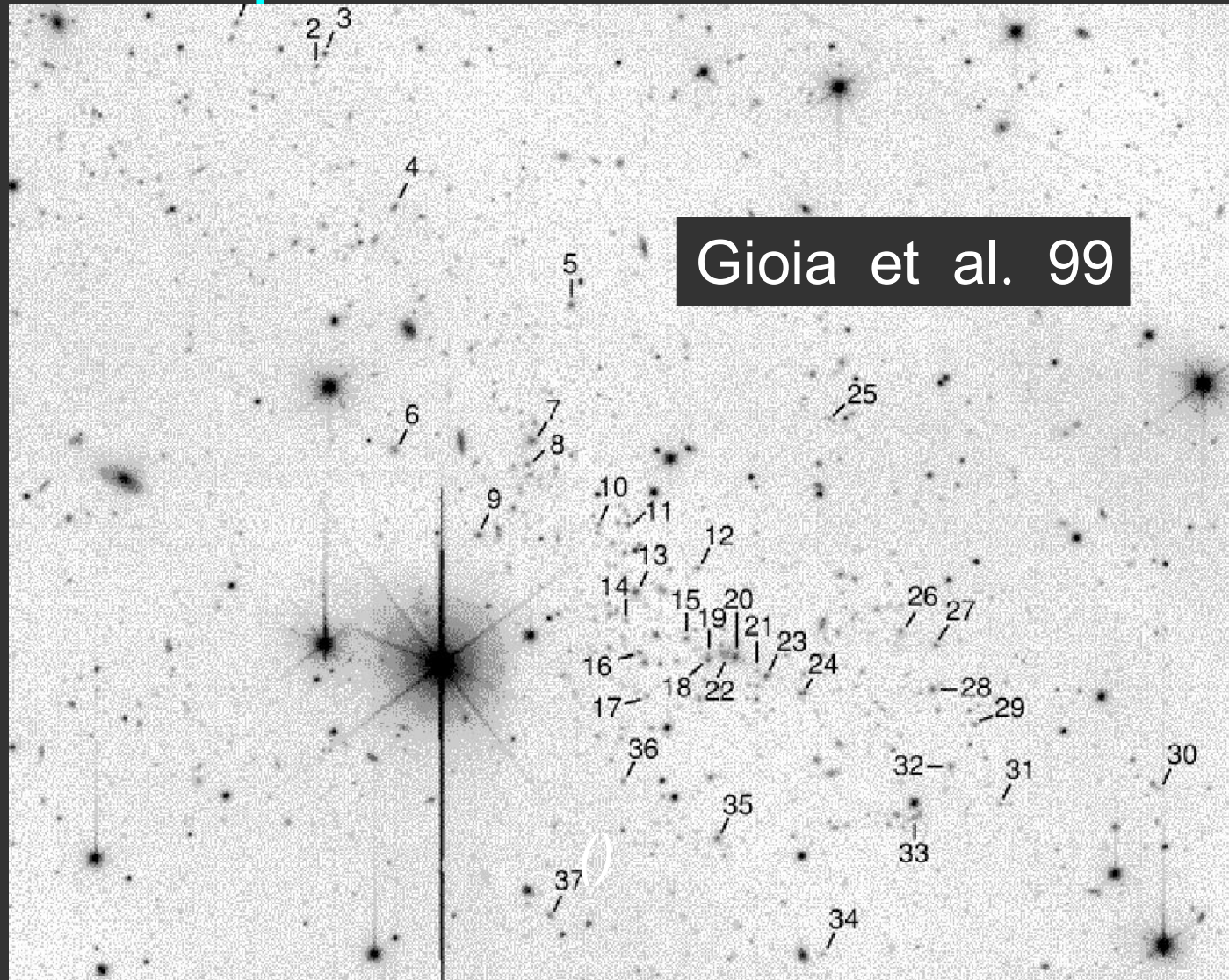
# Shape results: evolution



*(Melott et al. 01, Plionis 02; but see Flin et al. 04)*

Higher- $z$  galaxy clusters are less spherical;  
trend in agreement with theoretical expectations  
*but maybe too strong?* *(Floor et al. 04)*

# Shape results: evolution



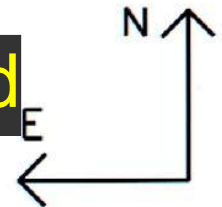
Very distant galaxy clusters are very elongated



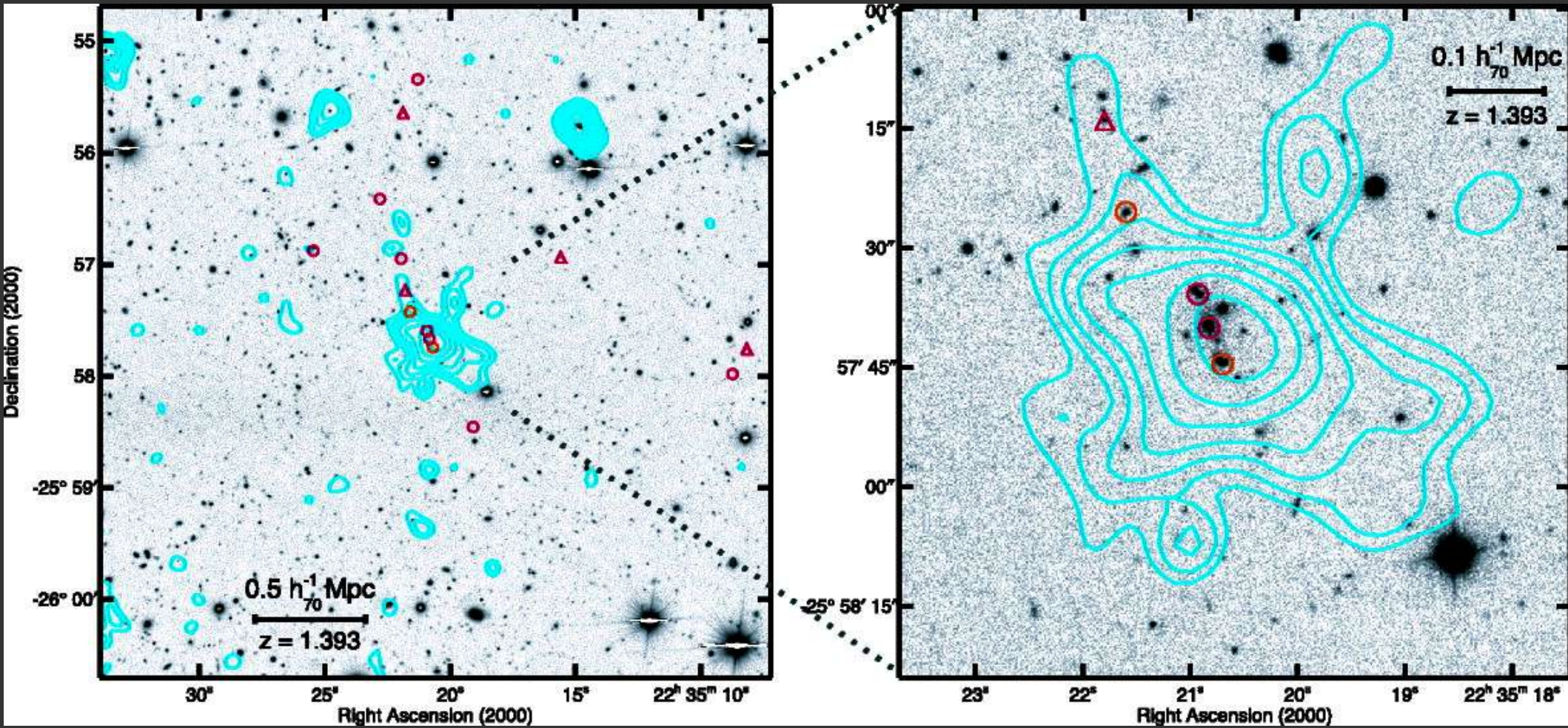
# Shape results: evolution

van Dokkum et al. 00

Very distant galaxy clusters are very elongated



# Shape results: evolution



*Mullis et al. 05*

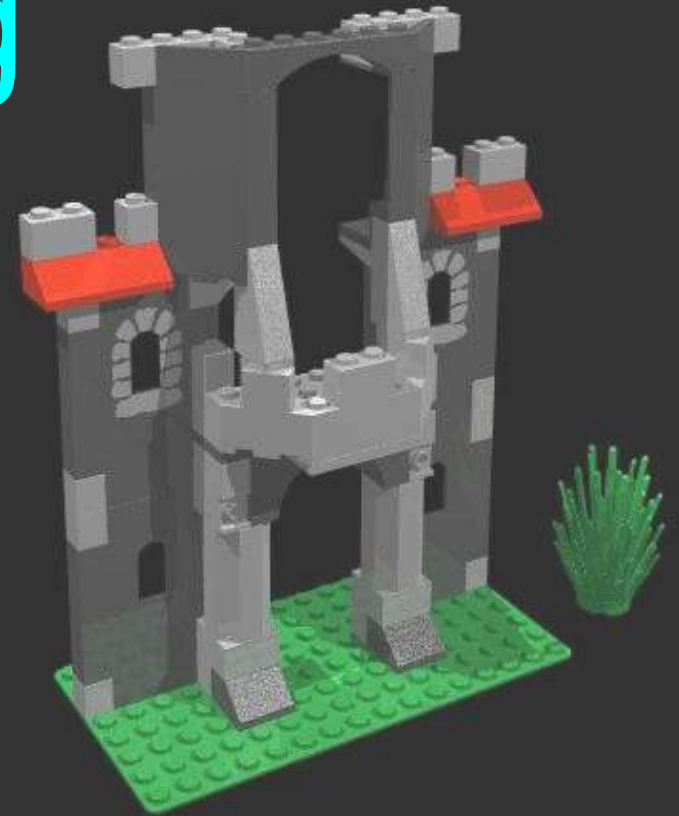
Very distant galaxy clusters are very elongated

# Shape results summary:

- ◆ Nearby clusters are less elongated than nearby groups  
Conflict with predictions from num. sims.?  
(but: are observed groups *virialized* low-mass haloes?)
- ◆ Distant clusters are more elongated  
Projection effects more severe for mass estimation

*Progress: clusters shape distribution at high-z*

# Subclustering





# Historical



Excess of low-velocity galaxy pairs in Virgo  
from van den Bergh (1961)

