

poly3D

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1 Todo List

Global `poly3D::operator+= (const trino3D &oth)`

allow for annihilation of coefficients and elimination of associated products..

2 Data Structure Index

2.1 Data Structures

Here are the data structures with brief descriptions:

<code>point3D</code>	2
<code>poly3D</code>	4
<code>trino3D</code>	7
<code>Zern3DRadii</code>	9

3 File Index

3.1 File List

Here is a list of all files with brief descriptions:

<code>poly3D.cpp</code>	10
<code>poly3D.h</code>	12

4 Data Structure Documentation

4.1 point3D Class Reference

Public Member Functions

- `point3D ()`
- `point3D (const double X, const double Y, const double Z)`
- `point3D (const double cart[TURB3D_DIM])`
- `point3D (const point3D &orig)`
- `double dist () const`
- `double dist (const point3D &oth) const`
- `void scale (const double radius)`
- `void normalize (const double newleng)`
- `void phithet (double rtp[3]) const`
- `point3D & operator= (const point3D &right)`
- `point3D & operator*= (const double c)`
- `point3D & operator+= (const point3D &right)`
- `point3D & operator-= (const point3D &right)`

Data Fields

- `double xyz [3]`

4.1.1 Detailed Description

A point in a 3D domain.

Since

2008-09-22

4.1.2 Constructor & Destructor Documentation

4.1.2.1 point3D::point3D ()

Default Ctor at the origin of coordinates

4.1.2.2 point3D::point3D (const double X, const double Y, const double Z)

Ctor from individual cartesian coordinates

4.1.2.3 point3D::point3D (const double cart[TURB3D_DIM])

Ctor with given 3D coordinates

4.1.2.4 point3D::point3D (const point3D & orig)

Copy constructor.

4.1.3 Member Function Documentation

4.1.3.1 double point3D::dist () const

Distance to the origin

4.1.3.2 double point3D::dist (const point3D & oth) const

Distance to another point

4.1.3.3 void point3D::normalize (const double newleng)

Scale components so the new length equals a given number

Parameters

<i>newleng</i>	the distance to the origin (or vector length) on return
----------------	---

4.1.3.4 point3D & point3D::operator*=(const double c)

Multiply by a constant in the sense that this is a vector shortened/lengthed.

Parameters

<i>c</i>	the constant to multiply with
----------	-------------------------------

Returns

the new vector that results

4.1.3.5 point3D & point3D::operator+=(const point3D & right)

Add a vector to define the new location.

Parameters

<i>right</i>	the vector to add
--------------	-------------------

Returns

the new vector that results

4.1.3.6 point3D & point3D::operator- (const point3D & *right*)

Subtract a point to define the difference vector.

Parameters

<i>right</i>	
--------------	--

Returns

the difference vector that results

4.1.3.7 point3D & point3D::operator= (const point3D & *right*)

Assignment Operator.

Parameters

<i>right</i>	the right hand side of the assignment
--------------	---------------------------------------

Returns

the new vector that results

4.1.3.8 void point3D::phithet (double *rtp*[3]) const

Convert point to spherical angular coordinates.

Parameters

<i>rtp</i>	radius, theta and phi on return. $r = \sqrt{x^2+y^2+z^2}$; $x=r \sin(\theta) \cos(\phi)$ $y=r \sin(\theta) \sin(\phi)$ $z=r \cos(\theta)$
------------	--

4.1.3.9 void point3D::scale (const double *radius*)

Scale the points such that those with distance 'radius' appear to be at distance 1

4.1.4 Field Documentation**4.1.4.1 double point3D::xyz[3]**

the 3 Cartesian coordinates.

4.2 poly3D Class Reference**Public Member Functions**

- [poly3D \(\)](#)

- `poly3D (int nl)`
- `poly3D (const int l, const int m, const bool cnots)`
- `poly3D & operator*=(const double cof)`
- `poly3D (const int n, const int l)`
- `poly3D (const int n, const int l, const int m, const bool cnots)`
- `double at (const point3D &pt) const`
- `void gradat (const point3D &pt, double gr[3]) const`
- `int hastype (const int e[TURB3D_DIM]) const`
- `int hastype (const trino3D &t) const`
- `poly3D & operator+=(const trino3D &oth)`
- `poly3D & operator*=(const trino3D &t)`
- `poly3D & operator+=(const poly3D &oth)`
- `poly3D & operator*=(const poly3D &oth)`

Data Fields

- `vector<trino3D> compo`

4.2.1 Detailed Description

Polynomial in 3D

Since

2008-09-24

4.2.2 Constructor & Destructor Documentation**4.2.2.1 poly3D::poly3D ()**

Default ctor.