# Scientific motivations

- Constrain cosmological build-up of structures
- Cluster mass estimates are affected by subclustering (collisions & mergers)
- Influence on internal properties of galaxies

# Subclustering results

**Frequency of clusters with subclusters: 30–80 %**

*(Geller & Beers 82, Dressler & Shectman 88, Salvador-Solé et al. 93, Bird 94, Escalera et al. 94, Girardi et al. 97, Kriessler & Beers 97 ...)*

*But fraction overestimated because of projection effects (Kolokotronis et al. 01)*

**Typical size of detected subclusters: 0.4–0.6 Mpc**

*(Geller & Beers 82, Salvador-Solé et al. 93, Escalera et al. 94, Girardi et al. 97)*

**Their typical mass: 10% Mass of parent cluster**

*(Escalera et al. 94, Girardi et al. 97)*

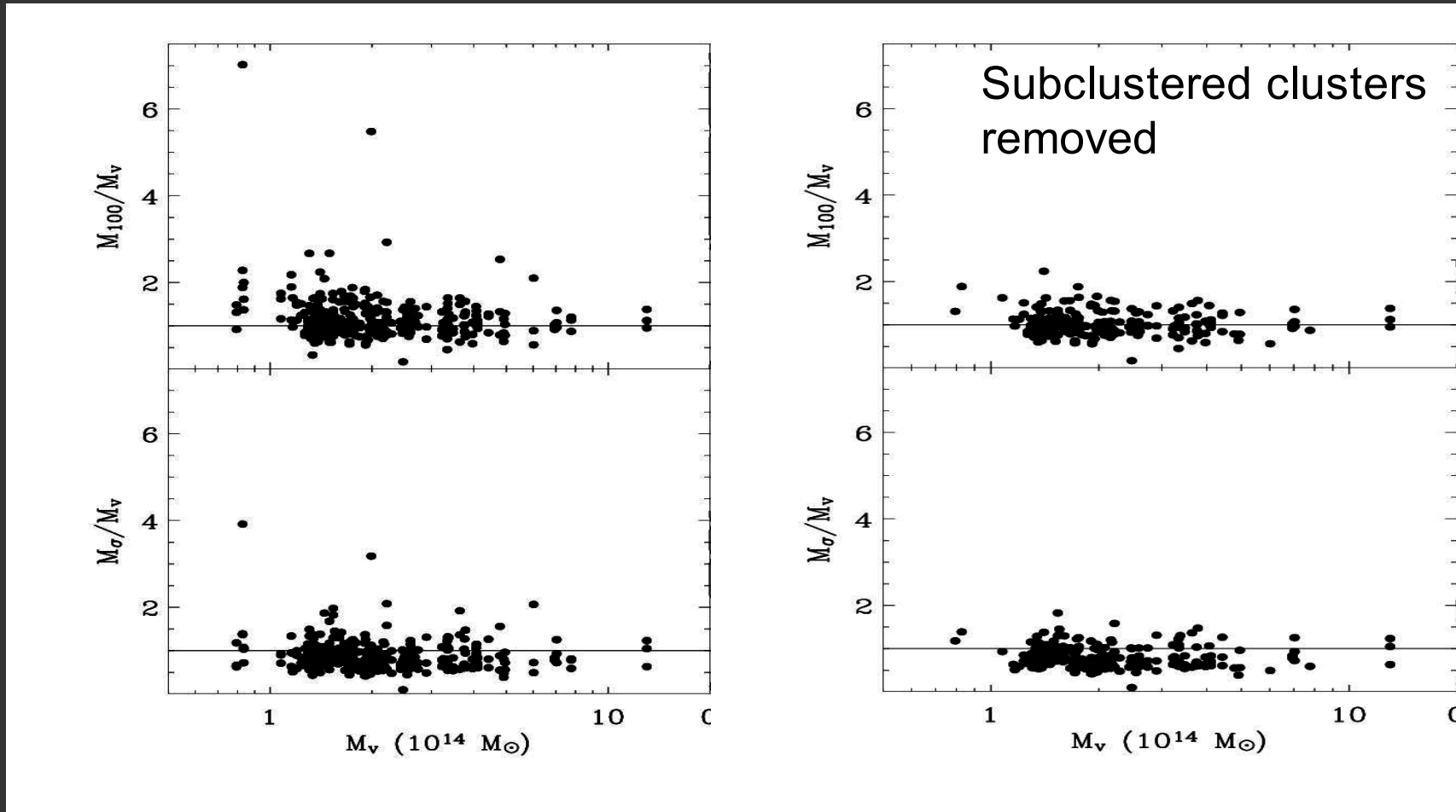
**10–20% clusters are bimodal** *(Girardi et al. 98)*

*Hence virial mass estimates are little affected on average*

# Subclustering results

Simulations: subclusters are a serious concern for virial mass estimates, when unaccounted for; but subclustered clusters can be identified and removed

$\sigma_v$ -based Mass-estimate    Virial mass estimate



(B., Murante, Borgani, Dolag et al. in prep.)

# Subclustering results: WINGS

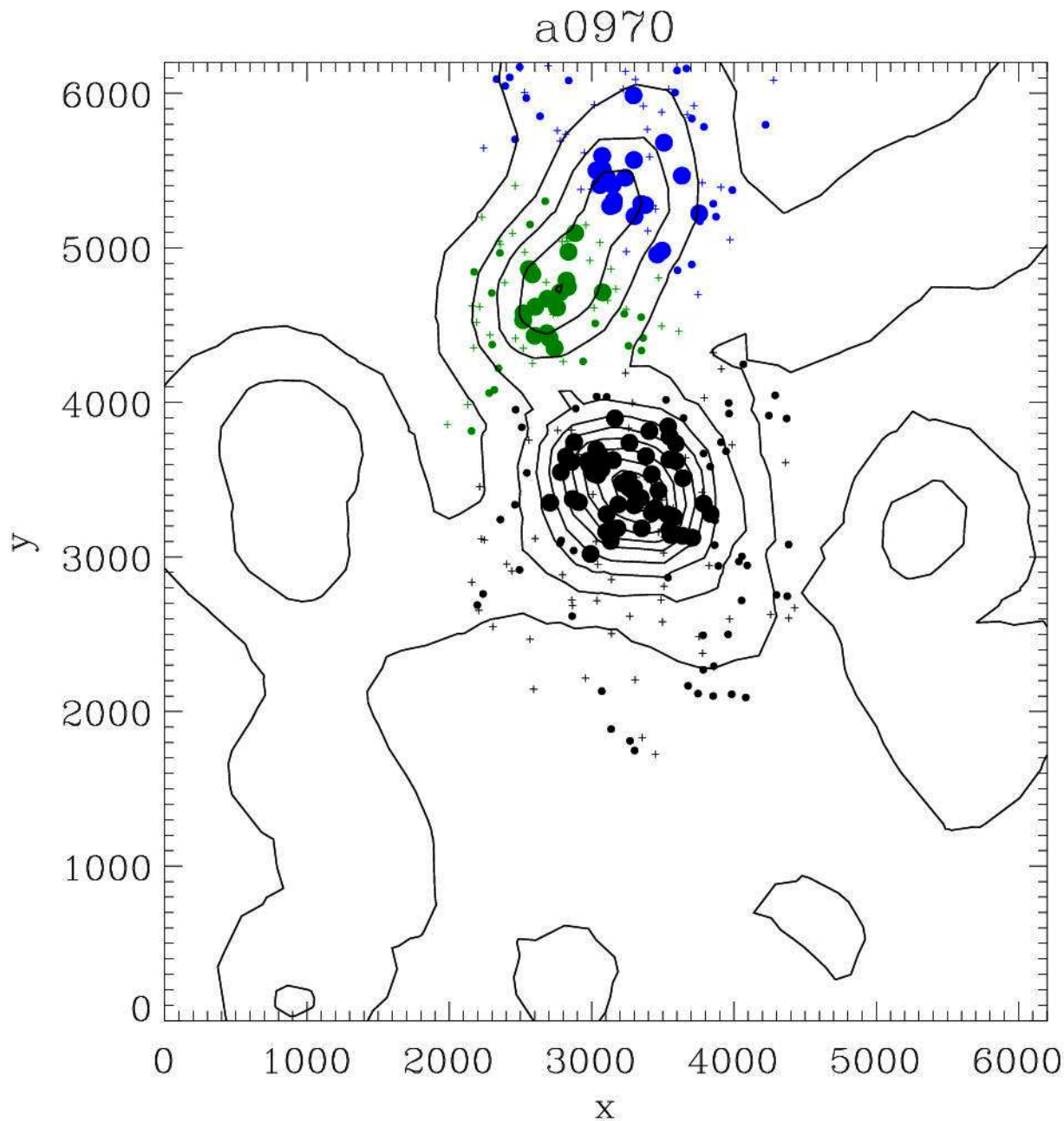
A wide-field, multiwavelength imaging and spectroscopic survey of 78 nearby clusters  
*(Fasano et al. 05)*

*Work in progress to establish the frequency of subclusters in WINGS clusters and the properties of subcluster galaxies relative to the whole cluster population.*

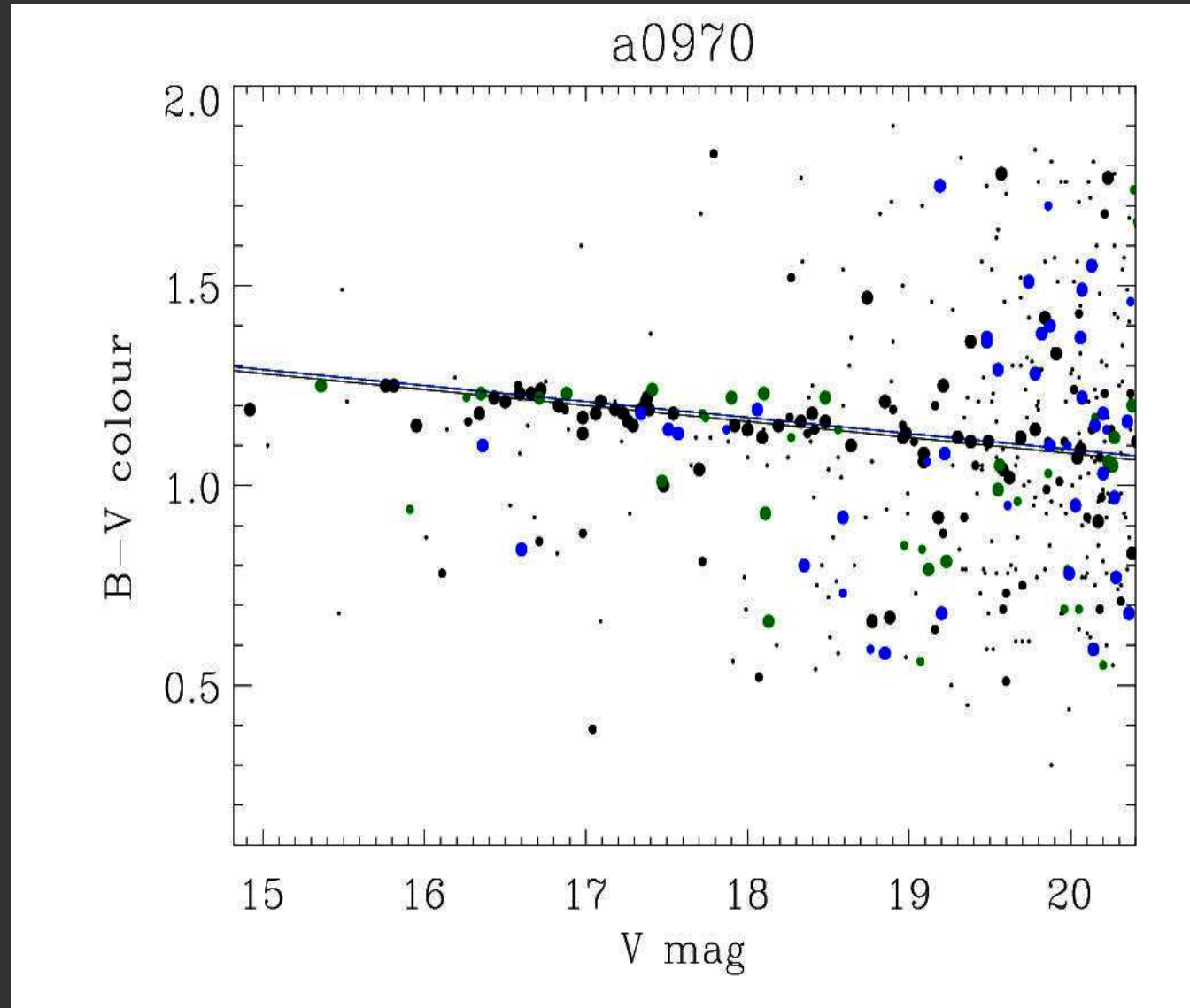
*Current analysis of projected galaxy distribution with the DEDICA algorithm for structure detection  
(Pisani 1996; Ramella et al. in prep.)*

# Subclustering results: WINGS

Three  
structures  
detected  
by DEDICA



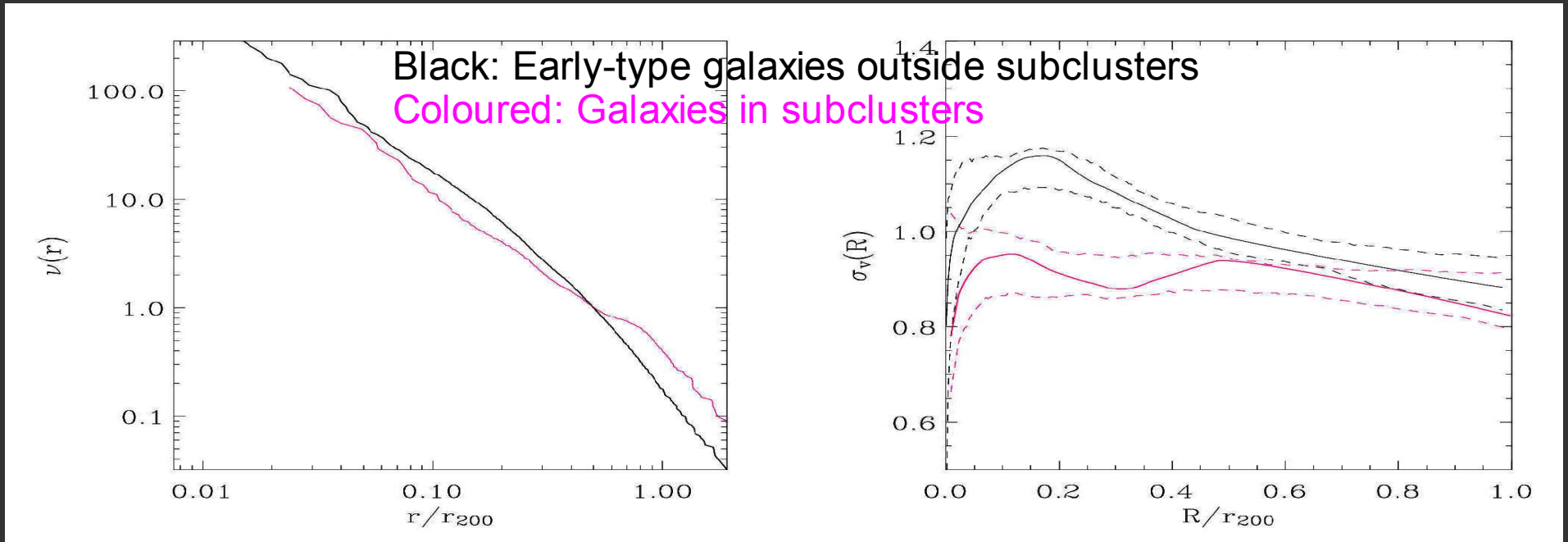
# Subclustering results: WINGS



Use location in colour-magnitude diagram to distinguish real subclusters from projected structures

# Subclustering results: ENACS *(Katgert & B. in prep.)*

Identify individual galaxies in substructures rather than subclusters as a whole



Preliminary results:

- 31 % cluster galaxies are in subclusters
- Substructure galaxies avoid the central cluster regions and have small velocities  $\rightarrow$  tangential velocity anisotropy
- There are relatively more emission-line galaxies in substructures than in the cluster as a whole ( $30 \pm 6$  % vs.  $15 \pm 3$  %)



# Subclustering results summary:

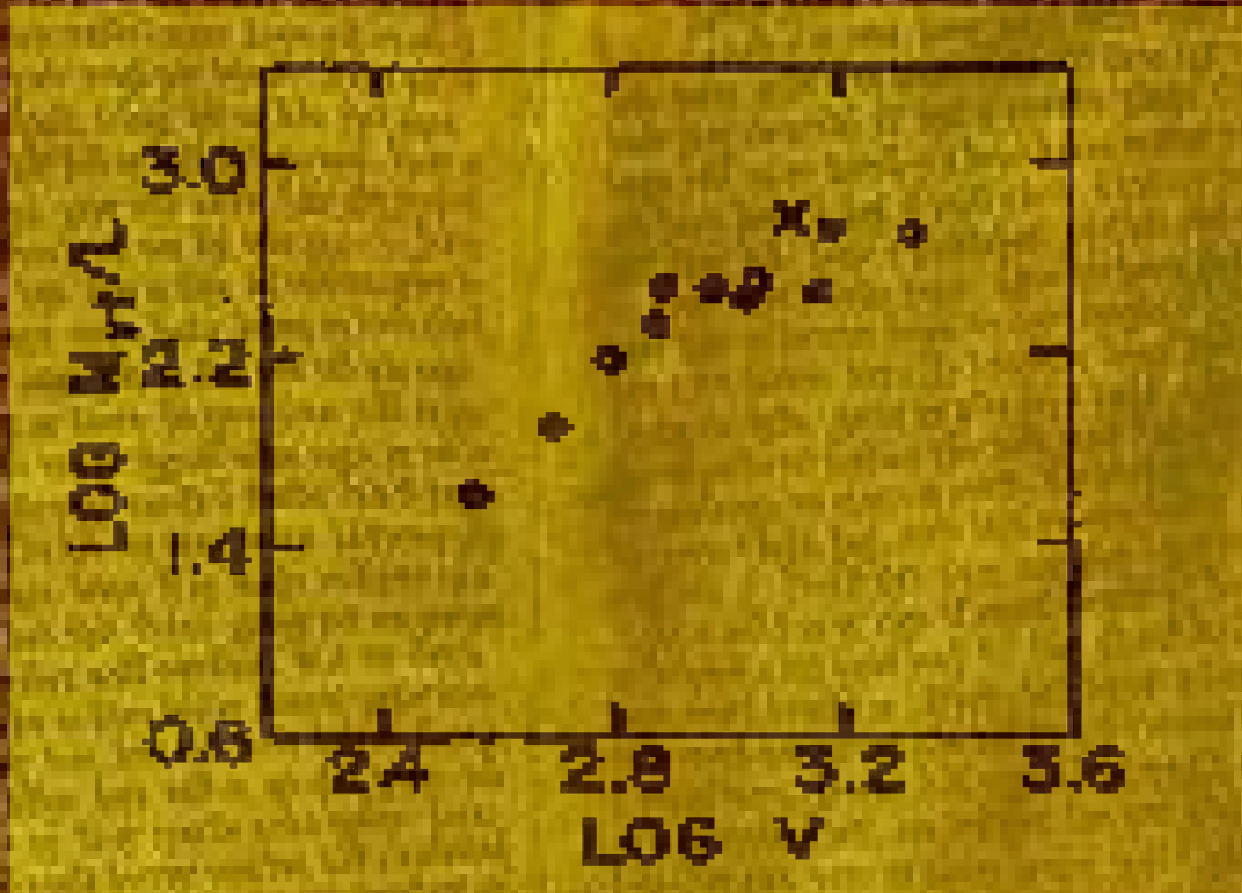
- ◆ Good identification of subclusters in nearby clusters: allows for a cleaner statistical sample of cluster masses
- ◆ Higher fraction of emission-line galaxies in subclusters than in the cluster as a whole
- ◆ Galaxies in subclusters follow tangential orbits
- ◆ Only sparse results on more distant clusters  
(e.g. *Halliday et al. 04: 10–100 % cls. with subcls.;*  
*Rosati et al. 99, Lubin et al. 00, Pentericci et al. 00*  
*and Haynes et al. 01: merging subcls. at high-z)*

*Progress: characteristics of subcluster properties and systematic analysis in distant clusters*

# Scaling Relations



# Historical



M/L increases with the velocity dispersion of the galaxy system (Rood 1974)