4.2.2.2 poly3D::poly3D (int nl)

Constructor of a radial polynomial r^{nl} with $r^2=x^2+y^2+z^2$

Parameters

<i>nl</i>	the power of r. Must be an even integer. nl must be an even integer which is not checked in this revision.
-----------	--

4.2.2.3 poly3D::poly3D (const int l, const int m, const bool cnots)

Constructor for a vector Harmonics $r^l Y_l^m$.

Parameters

<i>l</i>	the angular momentum quantum number
<i>m</i>	the magnetic quantum number in the range $0 \leq m \leq l$
<i>cnots</i>	true if this is a cosine type, false if a sine type there is no check that m=0 is only used with cnots equal to true

4.2.2.4 poly3D::poly3D (const int n, const int l)

Constructor for the radial Zernike polynomials $R_n^l(r)/r^l$.

Parameters

<i>n</i>	the main power
<i>l</i>	the angular momentum quantum number

4.2.2.5 poly3D::poly3D (const int *n*, const int *l*, const int *m*, const bool *cnots*)

Constructor for a general Zernike term $R_n^l Y_m$

Parameters

<i>n</i>	the main power
<i>l</i>	the angular momentum quantum number
<i>m</i>	the magnetic quantum number in the range $0 \leq m \leq l$
<i>cnots</i>	true if this is a cosine type, false if a sine type there is no check that $m=0$ is only used with cnots equal to true

4.2.3 Member Function Documentation

4.2.3.1 double poly3D::at (const point3D & *pt*) const

Evaluate it at a point in 3D param pt the location of the 3D point return the value, which is the sum over all terms.

4.2.3.2 void poly3D::gradat (const point3D & *pt*, double *gr[3]*) const

Gradient evaluation at a specified point in 3D space.

Parameters

<i>pt</i>	the point at which the gradient is computed
<i>gr</i>	on return the three components of the gradient

4.2.3.3 int poly3D::hastype (const int *e[TURB3D_DIM]*) const

Test whether a trinomial of an exponential signature is already one of the terms.

Parameters

<i>e</i>	the three nonzero exponents of the reference
----------	--

Returns

the index of the first term of that signature, or -1 if not found.

4.2.3.4 int poly3D::hastype (const trino3D & *t*) const

Test whether a trinomial of an exponential signature is already one of the terms.

Parameters

<i>t</i>	the trinomial of the reference
----------	--------------------------------

Returns

the index of the first term of that signature, or -1 if not found.

4.2.3.5 poly3D & poly3D::operator*= (const double *cof*)

Multiply by a constant

Parameters

<i>c</i>	the constant to multiply with
----------	-------------------------------

Returns

the product that results

4.2.3.6 poly3D & poly3D::operator*=(const trino3D & t)

Multiply all components with the other trinomial term.

Parameters

<i>oth</i>	the trinomial on the right hand side of the equation.
------------	---

4.2.3.7 poly3D & poly3D::operator*=(const poly3D & oth)

Multiply by another polynomial.

Parameters

<i>oth</i>	the polynomial on the right hand side of the equation.
------------	--

4.2.3.8 poly3D & poly3D::operator+=(const trino3D & oth)

Add another trinomial term to this one

Parameters

<i>oth</i>	the trinomial on the right hand side of the equation.
------------	---

Todo allow for annihilation of coefficients and elimination of associated products..

4.2.3.9 poly3D & poly3D::operator+=(const poly3D & oth)

Add another polynomial to this one

Parameters

<i>oth</i>	the polynomial on the right hand side of the equation.
------------	--

4.2.4 Field Documentation**4.2.4.1 vector<trino3D> poly3D::compo**

The individual terms.