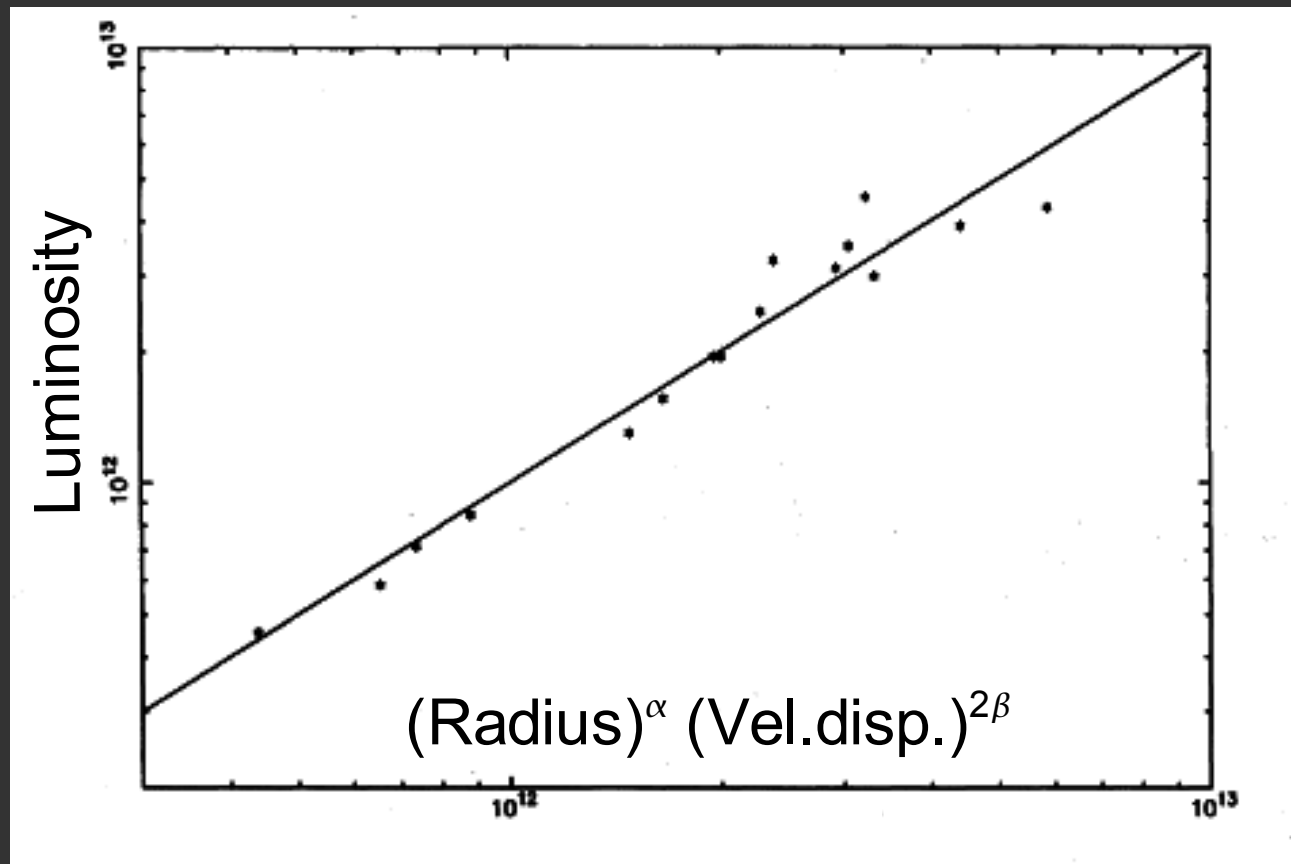
# Scientific motivations

- Understand the efficiency of galaxy formation, and/or the ageing/evolution of galaxies  
(*e.g. Bahcall et al. 00; Lin, Mohr & Stanford 04*)
- Use optical luminosities as cheap proxies for cluster masses (*e.g. Yee & Ellingson 03*)

# Scaling relations: results

Cluster global quantities lie on a fundamental plane

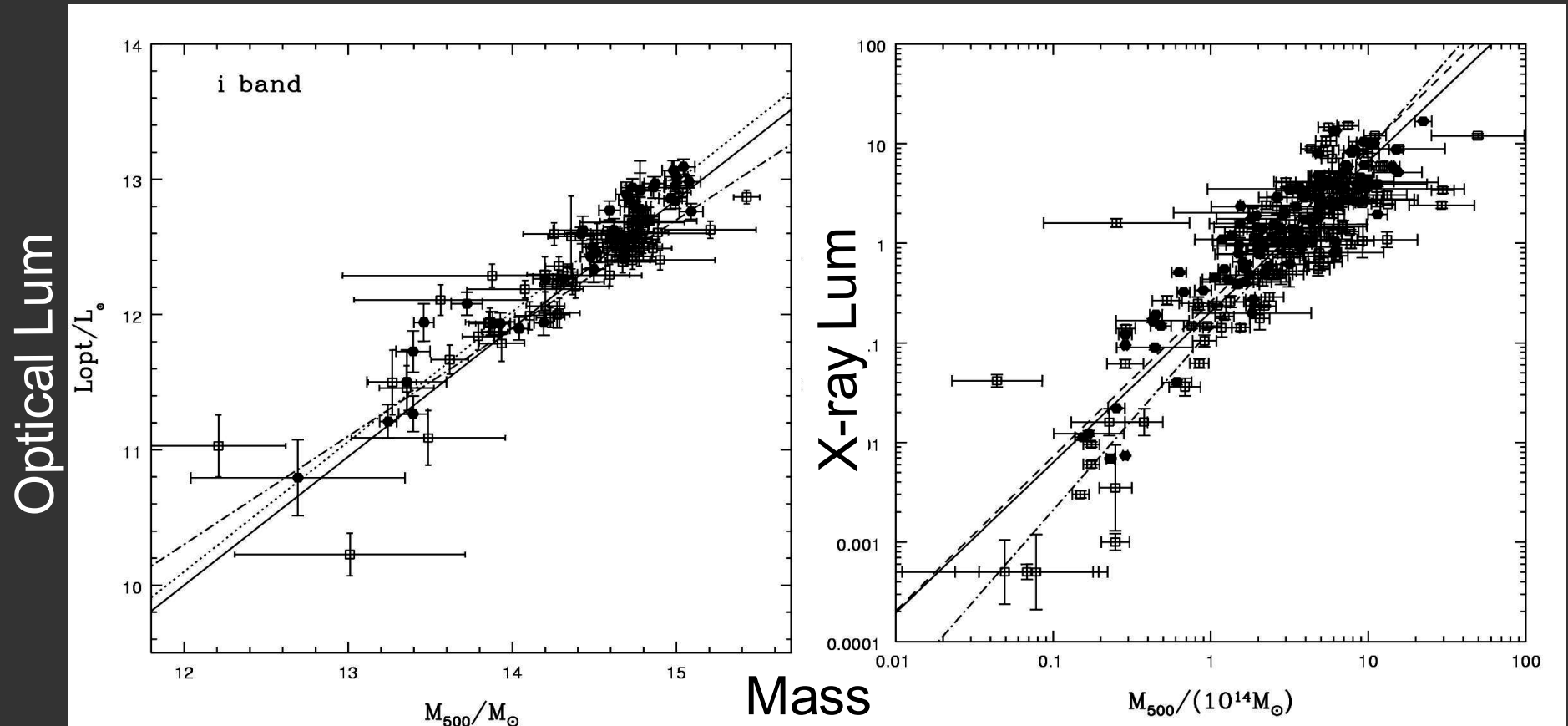
(*Schaeffer et al. 93, Adami et al. 98, ...*)



FP  $\Rightarrow M/L \propto M^\gamma, \gamma=0.4-0.5$

# Scaling relations: results

$L_{\text{opt}}$  is as good a proxy for  $M$  as  $L_x$  (or better)  
(*Yee & Ellingson 03; RASS+SDSS, Popesso et al. 05*)



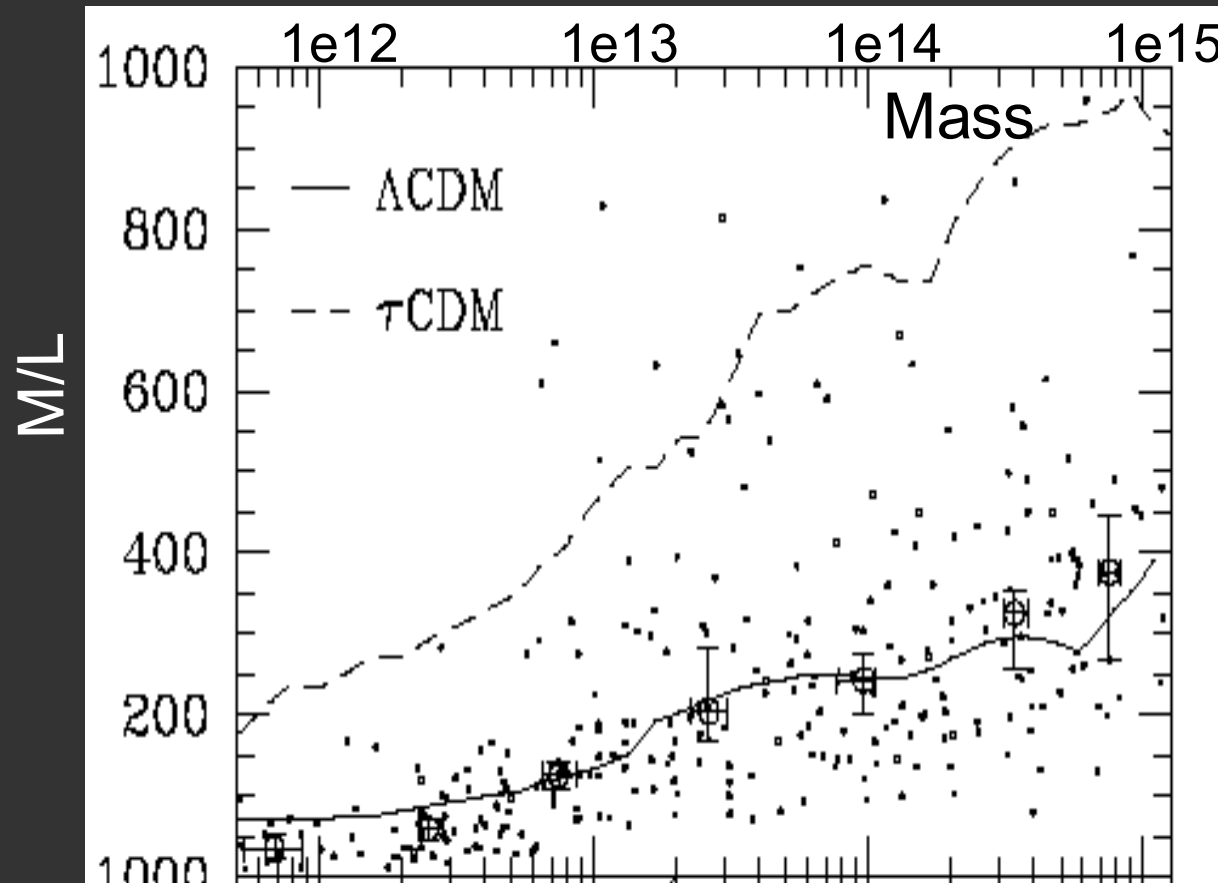
Fitting a power-law:  $M/L \propto M^{\gamma}$ ,  $\gamma=0.2$

The slope is the same in the four SDSS bands

# Scaling relations: groups & clusters

**M/L vs. M (or L) is not a power-law**

*(NOG groups + rich clusters catalogue, Girardi et al. 02)*

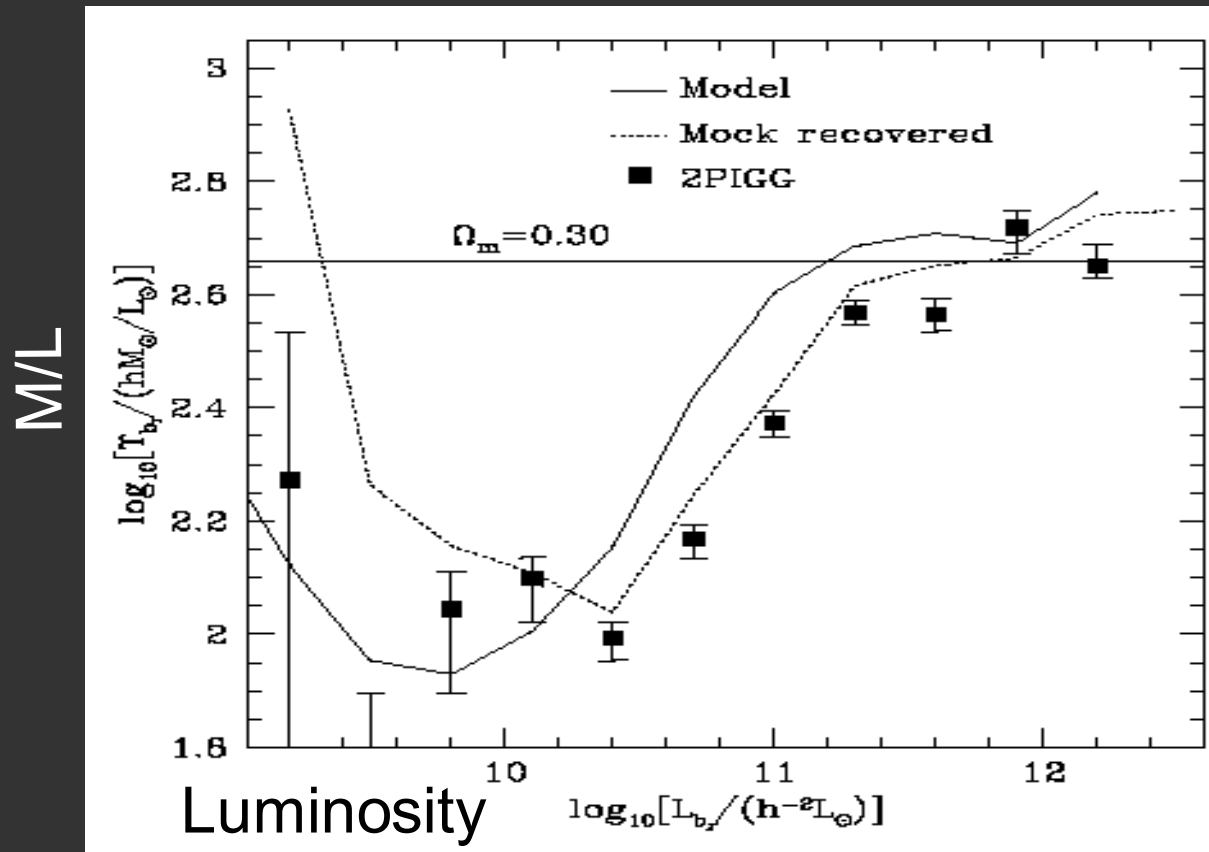


**Agreement with theoretical expectations**

*(Kauffmann et al. 1999)*

# Scaling relations: groups

Groups M/L vs. M (or L) is not a power-law  
(2dFGRS groups catalogue, Eke et al. 04)



Agreement with theoretical expectations  
(e.g. Benson et al. 2000)

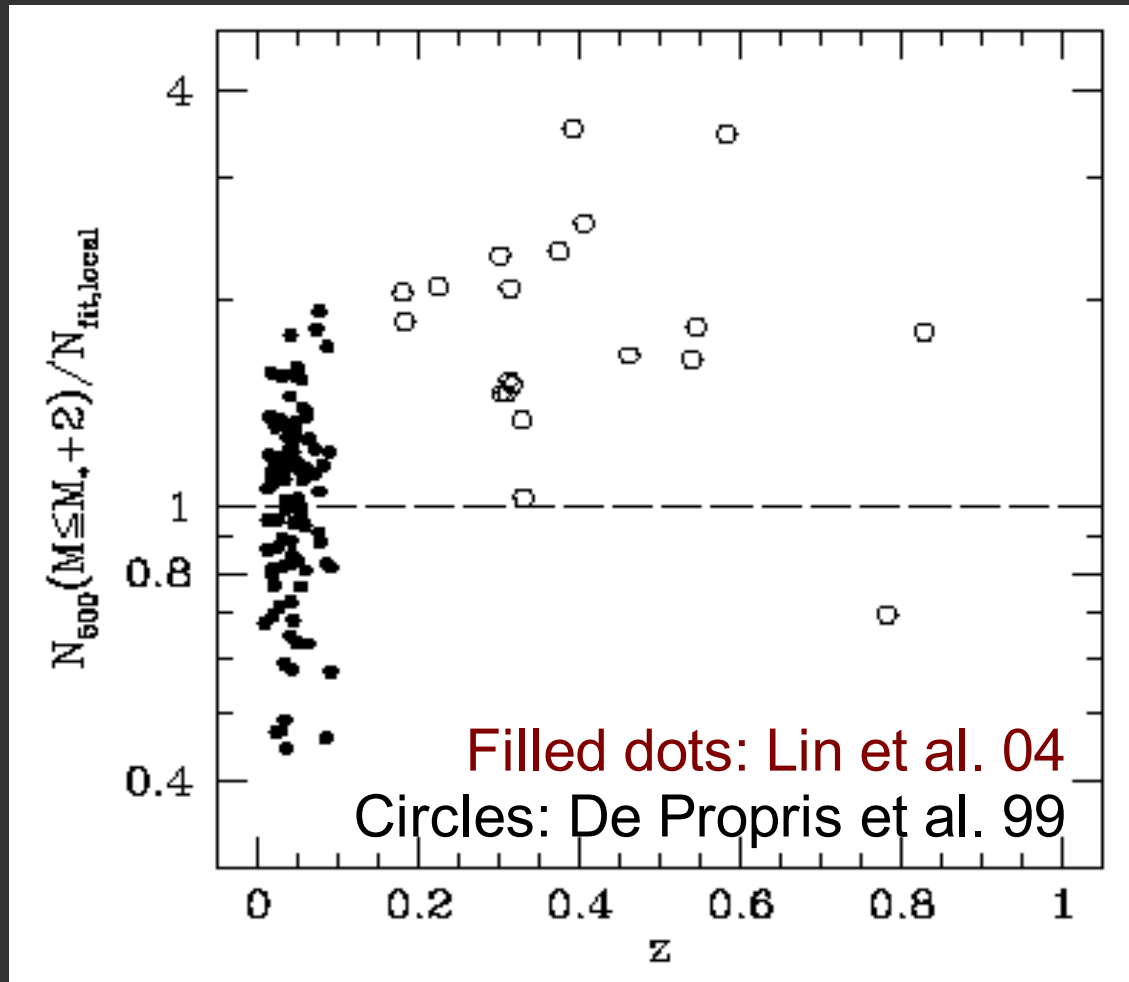


# Scaling relations: evolution

(Lin, Mohr, & Stanford 04)

More distant clusters have a higher mean number of galaxies per given mass

Scaled Halo Occupation Number



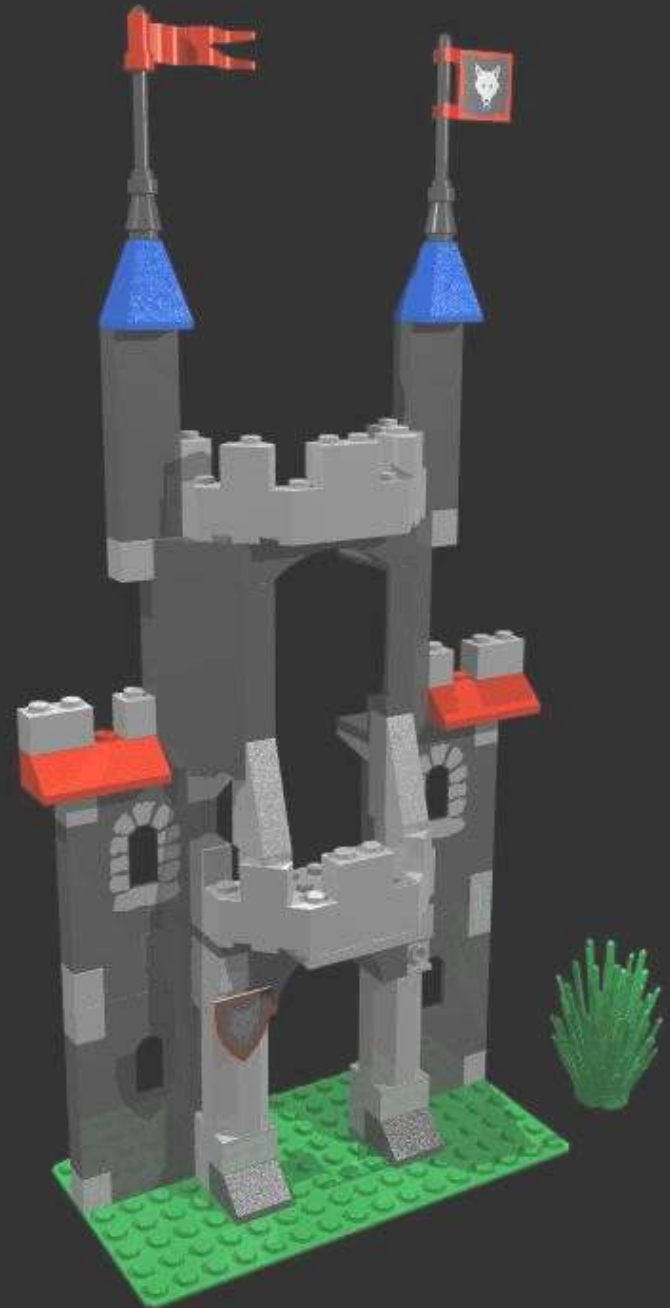
Galaxy evolution must act as to decrease cluster HON with time (merging, fading, stripping,...)