4.3 trino3D Class Reference**Public Member Functions**

- [trino3D \(const double c, const int exx, const int exy, const int exz\)](#)
- [double at \(const point3D &pt\) const](#)
- [void gradat \(const point3D &pt, double gr\[3\]\) const](#)
- [bool istype \(const int e\[3\]\) const](#)

- bool `istype` (const `trino3D` &oth) const
- `trino3D` & `operator*=(` (const double c)

Data Fields

- double `coef`
- int `expo` [TURB3D_DIM]

4.3.1 Detailed Description

A term in a 3D polynomial

Since

2008-09-24

4.3.2 Constructor & Destructor Documentation**4.3.2.1 `trino3D::trino3D (const double c, const int exx, const int exy, const int exz)`**

Ctor

Parameters

<code>c</code>	the coefficient in front
<code>exx</code>	the power of x
<code>exy</code>	the power of y
<code>exz</code>	the power of z

4.3.3 Member Function Documentation**4.3.3.1 `double trino3D::at (const point3D & pt) const`**

Evaluation at a specific point in 3D space

4.3.3.2 `void trino3D::gradat (const point3D & pt, double gr[3]) const`

Gradient evaluation at a specified point in 3D space.

Parameters

<code>pt</code>	the point at which the gradient is computed
<code>gr</code>	on return the three components of the gradient

4.3.3.3 `bool trino3D::istype (const int e[3]) const`

Test whether the polynomial is of some type of given exponents. Check whether the current polynomial is compatible with respect to addition.

Parameters

<code>p</code>	the three non-negative exponents of the reference type
----------------	--

Returns

true if the current type matches all three exponents of the reference type.

4.3.3.4 bool trino3D::istype (const trino3D & oth) const

Test whether the polynomial is of some type of given exponents. Check whether the current polynomial is compatible with respect to addition.

Parameters

<i>oth</i>	the trinomial to match against
------------	--------------------------------

Returns

true if the current type matches all three exponents of the reference type.

4.3.3.5 trino3D & trino3D::operator*=(const double c)

Multiply by a constant

Parameters

<i>c</i>	the constant to multiply with
----------	-------------------------------

Returns

the product that results

4.3.4 Field Documentation**4.3.4.1 double trino3D::coef**

The expansion coefficient

4.3.4.2 int trino3D::expo[TURB3D_DIM]

The non-negative powers of x, y and z

4.4 Zern3DRadi Class Reference**Public Member Functions**

- [Zern3DRadi](#) (const int lowIdx, const int upIdx)

Data Fields

- int *n*
- int *l*
- vector< double > *coef*
- int *alpha*

4.4.1 Detailed Description

Zernike 3D radial polynomial

Since

2008-09-25

4.4.2 Constructor & Destructor Documentation

4.4.2.1 `Zern3DRadi::Zern3DRadi (const int lowIdx, const int upIdx)`

4.4.3 Field Documentation

4.4.3.1 `int Zern3DRadi::alpha`

auxiliary mixed excess index

4.4.3.2 `vector<double> Zern3DRadi::coef`

4.4.3.3 `int Zern3DRadi::l`

upper index, representing the family

4.4.3.4 `int Zern3DRadi::n`

main quantum number, lower index

5 File Documentation

5.1 poly3D.cpp File Reference

Functions

- `point3D operator+ (const point3D &left, const point3D &right)`
- `point3D operator- (const point3D &left, const point3D &right)`
- `point3D operator* (const double c, const point3D &right)`
- `ostream & operator<< (ostream &os, const point3D &some)`
- `trino3D operator* (const trino3D &left, const trino3D &right)`
- `ostream & operator<< (ostream &os, const trino3D &some)`
- `poly3D operator* (const poly3D &left, const poly3D &right)`
- `ostream & operator<< (ostream &os, const poly3D &some)`

5.1.1 Function Documentation

5.1.1.1 `point3D operator* (const double c, const point3D & right)`

Multiply length by a factor.

Parameters

<code>c</code>	multiplier.
----------------	-------------

Returns

stretched ($c > 1$) or shranked ($c < 1$) or reverted ($c < 0$) vector.

5.1.1.2 `trino3D operator* (const trino3D & left, const trino3D & right)`

Multiply two 3D trinomials.

Parameters

<code>left</code>	the trinomial left to the multiplication sign
<code>right</code>	the trinomial right of the multiplication sign

Returns

the product. The coefficient is the product of the coeffienst and the exponents are the sums of the individual exponents of x, y and z.

5.1.1.3 poly3D operator* (const poly3D & left, const poly3D & right)

Multiply two 3D polynomials.