# Scaling relations results summary:

- ◆ Cluster global properties lie on a FP
- ◆ Mass-to-light is higher in higher mass galaxy systems
- ◆ M/L vs. M relation does not depend on  $\lambda$ 
  - $\neq$  galaxy formation efficiencies in clusters of  $\neq$  mass?  
or  $\neq$  galaxy evolution in clusters of  $\neq$  mass?  
*(simple ageing of galaxy populations cannot explain the scaling)*
- ◆ Higher number of galaxies per given system mass at higher  $z$

*Progress:* Scaling relations as a function of cluster properties and redshift

# Summary & conclusions



- ◆ Mass profile: at  $r > r_{200}$ , slope is -3 or -4,  
at  $r \simeq 0$ , cusp or small core (galaxy-sized) are allowed;  
similar  $M(r)$  for  $z \simeq 0$  and  $z \simeq 0.3$  clusters;  
trend of concentration with mass as expected
- ◆ Mass-to-light profile: red galaxies trace the mass within  $r_{200}$ ,  
but  $M/L$  decreases beyond  $r_{200}$  and also at  $r \simeq 0$ ;  
groups have higher  $M/L$  near the centre;  
 *$z \simeq 0.4$  clusters have flatter  $M/L$*
- ◆ Orbits of galaxies: isotropic for E, S0, Sa-b,  
increasingly radial with radius for Sbc-Irr,  
*tangential for galaxies in subclusters;*  
 *$z \simeq 0.3$  clusters have more galaxies on radial orbits*

- ◆ Shape: richer galaxy systems are less elongated, distant clusters are more elongated
- ◆ Subclusters: subcluster detection allows correcting wrong cluster mass estimates,  
*1/3 of all cluster galaxies are in subclusters, subclusters contain relatively more emission-line galaxies, subclusters have tangential orbits*
- ◆ Scaling relations: cluster global properties obey a FP, M/L increases with M, slope of M/L vs. M relation changes with M, not with  $\lambda$ ,  
*the halo occupation number increases with z*

# Conclusions

*Current constraints on cluster structure from optical observations (lensing excluded):*

- ✓  $M(r)$  and orbits of red galaxies out to  $z \simeq 0.3$ ,*
- ✓ cluster shapes out to  $z \simeq 0.2$ ,*
- ✓  $M/L$ , orbits of blue galaxies, subclusters, and scaling relations only at  $z \simeq 0.0$*

*...more to come soon from EdisCS and IMACS!*

Thank you for  
your attention!



More material  
(not shown at  
the workshop)

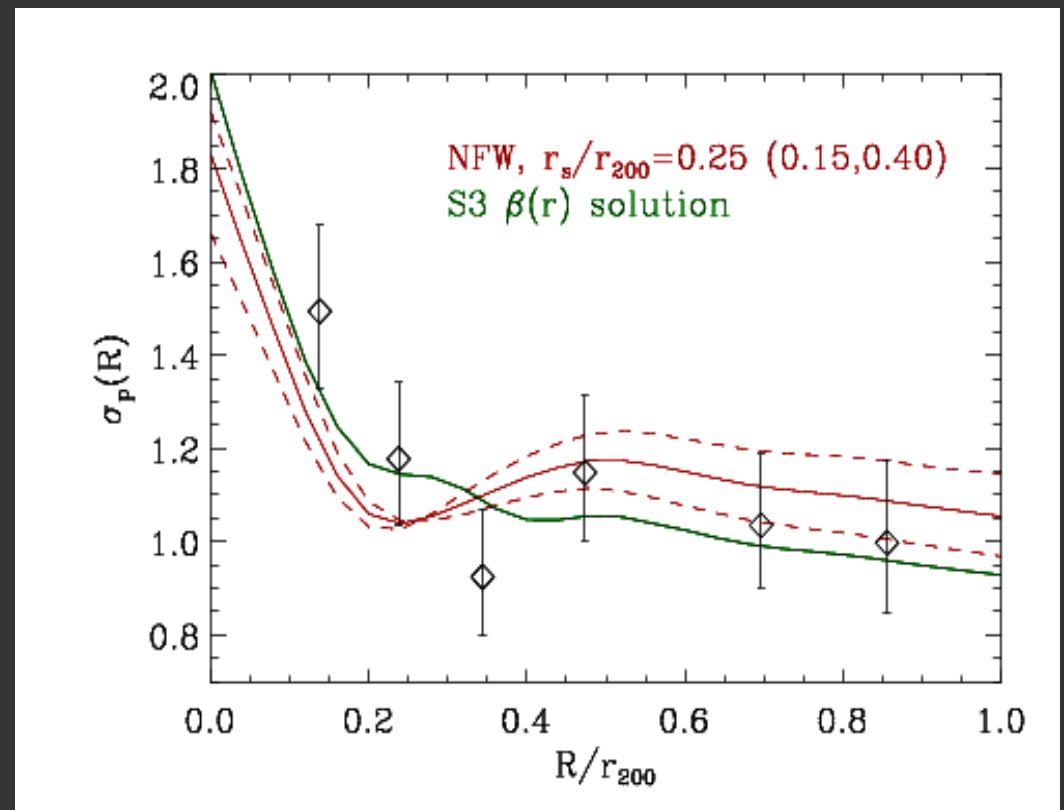


# M(<r) for clusters from the ENACS

E+S0 M(<r) confirmed using other cluster galaxy populations

Given M(<r) solve  
Jeans eq.s for  $\beta(r)$

(see Binney & Mamon 82,  
Merrifield & Kent 90,  
Solanes & Salvador-Solé 90,  
Dejonghe & Merritt 92)



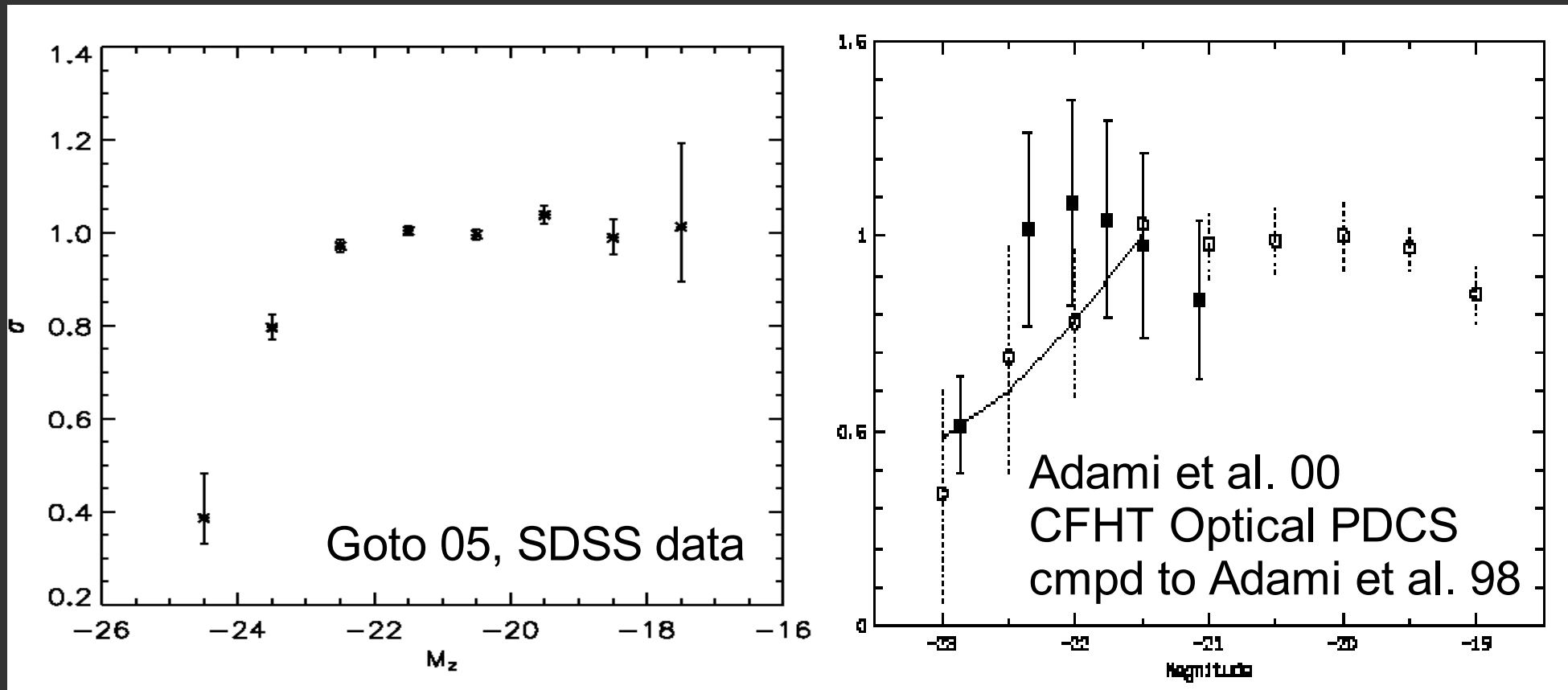
Early spirals in equilibrium within the same grav. potential  
traced by E+S0, with nearly isotropic orbits