Parameters

<i>left</i>	the polynomial left to the multiplication sign
<i>right</i>	the polynomial right of the multiplication sign

Returns

the polynomial which is the sum over all products of the components.

5.1.1.4 point3D operator+ (const point3D & left, const point3D & right)

Add two 3D points in the sense that the first is a point, the 2nd a vector for translation.

Parameters

<i>left</i>	the point/vector left to the summation sign
<i>right</i>	the point/vector right of the summation sign

Returns

the sum. This contains the sum of the two inputs in each component.

5.1.1.5 point3D operator- (const point3D & left, const point3D & right)

Subtract two 3D points in the sense that the first is a point, the 2nd a point and the result is the vector from the second to the first.

Parameters

<i>left</i>	the point/vector left to the subtraction sign
<i>right</i>	the point/vector right of the subtraction sign

Returns

The difference.

5.1.1.6 ostream& operator<< (ostream & os, const point3D & some)

Print a Position.

Parameters

<i>os</i>	the output stream to print to
<i>some</i>	the term to be printed

5.1.1.7 ostream& operator<< (ostream & os, const trino3D & some)

Print a trinomial term

Parameters

<i>os</i>	the output stream to print to
<i>some</i>	the term to be printed

5.1.1.8 `ostream& operator<< (ostream & os, const poly3D & some)`**5.2 poly3D.h File Reference****Data Structures**

- class [point3D](#)
- class [trino3D](#)
- class [Zern3DRadi](#)
- class [poly3D](#)

Macros

- `#define TURB3D_DIM 3`

Functions

- `point3D operator+ (const point3D &left, const point3D &right)`
- `point3D operator- (const point3D &left, const point3D &right)`
- `point3D operator* (const double c, const point3D &right)`
- `ostream & operator<< (ostream &os, const point3D &some)`
- `trino3D operator* (const trino3D &left, const trino3D &right)`
- `ostream & operator<< (ostream &os, const trino3D &some)`
- `poly3D operator* (const poly3D &left, const poly3D &right)`
- `ostream & operator<< (ostream &os, const poly3D &some)`

5.2.1 Macro Definition Documentation**5.2.1.1 #define TURB3D_DIM 3****5.2.2 Function Documentation****5.2.2.1 point3D operator* (const double *c*, const point3D & *right*)**

Multiply length by a factor.

Parameters

<i>c</i>	multiplier.
----------	-------------

Returns

stretched (*c* >1) or shranked (*c*<1) or reverted (*c*<0) vector.

5.2.2.2 trino3D operator* (const trino3D & *left*, const trino3D & *right*)

Multiply two 3D trinomials.

Parameters

<i>left</i>	the trinomial left to the multiplication sign
<i>right</i>	the trinomial right of the multiplication sign

Returns

the product. The coefficient is the product of the coeffienst and the exponents are the sums of the individual exponents of x, y and z.

5.2.2.3 poly3D operator* (const poly3D & left, const poly3D & right)

Multiply two 3D polynomials.

Parameters

<i>left</i>	the polynomial left to the multiplication sign
<i>right</i>	the polynomial right of the multiplication sign

Returns

the polynomial which is the sum over all products of the components.

5.2.2.4 point3D operator+ (const point3D & left, const point3D & right)

Add two 3D points in the sense that the first is a point, the 2nd a vector for translation.

Parameters

<i>left</i>	the point/vector left to the summation sign
<i>right</i>	the point/vector right of the summation sign

Returns

the sum. This contains the sum of the two inputs in each component.

5.2.2.5 point3D operator- (const point3D & left, const point3D & right)

Subtract two 3D points in the sense that the first is a point, the 2nd a point and the result is the vector from the second to the first.

Parameters

<i>left</i>	the point/vector left to the subtraction sign
<i>right</i>	the point/vector right of the subtraction sign

Returns

The difference.

5.2.2.6 ostream& operator<< (ostream & os, const point3D & some)

Print a Position.

Parameters

<i>os</i>	the output stream to print to
<i>some</i>	the term to be printed

5.2.2.7 ostream& operator<< (ostream & os, const trino3D & some)

Print a trinomial term

Parameters

<i>os</i>	the output stream to print to
<i>some</i>	the term to be printed

5.2.2.8 `ostream& operator<< (ostream & os, const poly3D & some)`

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