# M/L results: evolution

Brighter galaxies move slower in clusters

(*B. et al. 92, Adami, B. & Mazure 98, Goto 05*)

and perhaps also in groups (*Girardi et al. 03, Lares et al. 04*)



Some evolution of luminosity segregation in clusters at  $z \simeq 0.4$ ?  
→ larger M/L at  $r \rightarrow 0$  in distant clusters

# M(<r) for clusters from the ENACS

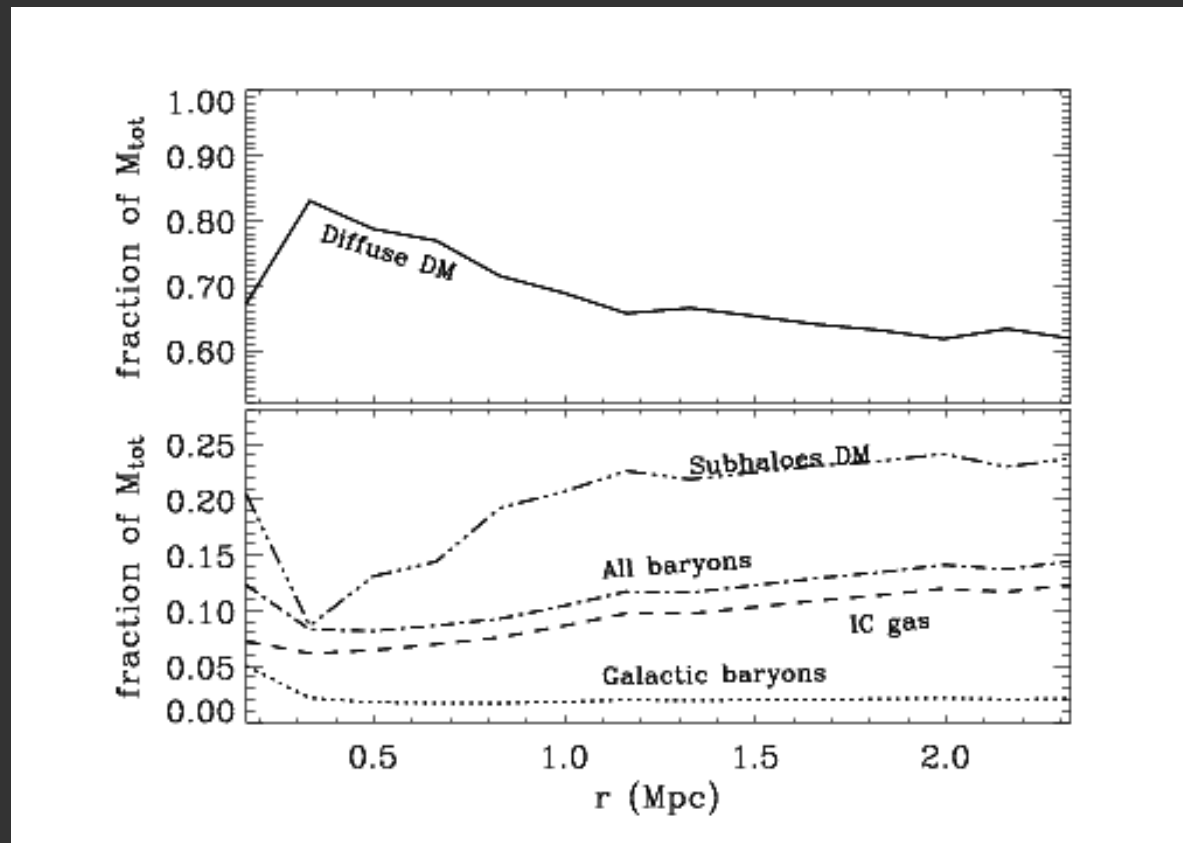
Biviano & Salucci 05 (work in progress):

Determine the DARK MATTER,  
not the TOTAL MATTER profile

- *Convert galaxies luminosities into baryonic masses (Borriello, Salucci & Danese 03; Persic & Salucci 99)*
- *Estimate the Intra-cluster gas baryonic mass profile using the clusters sample of Reiprich & Boehringer 02*
- *Determine the Dark Matter profile in subhaloes from galaxy luminosities (Shankar, Salucci & Danese 05) by also accounting for halo stripping and overlapping*

# M(<r) for clusters from the ENACS

Fractions of total mass in galactic and gas baryons and in dark matter subhaloes

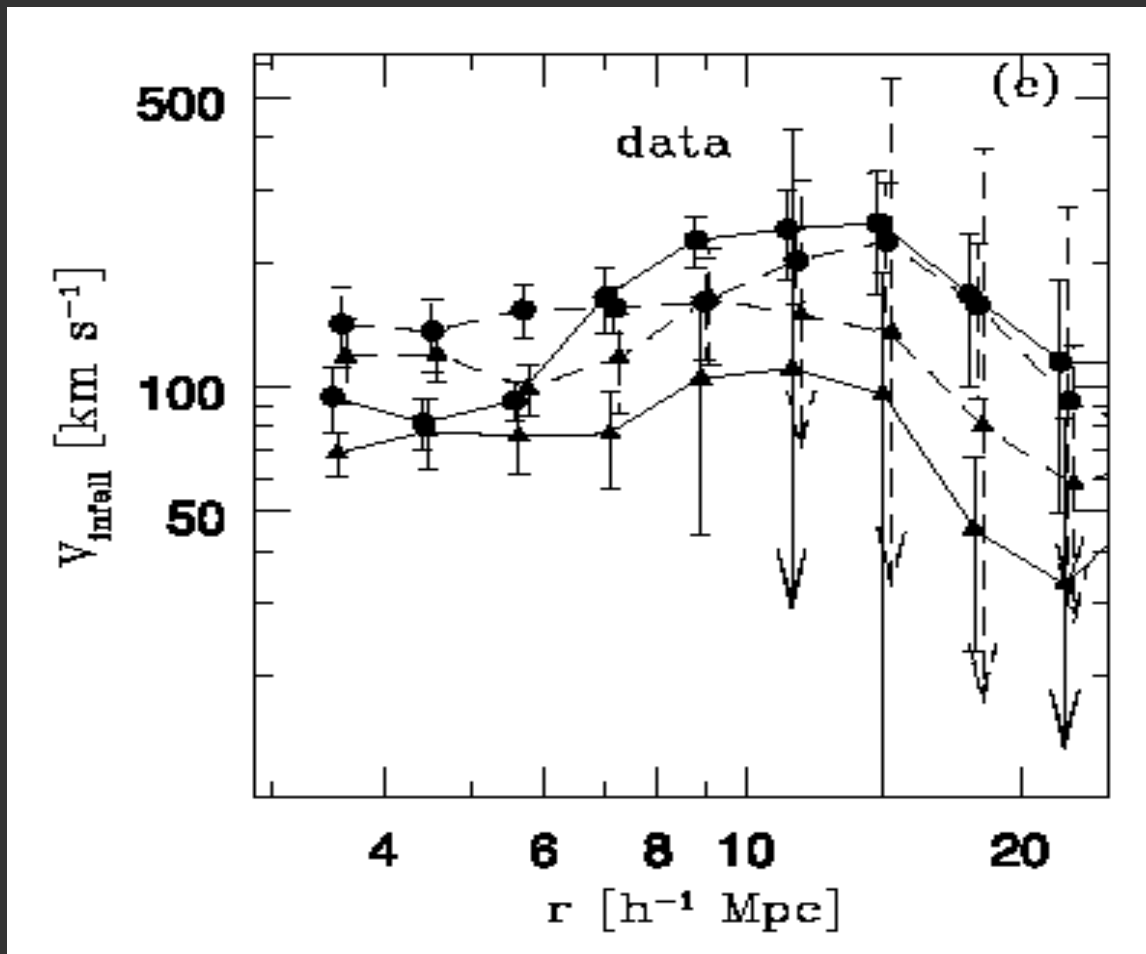


- Subtracting the baryons from the total mass makes M(<r) more concentrated (NFW  $c=5\pm 2$ , Burkert 95  $r_c=0.13 r_{200}$ )
- Subtracting also the Dark Matter subhaloes makes M(<r) even more concentrated (NFW  $c=8\pm 2$ , Burkert 95  $r_c=0.09 r_{200}$ )

Both the NFW and the Burkert 95 models are still acceptable

# Orbits results: infall *(Ceccarelli et al. 05)*

The infall of field galaxies into groups is measured directly by using the Catalog of Peculiar Velocities *(Giovanelli & Haynes 02)*



Dots: high-M or high-L groups

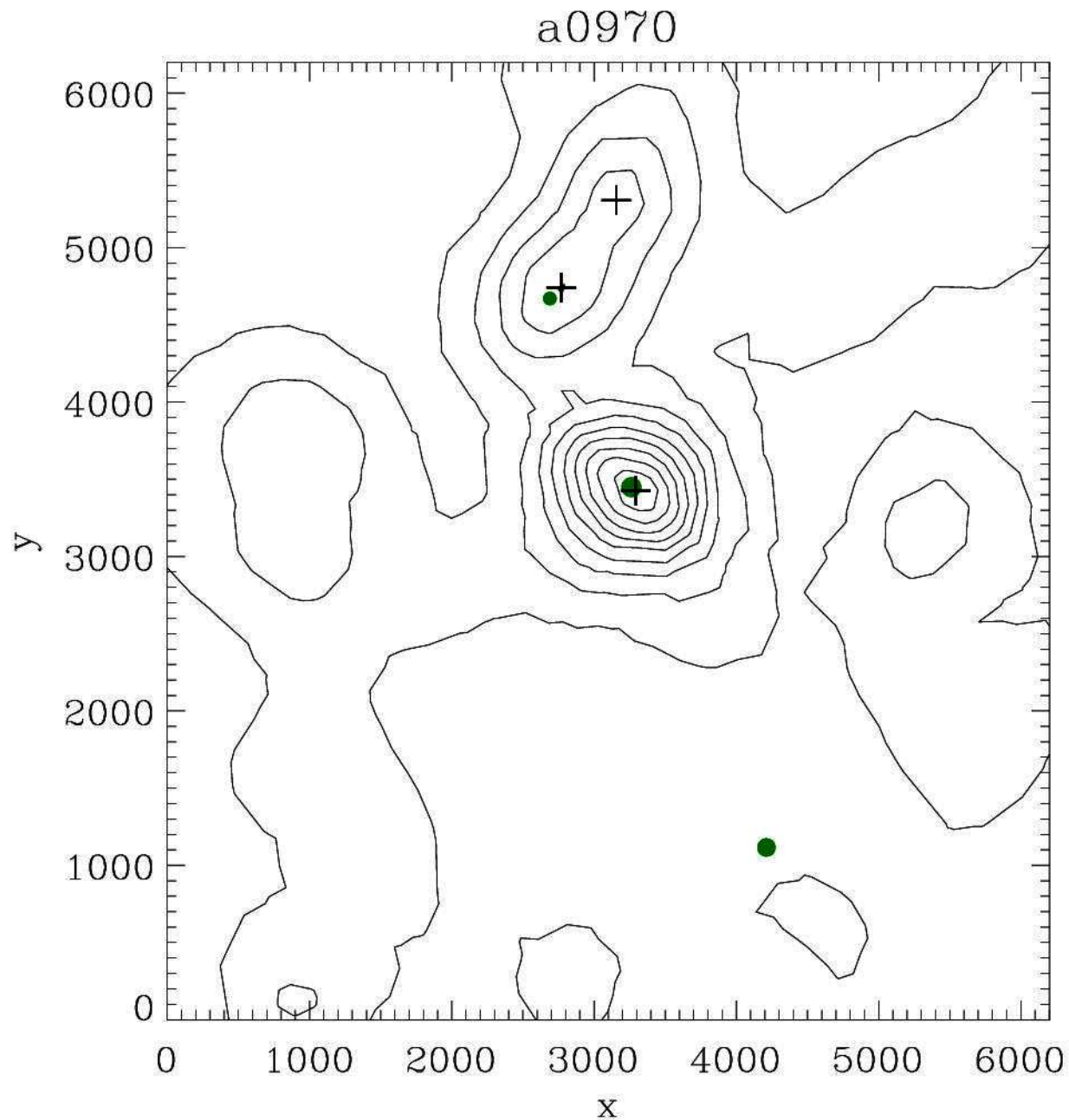
Triangles: low-M or low-L groups

Solid lines: groups divided by Lum

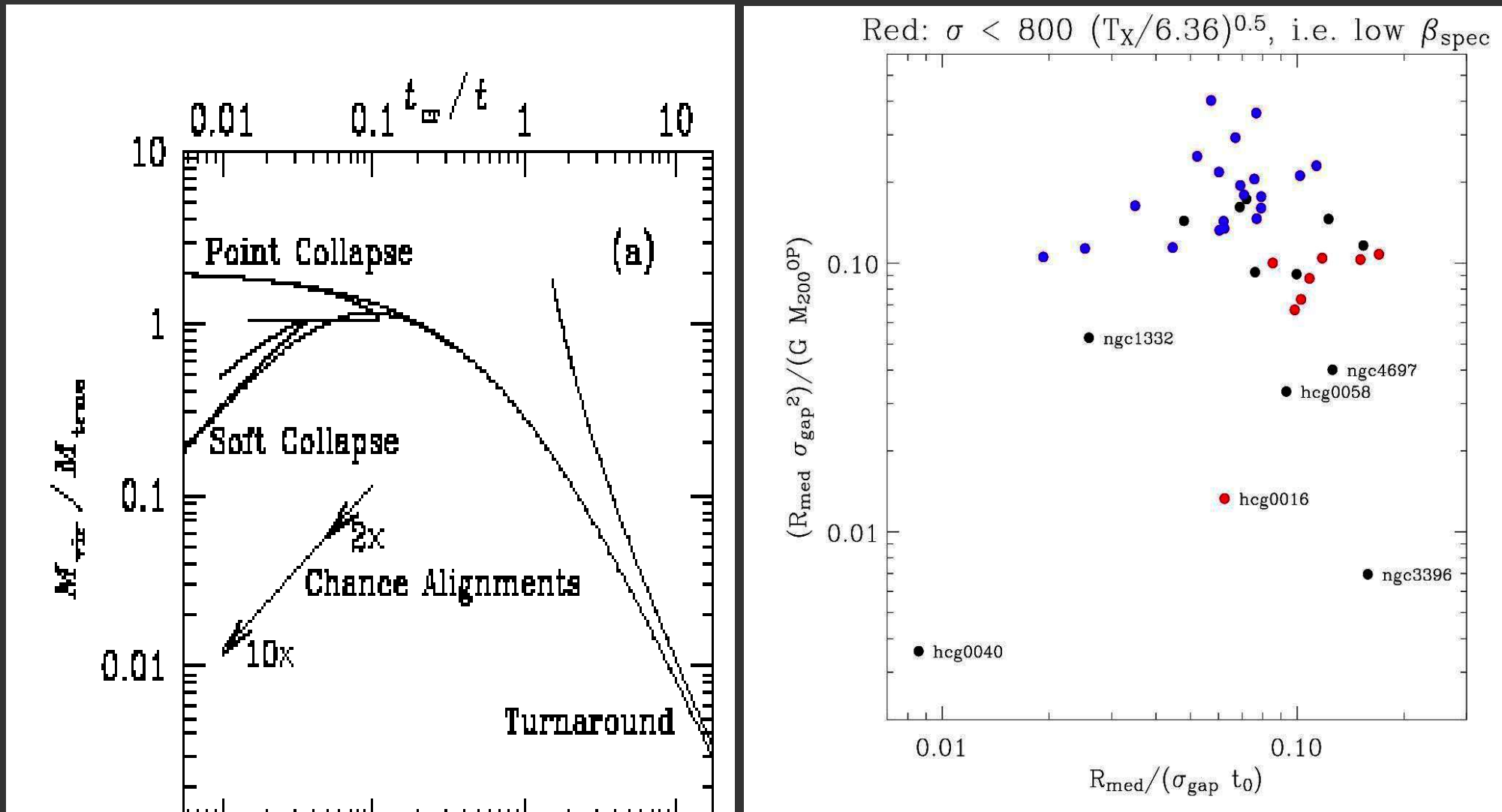
Dashed lines: groups divided by Mass

# Subclustering results: WINGS

Location of  
BCGs



# Are groups virialized? GEMS

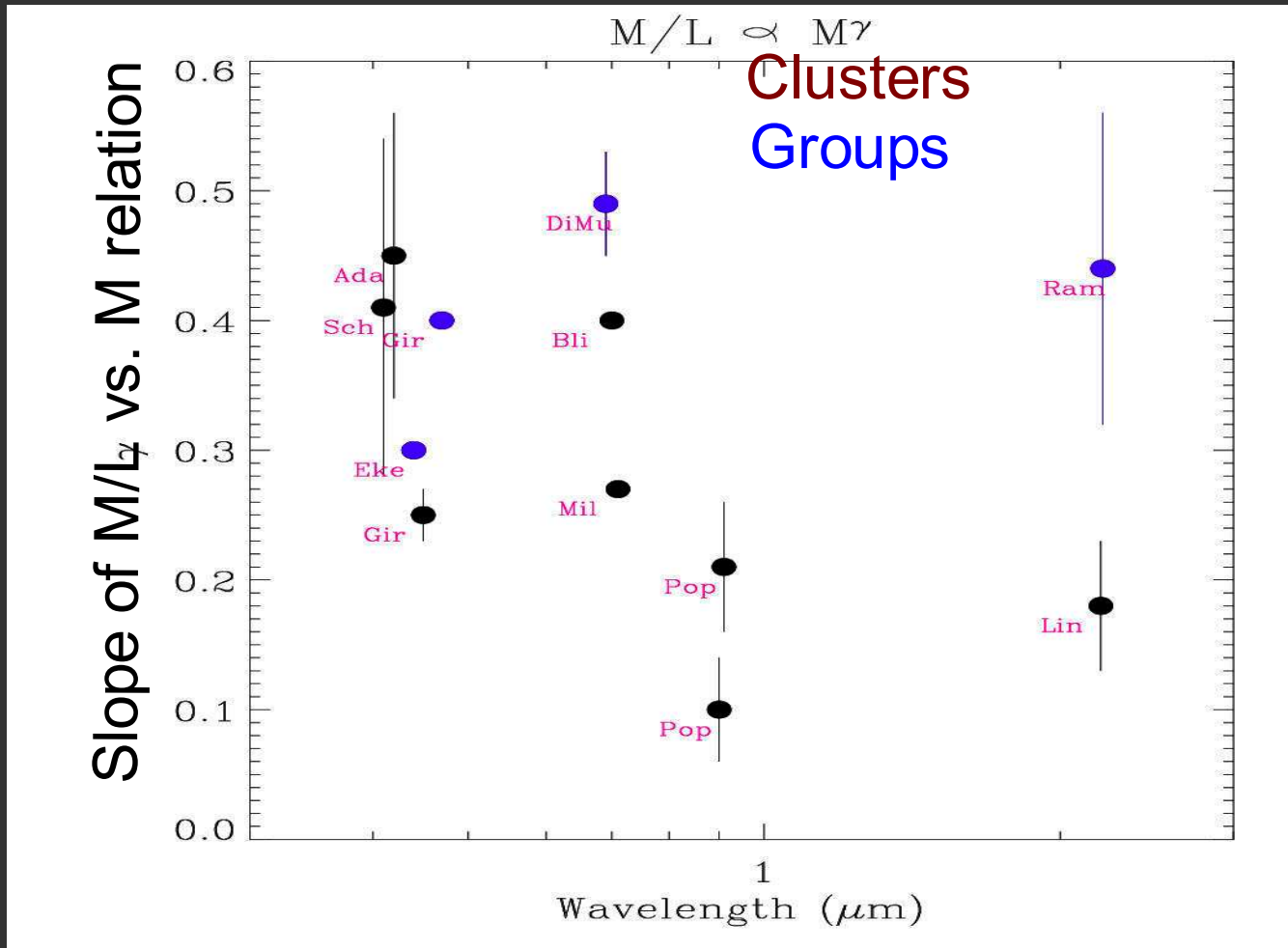


The 'fundamental track' diagram of Mamon 94  
(spherical collapse theory)

# Scaling relations: results

Does the slope  $\gamma$  of  $M/L \propto M^\gamma$  depend on  $\lambda$ ?

(no evidence in RASS-SDSS sample, Popesso et al. in prep.)



Implications for interpretation of why  $M/L \neq \text{const}$